

AN EVALUATION OF THE USE OF COMBINATION TECHNIQUES IN IMPROVING FORECASTING ACCURACY FOR COMMERCIAL PROPERTY CYCLES IN THE UK

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A thesis submitted in partial fulfilment of the requirements of Edinburgh
Napier University for the Degree of Doctor of Philosophy

September 2014

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Abstract

In light of the financial and property crisis of 2007-2013 it is difficult to ignore the existence of cycles in the general business sector, as well as in building and property. Moreover, this issue has grown to have significant importance in the UK, as the UK property market has been characterized by boom and bust cycles with a negative impact on the overall UK economy. Hence, an understanding of property cycles can be a determinant of success for anyone working in the property industry.

This thesis reviews chronological research on the subject, which stretches over a century, characterises the major publications and commentary on the subject, and discusses their major implications. Subsequently, this thesis investigates property forecasting accuracy and its improvement. As the research suggests, commercial property market modelling and forecasting has been the subject of a number of studies. As a result, it led to the development of various forecasting models ranging from simple Single Exponential Smoothing specifications to more complex Econometric with stationary data techniques.

However, as the findings suggest, despite these advancements in commercial property cycle modelling and forecasting, there still remains a degree of inaccuracy between model outputs and actual property market performance. The research therefore presents the principle of Combination Forecasting as a technique helping to achieve greater predictive outcomes. The research subsequently assesses whether combination forecasts from different forecasting techniques are better than single model outputs. It examines which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best. As the results of the study suggest, Combination Forecasting, and Regression (OLS) based Combination Forecasting in particular, is useful for improving forecasting accuracy of commercial property cycles in the UK.

Declaration

The thesis is submitted to Edinburgh Napier University for the Degree of Doctor of Philosophy. The work described in this thesis was carried out under the supervision of Professor Brian Sloan and Dr. Andrew Brown. The work was undertaken in the School of Engineering and the Built Environment.

In accordance with the regulations of Edinburgh Napier University governing the requirement for the Degree of Doctor of Philosophy, the candidate submits that the work presented in this thesis is original unless otherwise referenced within the text.

The following published papers were derived from the work in this thesis. As set of papers is bound where possible with the thesis and may be found inside the back cover. Full permission from the relevant publishers or copyright holders has been obtained. The numbering sequence makes no attempt to follow that of the thesis proper, the pagination follows that of the parent journal or proceeding as appropriate.

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Abbreviations

| | |
|--------|---|
| ACF | Autocorrelation Function |
| AIC | Akaike Information Criterion |
| AR(p) | Autoregressive (model) |
| ARIMA | Autoregressive Integrated Moving Average (model) |
| ARIMAX | Integrated Autoregressive Moving Average model with Exogenous Explanatory Variable(s) (model) |
| BGS | British Government Securities |
| BIC | Bayesian Information Criterion |
| BLT | Brown's Linear Trend (model) |
| BoE | Bank of England |
| BR | Bank Rate |
| CBHP | CB Hiller Parker |
| CBRE | CB Richard Ellis |
| CCs | Construction Costs |
| COr | Construction Orders |
| COt | Construction Output |
| CSt | Construction Starts |
| DES | Double Exponential Smoothing |
| DW | Durbin-Watson (statistics) |
| E | Employment |
| ES | Exponential Smoothing (model) |
| ESRC | Economic and Social Research Council |
| GDP | Gross Domestic Product |
| GFD | Global Financial Data |
| GNP | Gross National Product |
| HLT | Holt's Linear Trend |
| HMRC | Her Majesty's Revenue and Customs |
| HP | Hodrick-Prescott (filter) |
| HW | Holt-Winters (statistics) |
| IPD | Investment Property Databank |

| | |
|------|--|
| IPF | Investment Property Forum |
| JLL | Jones Lang LaSalle |
| JLW | Jones, Lang & Wootton |
| LCES | London & Cambridge Economic Services |
| LSE | London Stock Exchange |
| MA | Moving Average |
| MAE | Mean Absolute Error |
| MAPE | Mean Absolute Percentage Error |
| ME | Mean Error |
| MFE | Mean Forecasting Error |
| MPE | Mean Percentage Error |
| MR | Multiple Regression |
| MSE | Mean Squared Error |
| MSFE | Mean Square Forecasting Error |
| MSPE | Mean Squared Percentage Error |
| NBER | National Bureau of Economic Research |
| ODPM | Office of the Deputy Prime Minister |
| OECD | Organisation for Economic Co-operation and Development |
| OLS | Ordinary Least Squares |
| ONS | Office for National Statistics |
| PACF | Partial Autocorrelation Function |
| PASW | Predictive Analytics Software |
| RICS | Royal Institution of Chartered Surveyors |
| RM | Regression Model |
| RSS | Residual Sum of Squares |
| SES | Single Exponential Smoothing (model) |
| SPSS | Statistical Package for the Social Sciences |
| SR | Simple Regression (model) |
| UK | United Kingdom |
| US | United States of America |
| VAR | Vector Autoregressive (model) |
| WT | White's Test |

Glossary of property and financial terms¹

| | |
|--------------------------|--|
| Absorption | Total demand for goods and services by all residents (consumers, producers, and government) of a country (as opposed to total demand for that country's output). |
| Autocorrelation | The state of an econometric relation such that some or all of the explanatory variables are highly correlated with each other; poor specification of the relationship between variables in the regression equation is often the cause. |
| Average | A value showing the central tendency of a set of data and often used to compare that set with others. |
| Base rate | The rate of interest that a UK clearing bank uses as the basis of its structure of interest rates for lending and receiving deposits; lending rates are above, and rates on deposits below, base rate. |
| Boom | A period of expansion of business activity. |
| Business cycle | Recurrent but non-periodic fluctuations in aggregate economic activity as measured by fluctuations in real GDP about its trend. |
| Capital consumption (M2) | Depreciation; given that fixed assets have only limited life-span, it is necessary to add to the annual costs of an enterprise or a national economy an estimate of the amount nationally spent on the wear and tear of such assets. |
| Depression | A prolonged and severe slowing-down of economic activity exemplified by mass unemployment and a level of national income well below its potential level; more severe and long-lasting than recession. |
| Finance | The provision of money at the time it is needed. |

¹RICS (1994); Friedman (2000); Rutherford (2002); Dixit (2005); Collin (2007); Communities (2009)

| | |
|------------------------|--|
| Institutional investor | A group of investors who have funds to invest as a consequence of the conduct of their business; the group includes insurance companies, banks and investment trusts, and industrial companies who administer their own pension schemes or have other funds available. |
| Investment yield | Annual rent that is passing as a percentage of the capital value. |
| Macro-economics | A branch of economics concerned with analysis of the economy in the large, i.e. with such large aggregates as the volume of employment, saving and investment, the national income, and so on. |
| Market risk | Risk that results from trends in market prices and which cannot be avoided by diversification. |
| Micro-economics | A branch of economics concerned with analysis of the behaviour of individual consumer and producers, particularly with the optimistic behaviour of individual units such as households and firms. |
| Property cycle | Recurrent but irregular fluctuations in the rate of all-property total return, which are also apparent in many other indicators of property activity, but with varying leads and lags against the all-property cycle. |
| Recession | A significant reduction in employment and production, trade and investment; two consecutive quarters of decline in GDP. |

Acknowledgements

The author would like to use this opportunity to express his gratitude to Professor Brian Sloan and Dr. Andrew Brown, his Research Supervisors, for their patient guidance, enthusiastic encouragement, stimulating suggestions, and useful critiques of this research work. Funding for the project was provided by Edinburgh Napier University. The author would also like to thank Dr. Michael Smyth, Faculty Research Training Co-Ordinator, for the financial support towards tuition fees for Econometrics Summer School at the University of Cambridge. His grateful thanks are also extended to Sheila Sutherland, Fundraising Administrator at International, Development & External Affairs (IDEA), for funding towards Global Chinese Real Estate Congress. Finally, he wishes to thank his wife for her support and encouragement throughout the study. To her, this thesis is dedicated.

CHAPTER 1 INTRODUCTION

1.1 Background for the research

In light of the financial and property crisis of 2007-2013 it is difficult to ignore the existence of cycles in the general business sector, as well as in building and property. Moreover, this issue has grown to have significant importance in the UK, as the UK property market has been characterised by boom and bust cycles with a negative impact on the overall British economy. As a result, economists and scholars started researching this phenomenon in the belief that a better understanding of the cyclical nature of the economy and the property market would prevent cycles from happening in the future.

The nature, development, and reasons behind property cycles have been researched for a number of years (Hakfoort, 1992; RICS, 1993). As Rottke and Wernecke (2002, p.3) observed, 'in the US research on property cycles began as early as the 1930s...The number of publications rose rapidly at the beginning of the 1980s...Up to now in the US and the UK, cycle research papers have increased enormously both in terms of quantity and quality'. According to Barras (2009), the situation changed particularly after the Great Depression when academics and professionals became determined to find ways to prevent the recurrence of such dramatic events in the future. Therefore, they began to focus their attention on investment in building, as the most volatile element of the aggregate economic activity.

The subsequent developments in the field of property cycles research led to the construction of various mathematical models helping to explain the behaviour of the real property market (McDonald, 2002; Tonelli *et al.*, 2004; Barras, 2009; Byrne *et al.*, 2010). As a result, significant progress has been made within property market modelling and analysis (McDonald, 2002) resulting in the development of various forecasting models, ranging from simple single-equation methods to more advanced multi-equation

with stationary data techniques (Tsolacos, 2006; Lizieri, 2009b). The introduction of computer technology further accelerated the modelling process (Ball *et al.*, 1998; Barras, 2009). It therefore led some researchers to propose that the commercial property market movements are predictable (Wheaton *et al.*, 1997; Pyhrr *et al.*, 1999; Barras, 2009).

However, comparative studies, where authors assessed the accuracy of already produced forecasts with actual property market dynamics, suggest that despite these advancements, there still are inaccuracies within property market modelling and forecasting. Various factors were identified why models differ from actual property market performance. These were market uncertainty, object being forecasted, forecasting technique used, forecasting horizon, and data being employed (Newell *et al.*, 2002; Tonelli *et al.*, 2004; McAllister and Kennedy, 2007; IPF, 2012). Accordingly, it was suggested that greater forecasting performance could be achieved if any or all these forecasting inaccuracy causes are addressed.

1.2 Aims and objectives of the research

This research project aims to improve the forecasting accuracy of UK commercial property cycles. It therefore adopts the principle of Combination Forecasting as a means of improving overall modelling and forecasting accuracy. Researchers including Makridakis (1989), De Gooijer and Hyndman (2006), Goodwin (2009), Pesaran and Pick (2011) and Wallis (2011), were motivated by this concept and suggest that greater predictive results can be achieved from a combination of different methods and sources. Therefore, the principle of Combination Forecasting, which was developed by economists, has now been applied to UK commercial property market cycle analysis.

To complete this aim successfully, the following research objectives are set:

- i) Examine the key components of business and commercial property cycles and review the research and commentary on the subject chronologically;
- ii) Assess existing modelling and forecasting practices within the field of commercial property market research and explore the application of the principle of Combination Forecasting as an alternative methodology for UK commercial property cycle forecasting accuracy improvement;
- iii) Examine properties of the dependent and explanatory variables and present their key characteristics;
- iv) To draw conclusions from the data analysis and assess as to whether Combination Forecasting improves UK commercial property cycle forecasting accuracy;
- v) To draw conclusions on the data analysis and assess as to whether Combination Forecasting improves UK commercial property cycle forecasting accuracy;

- vi) To identify practical implications of this research project for commercial property market participants.

1.3 Methodological considerations

A multi-strand approach is proposed to address the objectives of the research. Initially, the study critically reviews the literature on the subject. A literature review presents how understandings of the property cycles have evolved over time, what the critical issues at each stage of cycle research were, and what the key considerations currently are. It allows for an assessment as to how the understanding and a critical analysis of the subject have changed over the century, and how the current investigation relates to previous studies. It then provides a rationale for the current study by revealing the contribution that the research makes to current knowledge.

The study then uses econometric modelling to assess potential improvements to the accuracy of UK commercial property cycle forecasting. The study selects key property market modelling techniques, including Exponential Smoothing, ARIMA/ARIMAX, Simple Regression, Multiple Regression and Vector Autoregression approaches. Following on from this, it then employs Combination Forecasting. There is a suggestion that forecasters and decision makers discover the best performing model, which is then accepted and used, while rejecting other alternatives. However, the aim of the research is to obtain the most accurate forecast. Therefore, discarding alternative models is unproductive. What is more, there is a difficulty in deciding which model to choose when different specifications suggest different results. As such, Combination Forecasting eliminates these modelling deficiencies and provides a solution in improving overall forecasting accuracy.

1.4 Outline of the thesis

Chapter 2 discusses Efficient Market Hypothesis and its links with the property market. It assesses the key characteristics of business and property cycles. It then examines similarities between business and property cycles and presents the pattern of an idealised property cycle. Subsequently, it reviews the research on the subject chronologically, over a one hundred year span, characterising the major publications and commentary on the subject, and discussing the major implications. Following on from this, it investigates property forecasting accuracy and its improvement. It suggests that property cycle research resulted in the development of various forecasting models ranging from single exponential smoothing specifications to more complex structural with stationary data techniques. However, the findings indicate that despite these advancements in property market modelling and forecasting, there still remains a degree of inaccuracy between model outputs and actual property market performance.

Chapter 3 discusses difficulties related with use of different forecasting methods and then presents the principle of Combination Forecasting as a robust way of improving commercial property market modelling and forecasting. It covers the general principles of model implementation using the statistical software package PASW 18 (SPSS 18). It also assesses the issue of modelling using spread-sheets. Following on from this, the Chapter presents each modelling technique used for the research, including Single Exponential Smoothing (SES), Holt's Linear Trend (HLT), Brown's Linear Trend (BLT), ARIMA, ARIMAX, Simple Regression (SR), Multiple Regression (MR), and Vector Autoregression (VAR). It also considers the principle formulae for Simple Averaging and OLS based Combination Forecasting (CF). Subsequently, the Chapter addresses statistical difficulties related to the construction of a real estate model.

Chapter 4 discusses the importance of long-term series in analysing property cycles. It assesses difficulties related to UK property data and its

acquisition. It then presents the principle of Chain-Linking as the solution for time-series combination. Following on from this, Chapter evaluates properties of the dependent and explanatory variables. Subsequently, it presents five variable reduction techniques which are employed to select the key variables for modelling.

Chapter 5 reports the empirical findings of the study. It presents estimates obtained using each modelling technique, as well as Combination Forecasting. Modelling accuracy in- and out-of-sample is discussed along with a graphical presentation of the findings. Chapter then analyses and interprets results. It transforms the modelling estimates obtained into credible evidence about UK commercial property market modelling and forecasting, and its accuracy improvement through Combination Forecasting.

Chapter 6 concludes the thesis. It presents the key findings and implications of the research for commercial property market stakeholders, critically evaluating them and then proposing avenues for further work.

CHAPTER 2 LITERATURE REVIEW

The objective of this chapter is to review the literature concerning property cycles, modelling and forecasting. It is divided into three sections.

Section 1 starts with a discussion on Efficient Market Hypothesis and its relation to fluctuations in real estate. The findings support the idea that asset markets, and property market in particular, are inefficient. Imperfect information, high levels of transaction, production time lags, are just a few facts which add to inefficiency and therefore market cyclicity. The section then characterises business and property cycles. It presents the pattern of an idealised property cycle and discusses similarities between business and property cycles. It then examines key publications on the subject and assesses how understanding of the property cycles has evolved over time. The discussion is divided into five principal parts which follow so called 'property cycles research eras'. 'The Early Studies' part reviews the earliest publications on the subject. Then follows 'Post-War studies' or as Barras (2009) calls it 'empirical work' period. This section concentrates on three key publications on the subject, one from the UK and two from the US, which offered a comprehensive analysis of the subject at that time. Subsequently, the 'Post-1970s Crash Period Studies' part assesses publications produced over the 1980s and explores the key findings of that time. Following on from this, the 'Post 1990s Property Crash' studies are examined. Finally, the so called 'Modern Studies' part assesses the most recent publications on property cycles.

Section 2 examines the issue of property market modelling. It assesses different property market modelling classifications discussed in the literature. It then presents a group of quantitative real estate forecasting methods and reviews their key characteristics. Subsequently, it discusses further issues in modelling, including stationarity and unit-root testing, Granger causality, and accuracy.

Section 3 assesses the accuracy of property market forecasting. It reviews studies on the subject where forecasters assessed the predictive capacity

of their models by comparing them with actual property market performance. It then examines studies on indirect accuracy measurement where researchers assessed the accuracy of already produced forecasts by comparing them against established property market benchmarks.

2.1 Property and business cycles

2.1.1 Property market (in)efficiency

The Efficient Market Hypothesis (EMH) suggests that financial markets are information efficient. This means that markets adjust rapidly to new information (Fama et al., 1969). As such, prices of traded assets including corporate stocks, commodities, or real estate (Shiller, 2014) are well known in advance (Maier and Herath, 2009). Therefore investors cannot gain advantage in predicting future direction of these assets using publically available information (Cho et al., 2007). The principle behind EMH is random walk process. In his empirical study, Fama (1970) demonstrated that day-to-day price changes and returns on common stocks follow a random walk with their autocorrelations being close to zero, which means that their future prices cannot be predicted based on past information.

However, there is a body of knowledge suggesting just the opposite (Ding et al, 1993; Cho et al., 2007). Researchers are commenting that although EMH is plausible, there are a number of difficulties related to it (Beechey et al., 2000; Maier and Herath, 2009; Shiller, 2014). In property market research, as Maier and Herath (2009) comment, there are two major issues which need to be considered. The first issue relates to information. The second involves price volatility and cycle analysis.

Regarding information and property market (in)efficiency, Brown (1991), Evans (1995), Kummerow and Lun (2005) and Maier and Herath (2009) commented on the essential relationship between two facets. According to Smullyan (1994) and Kummerow and Lun (ibid.), property has always been an 'information business'. The information within the industry has always been 'thin'. Intrinsic property asset characteristics such as heterogeneity and low trading frequency combined with insider information add to the magnitude of price changes within the sector. All this combined can destabilise the overall economy. These suggestions corroborated

earlier observations of Grossman (1978) and Grossman and Stiglitz (1980) who commented on information and market efficiency. According to both commentators, 'informationally' efficient markets are impossible. If markets were perfectly information efficient, returns on gathering and analysing this information would be nil. This would make asset trading obsolete. Therefore, the market would eventually collapse.

In terms of volatility, cycles and bubbles and their link with information asymmetry, Shiller (2014, p.21) in his Nobel Prize lecture, documented that real estate 'prices are not at all well approximated by a random walk, as is the case for stocks, but often tend to go in the same direction, whether up or down, again and again for years and years'. What Shiller meant is that for 'smart money' to go in and out in the real estate market in response to news is impossible. This proposition was argued by Malpezzi and Wachter (2005) a decade ago. According to commentators, real estate prices are prone to cycles due to information arbitrage. Discovering prices is expensive, as such, prices become volatile. Similar findings were presented by Ball (2006) who argued that, on a European level, house prices varied over time implying market inefficiency. This therefore leads to boom-and-bust cycles in the property market.

Taken together, the discussion above suggests that market efficiency is important. Debates have continued for several decades. Thought results are inconclusive. However, the overriding idea is that asset markets, and property markets in particular, are inefficient. Imperfect information, low levels of transaction, and production time lags, are just a few factors which add to inefficiency and therefore property market cyclicity.

The following section discusses the key characteristics of the business and property cycle and the way they link together. It also presents a summary of the findings from property cycles research over a hundred year period.

2.1.2 Characterisation of the business and property cycle

The existence of cycles in the general business sector, as well as in building and property has been debated for more than a century (Mangoldt, 1907; Cairncross, 1934; Gottlieb, 1976; Hakfoort, 1992). According to Barras (2009, p.4), property cycles 'have been recorded throughout history'. However, as Cairncross (1934) observed, they have been neglected by researchers, their statistics unassembled, and their organisation practically unknown. The situation changed after the Great Depression when academics and professionals determined to find ways to prevent the recurrence of such severe economic causalities in the future. Therefore, as Barras (ibid.) suggested, focus shifted into building investment, as the most volatile element of aggregate economic activity.

The subject has grown to a significant importance in the UK, as the UK property market has been characterised by boom and bust cycles with a negative impact on the overall British economy. As a result, property cycles became a popular research topic amongst property professionals and scholars, with a greater understanding of the cyclical behaviour of the property market being seen as a major guide to the financial success (or failure) of property investments (Pyhrr *et al.*, 1999; RICS, 1994, Barras, 2009). This subsequently led RICS (1994; 1999) and Baum (2001) to suggest that the concept of cycles is firmly embedded within property research.

Commentators, including Ball *et al.* (1998) and Barras (2009), argue that property cycle formation theories are mostly derived from business cycle research. As their studies show, the correspondence between property and business cycles is in the way both phenomena are defined, i.e. linguistic issue; the way they are expressed, i.e. visual issue; as well as in the way they are constructed, i.e. theoretical issue.

According to the standard definition of the business cycles presented by Parkin and Bade (1988, p.31), 'business cycles are recurrent but non-periodic fluctuations in aggregate economic activity as measured by

fluctuations in real GDP about its trend'. Following the RICS' (1994, p.9) definition of property cycles (which is now generally accepted within the property community) 'property cycles are recurrent but irregular fluctuations in the rate of all-property total return, which are also apparent in many other indicators of property activity, but with varying leads and lags against the all-property cycle'. As these definitions suggest, both phenomena are expressed as recurrent, however irregular fluctuations. What is more, they are quantitatively defined, i.e. the business cycle is measured as fluctuations in GDP, while property cycles are measured as fluctuations in the rate of All-Property Total Returns.

The similarity between business and property cycles is also visually observed. The idealised property market cycle is perceived as a four phase nomenclature which is similar to that of the business cycle (Mueller, 1999; Pyhrr *et al.*, 1999). Both business and property cycles follow four major phases: recession (trough), recovery, expansion (peak), and contraction. 'Peak' and 'trough' are the major turning points of the cycle. Peak constitutes the end of 'expansion' and the beginning of 'recession', and 'trough' – the end of recession and the beginning of 'expansion' (Zarnowitz, 1992; Su, 1996). What is more, both concepts are expressed as a sine wave which deviates around its equilibrium. This interrelationship is illustrated in the 'Schematic diagram of recurrent fluctuations in economic activity' (Figure 2.1) and idealised 'Property cycle phase nomenclature' (Figure 2.2).

However, not all property researchers adopted the same cycle nomenclature. Commentators including Roulac (1996) and Hewlett (1999) identified the sequence of the property cycle somewhat differently. Roulac (1996) presented the property cycle as a sequence of expansion, slowing, contraction, correction, recovery, and again expansion. Hewlett (1999) saw a property cycle as a three phase framework consisting of upturn, maturity and downturn. Nevertheless, as Ball *et al.* (1998) commented, the pattern of an idealised property cycle is still the same despite a terms to describe them.

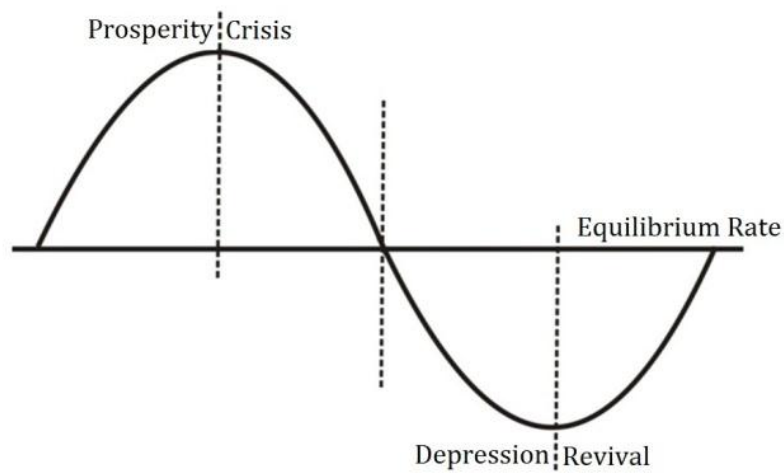


Figure 2.1 Schematic diagram of recurrent fluctuations in economic activity
Adapted from: Frank (1923)

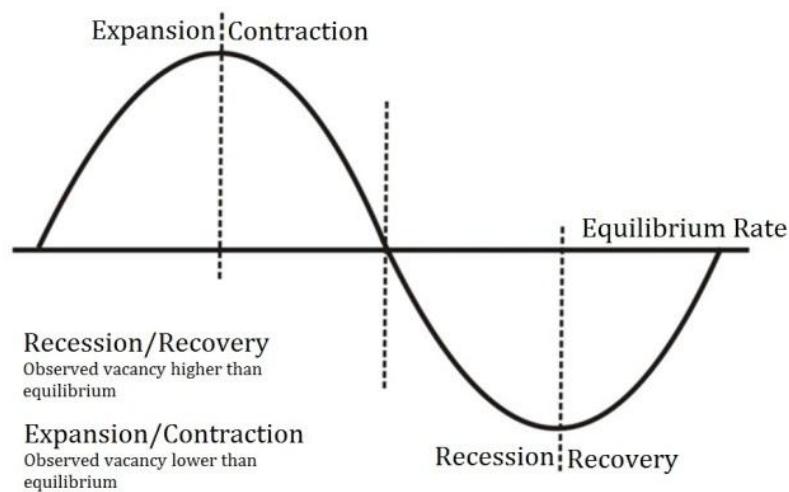


Figure 2.2 Property cycle phase nomenclature
Adapted from: Pyhrr *et al.* (1999)

As it was noted above, the relationship between property and business cycles is also evident in the way property cycles are characterised. According to Ball *et al.* (1998), the pattern of the idealised property cycle is as follows:

- *Business upturn and development*: an increase in the economic activity generates strong user demand for space; existing space is absorbed quickly; vacancy rates fall and rents rise; this thus works as a signal for new property developments to begin;
- *Business downturn and overbuilding*: business cycle turns downwards which reduces demand for space; however, new stock reaches the market (normally it takes few years to build the building); as a result, vacancy rates rise and rents fall;
- *Adjustment*: following on from this, growing vacancy rates trigger further falls in rents; developers and investors are unable to generate income from properties they hold. This leads to a series of bankruptcies;
- *Slump*: both demand for space and development activity are at their lowest levels, with vacancy rates being above equilibrium level and rents being below equilibrium level.
- *The next cycle*: when the next business upturn occurs, there is still a substantial level of vacant space available from the previous cycle, which implies limited need for new developments.

In general, this simple explanation of the property cycle suggests that the property cycle is a product of overall business dynamics. The hypothesis is that cyclical fluctuation in business activity generates demand for and production of property and *vice-versa*, which comes from the necessity to occupy property to undertake activity (Ball *et al.*, 1998). However, the idea that property and business cycles are interlinked with each other was not argued until more recently (Ball *et al.*, 1998). The developments in understanding of property cycles are described in greater detail in the following section.

2.1.3 Understanding of the property cycle

Early studies

The first serious discussions and analyses of property cycles emerged during the late nineteenth and early twentieth century. As Gottlieb (1976) and Barras (2009) indicated, German scholars were pioneers of property cycle research. The major object of their investigations was the urban growth of German cities and its impact on residential construction, property market activity and land values. In his general work, Mangoldt (1907) demonstrated the tendency for urban growth to run in long waves in the city of Freiberg. Reich (1912) investigated the residential market in Berlin between 1840 and 1910. Eychmüller (1915) studied the economic development, urban land and building policies of the city of Ulm for the period 1850-1919. In her manuscript, Carthaus (1917) assessed the history of the land crisis in German big cities with a special emphasis on Greater Berlin. Eisenlohr (1921) in his study discussed urban and housing conditions of the city of Mannheim. These studies were subsequently followed by the researchers from other metropolitan areas.

It is considered that in the US research on the subject started in 1933 with Hoyt's publication. In his book Hoyt investigated cyclical fluctuations of the Chicago property market. Generally, Hoyt suggested that business conditions, commodity price levels, value of money and especially a rapid increase in population within a relatively short period of time were the major causes of the real estate cycles. The author affirmed that past property cycles were mostly generated by the sudden and unexpected increase in population seeking greater industrial opportunities within the area. It therefore led Hoyt to hypothesise that future property cycles would be generated by the identical increase in population, which would result from an expansion of industrial opportunities. Accordingly, he identified relatively long and uncertain (on average 18 years) real estate cycles. These observations add to Wenzlick's (1933) findings, who identified similar cycles for St. Louise, and Maverick's (1933) observations, who

estimated similar real estate fluctuations for Los Angeles and San Francisco.

In the aftermath of the Great Depression, Newman (1935) further investigated building cycles. In his monograph, the author stressed that 'it is highly important that the nature of, and reasons for, fluctuations in such activity be subject to rigorous inductive and deductive analysis' (ibid., p.2). The building industry was chosen due to its size and importance to the US economy, and the number of people employed. As Newman estimated, building comprised around 50 percent of the total US economy. He therefore expected fluctuations in private building to have a major effect on the economy. Newman used the term 'building industry' to refer to durable and fixed goods which provide shelter to individuals and businesses. His empirical estimates were based on the building activity index which was comprised from the dollar value of the building permits. The outstanding characteristic of this research was identification of so called 'major cycles', lasting between fifteen to twenty-one years. The other findings included a tendency for the building cycle to precede the business cycle (business lagged three months behind building) and considerable independence between movements of the two series. Newman also stressed a close relationship between building and population. However, he appreciated that factors such as availability of capital, or general business conditions play an important role in this process. He therefore concluded that 'fluctuations in building activity were found to be closely associated with shifts in population ... and these shifts in population are, of course, reflections of economic and social alterations which make a change of residence desirable to a larger number of people' (ibid., p.56).

A significant contribution towards the research and understanding of building cycles was made by the American economist Clarence D. Long, Jr. In 1936, Long published a study on the building industry of Manhattan in which he explored the major components of the industry of that time. His statistical analysis suggested the existence of two types of building

cycles, .i.e. major cycles of a period between 15 to 20 years, and minor cycles of around 5 years in length.

After this study on a local building market, Long (1939) published an article on national building activity. This study comprised both residential and non-residential building indices of the US for the 1856-1935 period. The value-index included 27 and the number-index included 29 of the most populous cities of the country. Similar to Newman (1935), Long (ibid.) pointed out that major building cycles were somewhat independent of the business cycle. He also hypothesised that building cycles precede the general business cycles in the downturn, however lag in the upturn. Subsequently, Long (ibid.) identified 18-19 years building cycles in both residential and non-residential building.

A year later, Long (1940) published, as some authors (e.g. Singer, 1942; Barras, 2009) indicate, a second major study on the subject after Hoyt's Chicago case study. For his analysis Long constructed a monthly Index of Building for the period between 1868 and 1940, which was based on the local figures of building permits. The results of the statistical analysis led him to identify short building cycles of an average of 4 years duration, and long cycles of around 20 years in length. To substantiate his findings, Long referred to previous studies on the subject, including Hubbard (1924), Clark (1934), and Newman (1935) who identified similar building cycles.

One of the first studies on the UK building cycles was that of Cairncross (1934). In his analysis of the Glasgow building industry (1870-1914), which was considered at that time as probably the best documented property market in the UK, Cairncross identified that demand for housing 'naturally fluctuate with the number and incomes of potential tenants' in around every twenty years (ibid., p.4). Similarly to Wenzlick (1933), Cairncross noted that the marriage-rate and migration all have a significant effect on building cycles.

With regard to research on the subject in the United Kingdom, the same year as Cairncross (1934) published his research on the Glasgow building industry, Shannon (1934) produced a Building Index (index of brick production) for England for the period between 1785 and 1850. Statistical analysis of the data led the author to identify 16 year-long building cycles, which were closely linked to population growth.

In 1937, Bowley published an investigation into fluctuations of the house-building and trade cycles for the 1924-1936 period for England and Wales. Her analysis led to the conclusion 'that there has been little causal connection between the trade cycle and house-building activity since the War [WWI]' (ibid., p.181). Population change was identified as the primary factor influencing demand for housing.

A more robust discussion on the building and trade cycle was presented by Bowen (1940). His national investment analysis covered the 1924-1938 period for all the UK. Bowen compared three series: Building Plans Passed, Ministry of Health Returns of Houses Completed, and Ministry of Labour Insured Unemployment Returns for the Building Industry. The results of the study suggested that building activity and the general trade cycle are interconnected.

Table 1 summarises the key publications on property cycles during this research era. It contains title, data and data analysis techniques which were employed by researchers, as well as outcomes of these studies. The following section reviews the key publications produced during the post-war period.

| Publication | Data employed | Statistical technique | Outcomes of the Study |
|---|---|--|--|
| Hoyt, H. (1933) One hundred years of land values in Chicago. The relationship of the growth of Chicago to the rise in its land values, 1830-1933. The University of Chicago, US, pp.452 | Land values; New construction; Lots subdivided; Public improvements; Population; Foreclosures; Real estate transfers; Bank clearings; Canal-rail stock prices; Wholesale commodity prices | Data comparison; Turning point analysis; Time-series analysis (1830-1933); Visual data analysis (of maximum and minimum) | 18 years building cycles; Real estate cycles may be a passing phase |
| Cairncross, A.K. (1934) The Glasgow Building Industry (1870-1914). The Review of Economic Studies, Vol.2, No.1, pp.1-17 | House building and demolition; Rents; Site values; Heavy industry activity; Interest rates; Population (rate of marriage and immigration) | Data comparison; Turning point analysis; Time-series analysis (1870-1914); Visual data analysis (of maximum and minimum) | 20 years building cycles; Real estate cycles have a great correlation with population |
| Newman, W.H. (1935) The building industry and business cycles. University of Chicago Press, Chicago, pp.72 | Building permits; Building costs; Population growth; Bond yields; Rents; Operating expenses; B.B.N index | Time-series analysis (1875-1933); Turning point analysis; Correlation analysis; Index composition | 15-21 years 'major cycles'; 4-5 years 'minor cycles'; Building cycles precede business cycles; Independence between movements of two series; Constant correlation between building space and population |
| Long, C.D., Jr. (1940) Building Cycles and the Theory of Investment. Princeton University Press, NJ, pp.239 | Gross capital formation; Total construction; Building costs; Incomes; Interest rates; Building levels; Population; Taxes; Housing costs | Time-series analysis (1868-1940); Turning point analysis; Simple mathematical calculations (averages, deviations, medians); Correlation analysis; Assumption testing; Index composition; Index smoothing (by means of the Macaulay 43-term graduation) | 4 years short building cycles; 20 years long building cycles; Greater volatility of cycles in building than in business; Building cycles precede business cycles; Correlation between long building cycles and the general business conditions |
| Bowen, I. (1940) Building Output and the Trade Cycle (U.K. 1924-38). Oxford Economic Papers, No.3, pp.110-130 | Building plans passed; Returns of houses completed; Insured unemployment returns for the building industry; Savings | Time-series analysis (1924-1938); Correlation analysis; Data comparison; Visual data analysis; Data smoothing (3 year moving average); Trend analysis | Correlation between building an population; A greater role of building within the economy |

Table 2.1. Key 'Early era' publications on property cycles

Post-War studies

During the 1930's there were a number of studies and publications produced on building cycles. However, the post-war period saw a decline in the volume of research on the subject. As Lewis (1960) and more recently Barras (2009) noted, individual studies such as Grebler (1954) or Cairncross and Weber (1956) were published, which mostly repeated the major studies of the 1930's only by adding newer data or extending the statistics of their predecessors.

One of the first attempts to renew the discussion on the subject was Lewis' (1960) empirical study. In this work, he proposed a theoretical dynamic regional building model. Regional building cycles were identified as the major elements of the total building cycle mechanism. Lewis (*ibid.*, p.533) pointed out that 'there can be no national building boom without there being at least one local boom, and the justification for a local boom must lie in local need'. Lewis hypothesised that national building booms occur at a time when several regional building booms coincide with each other purely by accident or during a period of national prosperity.

The importance of local building activity was also addressed by Saul (1962). His investigation into house building activity in England between 1890 and 1914 led to the conclusion that investment in housing 'was largely determined by causes special to the domestic housing market' (*ibid.*, p.120).

In 1965, Lewis published a major study - a historic survey of British economic growth from 1700 to 1950. In this publication, Lewis investigated the existence of the long building cycles. First, he undertook a historical review of the UK building industry. He then created a mathematical simulation model to test his hypotheses. The identification of building cycles of 18 to 20 years in duration was one of the central findings of the book. Lewis argued that building cycles were generated by a number of endogenous and exogenous factors. The endogenous factors which Lewis considered were level of production, income, population structure,

migration, credit supply, and rent level. The key exogenous factors which the author emphasised were war and the level of harvest. Lewis appreciated the interconnection between these factors, as well as the economic context within which they occur. This led Lewis (ibid.) to suggest that, as these factors varied significantly over time, each building cycle was unique with its own inherent characteristics. Subsequently, study has shown that demand for building is a function of local factors, e.g. building activity in Manchester was linked to levels of the cotton industry, while in South Wales it was related to the coal trade, with both industries being the key to the region. What is more, two key factors, i.e. credit conditions and population in particular, were articulated by the author. According to Lewis, internal migration, emigration, and changes in the family structure were all powerful factors in determining housing demand.

Abramovitz (1964) published one of the major post-war studies on the subject in the US. As the author indicated, the purpose of this monograph was to 'review and assess the evidence bearing on the existence of long waves in aggregate construction and in the major types of construction activity in the United States' (ibid., p.1). The construction industry was chosen because of its size and importance to the US economy. The statistical analysis of the 38 annual time-series enabled Abramovitz to identify long waves in aggregate construction of duration between 15 and 25 years. Uniform long swings were also found in the other major areas of the American economy, including population growth and immigration, volume of import, and railroad development. Abramovitz therefore attributed the existence of long cycles within construction activity to the dynamics in the general economy, demographics and trade.

The study by Gottlieb (1976) offered probably the most comprehensive empirical analysis of the subject at that time. In this book, Gottlieb assessed the time-spread of long urban-building fluctuations in the US. Gottlieb then compared the dynamics of the building industry with the general business cycle, as well as with fluctuations of economic series in other countries. For his research Gottlieb employed over 200 long time-

series produced by the NBER on building, finance, demographics and real estate activities for the US, UK, Sweden, France, Australia, Netherlands, Germany, Canada, Italy, and Japan. The study suggested the existence of long building swings in modern capitalistic societies and apparent synchronisation between local and national cycles. What is more, the results of this study suggested that both long local and national building cycles were virtually of the same duration. According to Gottlieb's statistical analysis, the average length of long local building cycles was 19.7 years, and the average length of long national building cycles was 19.0 years. The argument behind these findings was that 'local cycles were simply a local phase of a national movement, while the national movement was in turn mainly a coalescence of local cycles' (ibid., p.9). Another important finding which emerged from the study was the relationship between building cycles and demographic changes. According to Gottlieb, favourable economic conditions encourage or discourage formation of new households, which consequently has a direct effect on the volume of demand for additional dwellings. This demand also affects old stock, land and credit markets. All this in combination triggers greater building and real estate market activity.

Table 2 summarises the key publications of this research period, which includes title, data and data analysis techniques employed and outcomes of these studies. The following section presents the key post-1970s crash studies on property cycles.

| Publication | Data employed | Statistical technique | Outcomes of the Study |
|--|---|---|--|
| Abramowitz, M. (1964) Evidences of Long Swings in Aggregate Construction since the Civil War. National Bureau of Economic Research, New York, pp.252 | 38 series on non-farm residential, private non-residential, farm, public and ship building, and transportation and public utilities | Data comparison; Time-series analysis (1870-1955); Turning point analysis; Visual data analysis (of maximum and minimum, and peaks and troughs); Data smoothing (5 and 10 year moving average); Amplitude measurement. | 15-25 years building cycles; Close interaction between building and the economy; Structural change of the US economy leads to demise of cycles |
| Lewis, P.J. (1965) Building Cycles and Britain's Growth. Macmillan, London, pp.396. | 20 time-series (import/export, building, marriage rate, bank rate, house prices, rents, etc.) | Time-series analysis (1700-1950); Turning point analysis; Correlation analysis; Index creation (artificial time-series); Probability modelling (experiments with multiplier-accelerator mechanism) | 18-20 years building cycles; Correlation between building and population and credit; Building is a function of the local factors |
| Gottlieb, M. (1976) Long Swings in Urban Development. National Bureau of Economic Research, New York, pp.360 | Around 200 long time-series (building, building costs, population, land values, etc.) | Time-series analysis (1840s-1930s); Comparison/Visual inspection; Smoothing (Time-series decomposition/Fixed term moving average); Turning point analysis; Correlation analysis; Data comparison; Visual data analysis (of maximum and minimum, and peaks and troughs); Amplitude measurement | 20 years building cycles; Correlation between building and population, as well as local and national cycles |

Table 2.2. Key post-war publications on property cycles

Post-1970s crash studies

According to Barras (2009), the 1960s was a period of apparent economic stability. It therefore led some commentators, including Abramovitz (1968) and Bronfenbrenner (1969), to question whether cycles were still relevant. However, the property market crash of the mid 1970s triggered a renewed wave of research on property cycles. As Barras (1994) indicated, his personal interest on the subject was first prompted by the 1970s property crash, which led to the publication of a number of papers including Barras (1983; 1984; and 1987), as well as a series of papers commissioned from the Economic and Social Research Council (ESRC) on building cycles in Britain, i.e. Barras and Ferguson (1985; 1987a; 1987b).

Barras (1983, p.1) proposed 'a simple theoretical model of the office development cycle' for Britain. He employed an accelerator type model and, by incorporating a long term production period between building order and its completion, explained how cycles are generated around their equilibrium growth path. The model was then tested in reality and compared with the results of previous empirical investigations.

Barras (1984) examined the major characteristics of the London office market. The researcher discussed the main factors which governed the growth of London as an international office centre. Subsequently, he illustrated the apparently cyclical nature of office development in the city. He then briefly reviewed development control policies, identifying difficulties associated with existing control strategies, and their effect on the property development industry. Finally, Barras assessed the 1980s development cycle. He particularly emphasised the impact of information technologies on user demand for London offices in the post 1980s development cycle.

Barras (1987, p.1) investigated 'urban development cycles' in Britain and their links with technological changes. According to the author, long swings of 20-30 years duration are normally generated by shorter cycles, i.e. two shorter cycles are generally superimposed by the dominant long

swing, causing pronounced building cycles. The author also suggested that building activity is particularly prone to cyclical fluctuations in comparison with other capital investment classes.

A significant analysis and discussion on the subject was presented by R. Barras and D. Ferguson in their three stage research project. In the first paper, Barras and Ferguson (1985) investigated the detailed chronology of five major building sectors including private industrial, private commercial, private housing, public housing, and other public building. The authors employed spectral analysis to determine and compare each building series, their cyclical characteristics, and relationships between the cycles. What is more, informal turning point analysis was used to identify the precise chronology of each cycle. It all allowed Barras and Ferguson to suggest that UK post-war building experienced 'strong cycles', i.e. 'short cycles' of 4 - 5 years, 'major cycles' of 7 - 9 years, and 'long swings' of 28 years within housing investment and 19 years within other building. Short cycles were linked to general business cycles, major cycles – to production lags within the construction industry and public expenditure policy, and long swings – to 'major waves of urban development' (ibid., p.1389).

In the second paper Barras and Ferguson (1987a) developed a theoretical dynamic model of property cycles. The model incorporated both endogenous and exogenous elements of the built environment. Endogenous mechanisms were related to the production lag within the industry. The exogenous influences were associated with variations in economic activity, particularly in the GDP and bank interest rate. The researchers assessed industrial, commercial and residential property sectors. As the authors indicated, public building was excluded as this type of property 'reflects not so much the dynamics of market behaviour, but rather the periodic shifts in public investment which result from changes in government policy' (ibid., p.353). The theoretical dynamic model was based on Box and Jenkins (1976) (ARIMA) time-series modelling technique. The researchers also included an error-correction

element into the framework in order to derive short-run adjustment dynamics and long-run equilibrium relationships between time-series. The user activity, which generated demand for space, was identified as being accountable for long-run equilibrium of property development, which at the same time is proportional to net investments in new buildings. Short-term property market dynamics was found to be highly dependent on exogenous variables, including building costs, property market prices, rents and yields, availability of finances, and financial performance of other types of long-term investments.

In the concluding paper, Barras and Ferguson (1987b) presented empirical results of their research for each property sector (private industrial, commercial and residential). As the results suggested, the equilibrium level of industrial and commercial property is dependent on the level of user activity which creates demand for this type of property. The residential property was identified as being a subject of investment activity. The commentators also identified that all types of property have one common component – construction lag, which serves as an endogenous cycle mechanism. This construction lag was distinguished as being the key driver behind the major cycle of a period of 35 quarters (8 years). The user activity, which generates fluctuations within business cycles, was identified as being the main exogenous mechanism which governs short building cycles within all types of property. It was also detected that user activity has links with movements in the level of GDP and investment activity. Development costs were identified as having the least impact on building cycles.

In the US, studies on the subject continued to be influenced by the NBER research agenda. In their publication, Grebler and Burns (1982) investigated short-term post-war cycles in the US construction sector following the established NBER methodology. The authors related these cycles to business fixed investment and 'reference cycle' in GNP. Their research concentrated on four key aspects. It assessed whether cycles became more severe over time, examined the impact of public activity on

cycles, appraised the relationship between business and construction cycles, as well as evaluated whether construction cycles lead or lag the general business cycles. The data for the study covered the 1950-1978 period. The empirical analysis of duration, amplitude and number of cycles led the authors to identify six cycles in private residential construction (18 quarters on average), four in private non-residential (29 quarters in average), and four cycles in state and local construction (28 quarters in average). The analysis also suggested that these cycles were generated by their own inherent characteristics and determinants.

In the US the post-1970s crash studies particularly concentrated on the office market and its dynamics. According to Wheaton (1987), Clapp (1993) and Barras (2009), this particular asset class attracted great attention due to its expansion in the late 1980s. Moreover, this market segment exhibited high levels of volatility in comparison to other types of commercial property.

One of the key studies was Wheaton's (1987, p.1) investigation into 'the cyclical behaviour of the national office market'. In this research, Wheaton assessed the post-war US office market and identified the existence of the recurrent ten years 'national office market cycles' (ibid., p.283). Wheaton analysed data for the 1960-1986 period for national office employment, building starts, building completions, absorption, and vacancy rate. He also compared historic office vacancy rates amongst ten major US cities. Time-series analysis suggested that exogenous impulses from the wider economy had a greater impact on office cycles than endogenous 1-2 years construction lag.

The dynamics of the US office market was further investigated by DiPasquale and Wheaton (1992) and Clapp (1993). In their article, DiPasquale and Wheaton (1992) developed a universal equilibrium model of real estate space (rent) and real estate asset (capital). For their research the authors employed comparative statistical analysis of a number of macroeconomic indicators, including short-term and long-term

interest rates, availability of construction finances, production level, and employment. Subsequently, they developed a four-quadrant diagram illustrating the interconnection between real estate space and real estate asset. The model demonstrated how exogenous forces impact the property sector as a whole.

In his work, Clapp (1993) presented the concept of the natural (normal) vacancy rate. According to the author, natural vacancy rate is estimated by dividing vacant space, which landlords keep vacant for possible repairs or search for better tenants, by the total amount of space. Subsequently, Clapp explored two possible models to measure this rate. The first model had a simple structure. The future of the office market was based on the expectations for the employment growth. The second model elaborated on this relationship and included expectations for employment at a less granular level. The equation considered managerial, technical, and clerical employment, and the expectations for the growth in this type of occupations.

Table 3 below summarises the key publications on property cycles which were produced during 1970s research period. It contains the title, data and data analysis techniques employed and outcomes of these studies. The following section presents the key post-1990s crash studies on property cycles.

| Publication | Data employed | Statistical technique | Outcomes of the Study |
|---|---|--|--|
| Barras, R. (1983) A simple theoretical model of the office development cycle. Environment and Planning A, Vol.15, No.10, pp.1381-1394 | Time-series (new orders, capital values, construction costs, returns) Statistics (inflation, interest rates, GDP) | Time-series analysis (1956-1980); Mathematical modelling; Historical overview; Correlation/Regression analysis; Turning point analysis | Model of the office development cycle; Clarification of the mechanics behind the cycle; Three crucial parameters – the length of the delay between new investment orders and completions, the adjustment rate and the depreciation rate; National average cycle period – 8 – 10 years |
| Barras, R. (1987) Technical change and the urban development cycle. Urban Studies, Vol.24, No.1, pp.5-30 | Time-series of 5 sectors – private industrial, commercial and house-building, and public house-building and other public building | Time-series analysis (1958-1983); Time-series modelling; Spectral analysis; Turning point analysis | 20-30 years 'urban development cycles'; Interconnection between 5 year, 10 year, and 20 year cycles; Suggestions for policy making |
| Wheaton, C.W. (1987) The cyclical behaviour of the national office market. Journal of American Real Estate and Urban Economics Association, Vol.15, No.4, pp.281-299 | Time-series (construction, completions, office employment, absorption, vacancy rate) | Time-series analysis (1960-1986); Visual data analysis; Multi-equation modelling | 10 year office cycles; Growing cycle amplitude over time; 3 possible scenarios (forecasts from 1986 to 1992) |
| DiPasquale, D. and Wheaton, W.C. (1992) The Markets for Real Estate Assets and Space: A Conceptual Framework. Journal of the American Real Estate and Urban Economics Association, Vol.20, No.2, pp.181-198 | Interest rates; Construction finances; Production level; Employment; GDP; Rents; Vacancy rates | Comparative statistical analysis; Time-series analysis; Multi-equation modelling | Universal equilibrium model (four-quadrant diagram) |

Table 2.3. Key post-1970s crash publications on property cycles

Post-1990s property crash studies

The 1990s property crash in the UK led to a renewed discussion on property cycles. As Barras (2005, p.63) observed, after this crash the same two questions were asked: 'why did it go wrong?' and 'how can we avoid it happening again?'. Property professionals and scholars blamed inaccurate data, its analysis and interpretation, and anticipated that things would improve next time (RICS, 1994; Barras, 2005). Subsequently, it prompted a number of important publications on the subject, including Barras (1994), RICS (1994; 1999), Grenadier (1995), McGough and Tsolacos (1995a; 1995b), and Renaud (1995).

A seminal study commissioned by the Royal Institution of Chartered Surveyors (RICS, 1994) jointly with the University of Aberdeen and the Investment Property Databank (IPD) examined fundamentals of the UK property cycles. It investigated both endogenous and exogenous forces that produced these cycles. Although it was indicated that there is a link between property and economic cycles, the research identified that inherent property market characteristics made property cycles more than just a simple reflection of economic cycles.

The RICS (1994) study employed post-war economic and property data for Britain, which covered the period between 1962 and 1992. The visual and statistical data analysis identified short 4-5 years 'recurrent but irregular fluctuations in the rate of total return' (ibid., p.27). Other findings suggested close timing between economic and property cycles. This led the authors to suggest that there are obvious links between swings in property and the economy. The development cycle was identified as a subset of the property market which gives most of its idiosyncratic features to the property cycle. It was also observed that building booms and busts are the product of inherent construction lags and developers' reaction to market signals. Generally, the RICS (ibid.) considered property cycles to be readily understood despite their irregularities.

In their second study, RICS (1999) examined property cycles and their links with economic cycles. The researchers combined time-series on All Total Property Returns for the period between 1971 and 1992 from their earlier publication, and from 1921 to 1997 compiled from the work of an economic historian Scott (1996). This combination extended the time-series back to 1921. The visual data analysis confirmed the existence of recurrent, but irregular property cycles. Spectral analysis identified cycles ranging from 4 to 12 years. The average length of the cycles was 8 years. As the authors indicated, some fuller statistical tests suggested the existence of major cycles of 9 years duration, and minor cycles of 5 years duration. The subsequent analysis of property returns suggested the existence of three separate UK property epochs. The first was the interwar period between the 1920s and 1930s, which was characterised as being highly volatile, but with particularly high returns on property. The second was the post-war period through the 1950s and 1960s, which exhibited less volatile property fluctuations. And the third was the highly volatile post 1970s period. Moreover, historic data analysis demonstrated different correspondence between fluctuations in property returns and those from gilts and equities. The study suggested that property exhibited a lower volatility than the other two asset classes, thus attracting a higher attention from the institutional investors and offering greater diversification possibilities for their investment portfolios.

Similar to the RICS (1994), Barras (1994) hypothesised that property cycles are not simply random phenomena, but rather a set of recurring events. He analysed the post-war UK property market and identified major forces which generated these cycles. Time-series the author was using covered the period from 1952 to 1992. The starting point for his paper were findings presented in Barras and Ferguson (1985) that the property market is highly cyclical, cycles are of different duration, and that cycles operate on the basis of demand and supply for buildings. Economic growth was expressed as fluctuations in GDP. Commercial development and bank lending was expressed as fluctuations in bank loans to property

companies and commercial new building orders. Rents were expressed as fluctuations in All-Property Rents. From examining the findings, Barras demonstrated that both the 1970s and 1980s property cycles 'were triggered by the same particular combination of conditions in the real economy, the money economy and the property market'. It was also demonstrated that 'different cyclical forces are at work in the occupier market, the development industry and the investment market, sometimes opposing and sometimes reinforcing each other' (ibid., p.195). Subsequently, these hypotheses led Barras to suggest that a better knowledge of the interaction of these underlying forces leads to a greater understanding of the property cycles.

The study by McGough and Tsolacos (1995a) assessed forces generating the UK property development cycles. The property development cycles were referred to as cycles in office, industrial and retail building sectors. For the analysis of the demand for office space and its relationship with the real economy, the authors examined five alternative variables, i.e. GDP, GDP of service industries, output of business and finance, service sector employment and employment in financial services. The demand for industrial property was measured from the relationship between GDP, manufacturing output and manufacturing employment. The GDP, consumer expenditure and the volume of non-food retail sales were alternative variables which were representing the demand side for retail property.

The time-series the researchers employed covered the period from 1980 Q1 to 1994 Q4 quarterly. The raw data was smoothed using the Hodrick-Prescott filter. The study also included dynamics of other economic variables including movement of share prices, short-term and long-term interest rates, and rates of treasury bills. The commentators considered these indicators to reflect trends in economic activity, and thus demand for commercial space. After obtaining the data, the researchers estimated the statistical properties of the chosen variables: amplitude, persistence, procyclicality, and countercyclicality. Amplitude was measured by the

standard deviation, persistence - by first order autocorrelation, and both procyclicality and countercyclicality - by cross-correlation. The empirical results indicated an existing relationship between GDP, manufacturing and business output and the office and industrial property, and between GDP, consumer expenditure and non-food retail sales and retail property. Rents and capital values also exhibited conformity between each other. Rents were procyclical with the office cycles, but lagged industrial and retail cycles, while capital values led the property cycles. Surprisingly, financial indicators exhibited no cyclical pattern with reference to any of the property sectors.

In the US, a significant discussion on the subject was presented by Grenadier (1995). Grenadier investigated underlying causes of prolonged real estate cycles. He subsequently developed a leasing and construction model explaining the recurrence of over-building and stickiness of vacancy rates. Initially Grenadier (ibid.) tackled two standard explanations of real estate cycles. One, which explains property cycles as a result of construction lags. The other, which states that because of non-recourse lending, developers continue to build while funding is available. As Grenadier argued, developers certainly make errors in their future market forecasts, however, they are well aware that it takes time to complete a project. Therefore, developers take into consideration the timing needed to complete the project while developing their strategies. Grenadier affirmed that the first explanation implies myopic behaviour of property developers, but which is an incorrect assumption. The second explanation, as the author indicated, also 'fails to stand up to closer scrutiny' (ibid., p.98). According to Grenadier, investors do learn from their past mistakes and are not willing to lend money to the property developers in booming times, suggesting that non-recourse lending does not account for overbuilding.

Following on from this, Grenadier (ibid.) employed an option pricing methodology to develop his model. The model was split into three stages. In the first stage, fully developed rental property was analysed. In this case, when the market is growing the property owner has an option to wait

and let vacant space at a higher price. If the decision is made to rent the property, the owner loses the option to receive a greater income. Conversely, in a falling market the property owner offers discounted rent to keep the tenant if he wants to ensure a low vacancy rate. In the second stage, the developer faces greater uncertainty about the future demand for space because of construction lags. Therefore, there is an option of completing or withdrawing from the project. However, as the author emphasised, there is a difficulty to reverse construction once started. The third stage assessed the best timing to start the project. The timing was highly linked to land value. Therefore, as the model estimated, valuation of raw land can encourage or discourage developers to commence construction.

Table 4 below summarises the key publications on property cycles which were produced during this research era, containing title, data and data analysis techniques employed and outcomes of these studies. The following section presents the most recent studies on commercial property cycles.

| Publication | Data employed | Statistical technique | Outcomes of the Study |
|---|---|---|---|
| Barras, R. (1994) Property and the economic cycle: Building cycles revisited. Journal of Property Research, Vol.11, No.3, pp.183-197 | GDP; Capital values; Yields; Investments; Bank lending; Rents; Commercial development | Accelerator type model (second-order difference equation); Time-series analysis (1952-1992); Turning point analysis | Property market is highly cyclical; Cycles are of different duration; They operate on the basis of demand and supply for building; Suggestions for policy making; Predictions for the next decade |
| RICS (1994) Understanding the property cycle: Economic Cycles and Property Cycles. The Royal Institution of Chartered Surveyors, London, pp.97 | Property returns; Rents; Yield; Construction; Investment; GDP; Consumer spending; Manufacturing output; Employment; Interest and gilts rates; Inflation | Time-series analysis (1962-1992); Visual data analysis; Property performance measurement; Turning point analysis; Spectral analysis; Simple regression modelling; Model testing | 4-5 years property cycles; Close timing with economic cycles; UK property market is cyclical; UK property cycles are the product of economy and its endogenous (particularly development lag) characteristics; Statistical analysis; Existence of property cycles |
| RICS (1999) The UK Property Cycle - a History From 1991 to 1997. The Royal Institution of Chartered Surveyors, London, pp.57 | Property returns; Yield; Rents; Capital growth; GDP; Building investment; RPI, Gilts, Equities, Treasury bills | Time-series analysis (1921-1997); Turning point analysis; Visual data analysis; Correlation analysis; Time-series simulation; Time-series desmoothing; Filtering (HP technique); Spectral analysis; Multivariate time-series regression with variable additions/deletion; Long-run cointegration; Modelling - capital asset pricing mode (CAPM) | 4-9 years cycles; Correlation with the economy; Strong cyclical pattern; Long-run analysis adds little to the ability to understand or predict the market |
| McGough, T. and Tsolacos, S. (1995) Property cycles in the UK: an empirical investigation of the stylized facts. Journal of Property Finance, Vol.6, No.4, pp.45-62 | GDP; Employment; Consumer expenditure; Industry output; Interest rates | Time-series analysis (1980-1994); Statistical analysis (amplitude – standard deviation, persistence – first order autocorrelation, procyclicality and countercyclicality – cross-correlation) | Tight correlation between GDP, manufacturing and business output and the office and industrial property; and between GDP, consumer expenditure and non-food retail sales and retail property; Establishment of stylized facts |

Table 2.4. Key post-1990s crash publications on property cycles

Modern studies

A considerable amount of literature on property cycles was published from the late 1990s. As Barras (2004) observed, in both the late 1980s and late 1990s property cycles were truly global events, which affected most markets internationally. As a result, property scholars investigated cycles as an international phenomenon, as well as their links with capital markets. According to Barras (2009, p.71) 'the inevitable result was the launch of a new and more extensive phase of research on real estate cycles during the 1990s'. An international phenomenon of property cycles was discussed in Renaud (1995), Pyhrr *et al.* (1999), Dehesh and Pugh (2000), Pugh and Dehesh (2001), Sirmans and Worzala (2003), and Jackson *et al.* (2008). Links between property cycles and capital markets were discussed by Herring and Wachter (1998), ECB (2000), Davis and Zhu (2004), and Lizieri (2009a).

Renaud (1995) investigated the global property cycle for the period between 1985 and 1994. The author assessed international and domestic factors which generated this cycle. The data was obtained from the Organisation for Economic Co-operation and Development (OECD) and Newly Industrialised Economies (NIE). As the analysis suggested, liberalisation of the capital market and financial deregulation, new macroeconomic policies, individualised structure of the property sector itself, as well as lax fiscal policies and incentive structures, which all generated high levels of borrowing, were the primary domestic reasons behind this cycle. The international dominance of Japanese financial institutions was an international factor for this cycle to occur. These arguments were substantiated empirically and also by referring to the work of other researchers, including Glick (1991) and Werner (1993; 1994). The composite evidence collected from the research led Renaud to suggest that the next global property cycle, similar to the one in 1985-1994, is preventable. As the author suggested, better research, adequate policy

making and institutional arrangements are all levers governments can employ to smooth the next global property cycle.

Dehesh and Pugh (2000) examined post Bretton-Woods 'Property Cycles in the Global Economy'. The research covered the post-1980s period with particular emphasis on Asian economies, especially Japan. The post Bretton-Woods period was characterised as an internationally integral and deregulated world economy with an open capital mobility and growing financial engineering. As such, the breakdown of the Bretton-Woods system has placed property in a wider context which made it an international assets class. According to the authors, this had two key implications. First, financial deregulation and growing competition between financial intermediaries led to over-investment in property. Second, international capital mobility created greater liquidity, and, as a result, led to the rise in property prices. Accordingly, commentators suggested that post-1980s major property cycles were products of the internationalisation of the economies.

In their following paper on the subject, Pugh and Dehesh (2001) investigated post-1980s property cycles, the role of institutional investors, as well as the international interdependence between property and finance. In this comparative evaluative review the authors identified that economic decline affects the socio-economic level of the national economies and thus has an impact on the finance and property sectors both locally and internationally.

The internationalisation of property markets and global transmission of cyclical instability since the 1990s triggered property professionals and scholars to investigate links between property and financial markets (Barras, 2009). Some of the empirical studies on the subject focused particularly on residential property. As Davis and Zhu (2004) observed, this was because of the data available for this type of research. Country-specific studies identified a correlation between housing and the capital markets. Empirical analysis by De Greef and De Haas (2000) identified the link between

housing and the mortgage market in the Netherlands. In the US, Quigley's (1999) study suggested that housing prices and financial conditions are interconnected. Gerlach and Peng (2002) indicated the existence of a long-run dynamic relationship between house prices and bank lending in Hong Kong.

Davis and Zhu (2004) assessed the interconnection between the commercial property market and bank lending from the macroeconomic perspective. The authors were motivated by the existence of a bilateral link between the banking and the commercial property markets. Although Herring and Watcher (1998) stated that property cycles may occur without a banking crisis, and that a banking crisis may occur without property cycles, the Davis and Zhu's study concluded that both phenomenon have demonstrated a high degree of correlation over a long period of time. For their research, the commentators catalogued annual data for 17 countries for the period between 1985 and 1995 collected by the Bank for International Settlements (BIS). They then developed a reduced-form single equation model based on the work of Wheaton (1999) in order to assess the relationship between banking and commercial property. Cross-country empirical analysis confirmed their hypothesis. The study also suggested that a rise in commercial property values triggers credit expansion, not vice versa. In addition to that, GDP was identified as having a dominant influence on both banking and property.

Subsequent research into the internationalisation of the property market, led property analysts and researchers to investigate the dynamics of the property market on a global scale. According to Chen and Mills (2005, p.1) 'global real estate investment has become an increasingly important component of efficient, global mixed-asset portfolios'. Researchers including Case *et al.* (1999), Jackson *et al.* (2008) and Stevenson *et al.* (2011) identified the high degree of synchronisation in cycles across international real estate markets. This therefore suggested significant concordance and commonalities across a large number of property markets. Despite the fact that Chen and Mills (2005) argued that economic

and property cycles in different regions exhibit low levels of correlation, more recent research suggests that real estate markets across the globe and especially across the key office markets such as New York and London are correlated (Stevenson *et al.*, 2011). The relationship between the macro-economy and the property market and the effect of globalisation is well discussed in Barkham (2012).

In order to reflect this dynamics of the international property market, Grosvenor (2011) and IPD (2012) created global property market benchmarks. Grosvenor's (ibid.) global office yield composite indicator serves as a benchmark representing property market dynamics on an international scale. This index reflects the current position of the property market globally relative to its long term history. By using this indicator, investors can therefore minimise risk, enhance returns and maximise Net Asset Value (NAV) growth. IPD's Global Annual Property Index reports the market rebalanced returns of the 24 property markets where IPD and its partners operate. The index (partially) reflects the dynamics of the real estate market globally.

Table 5 below summarises the key 'modern' studies on the subject, containing title, data and data analysis techniques employed and outcomes of these studies. The following section turns into property market modelling and forecasting side of the subject. It reviews quantitative property market modelling techniques and discusses their accuracy.

| Publication | Data employed | Statistical technique | Outcomes of the Study |
|---|--|--|--|
| Wheaton, C.W., Torto, R.G. and Evans, P. (1997) The Cyclic Behavior of the Greater London Office Market. <i>Journal of Real Estate Finance & Economics</i> , Vol.15, No.1, pp.77-92 | Absorption; Rent; New construction orders; Vacancy; Total and occupied stock; Interest rates; Office employment; Real construction costs | Time-series analysis (1970-1995); Structural econometric methodology – multi-equation adjustment model; Econometric outlook (scenario planning) | Employment can explain London office market movements; London office market is volatile; Commercial property in European cities is forecastable; Shocks (positive/negative) generates and ‘echo’ |
| Barras, R. (2005) A Building Cycle Model for an Imperfect World. <i>Journal of Property Research</i> , Vol.22, No.2, pp.63-96 | Take-up; Vacancy; Real rental growth; Building starts and completions | Time-series analysis (1970-2004); Multi-equation modelling (series of linear difference equations and set of second order linear difference equations); Building cycle simulation; Model testing | Property market is cyclical; Cyclical fluctuations are generated endogenously around and equilibrium growth path; The longer the construction lag, the longer the cycle period; 5 key parameters which determine model behaviour - the output growth rate; the depreciation rate; the construction lag; the combined transmission coefficient; the demand elasticity |
| Barras, R. (2009) <i>Building Cycles: Growth and Instability (Real Estate Issues)</i> . Wiley-Blackwell, London, UK, pp.448 | Output; Take-up; Building starts; Capital; Vacancy; Rents | Time-series analysis (1968-2006); Model simulation (series of difference equations); Model testing | 6 key parameters which determine model behaviour - the size of initial displacement; the construction lag; the output growth rate; the rate of depreciation; the combined transmission coefficient; the demand elasticity; the greater the construction lag, the greater the period of the cycle |
| Barkham, R. (2011) <i>Global Outlook: Grosvenor’s research perspective on world real estate markets</i> . Grosvenor, London, pp.4. | Stock market indices, bond rates, real estate spreads over bonds, GDP growth, national and international output gaps and indices of real estate rents and yields | Simple arithmetic average of the key office market yields | Indicator assesses long-ranged property cycle; presents current state of the property market relative to its long-term history |

Table 2.5. Key ‘modern’ publications on property cycles

2.2 Property market modelling and forecasting

As the discussion above suggests, the developments in the field of property cycle research led to the construction of various mathematical models helping to explain the behaviour of the real property market (McDonald, 2002; Tonelli *et al.*, 2004; Barras, 2009; Byrne *et al.*, 2010). These models, as Byrne *et al.* (2010) noted, have been produced for a range of different reasons, i.e. to improve one's understanding on the subject and its processes, to predict, forecast or explore possible scenarios; or to provide a basis for decision-making. According to Harris and Cundell (1995, p.76), 'the market crash which traumatized the property industry between 1991 and 1994 has led the institutions in particular to seek greater predictive input to their portfolio management and investment decisions'. As McDonald (2002) pointed out, after the 1980s property boom property researchers have responded to the crisis situation, and as a result substantial progress has been made in property market research and forecasting.

Following Mitchell and McNamara (1997), Tsolacos (2006), and Barras (2009), the area of property market modelling and forecasting, which was primarily developed within academia, has been quickly adopted by practitioners. Tsolacos (2006) further suggested that property practitioners started to employ both qualitative and quantitative research methods to arrive at the final decision. It has therefore resulted in the development of forecasting models, ranging from simple single-equation methods to more advanced multi-equation with stationary data techniques. Accordingly, it led property researchers, including McGough and Tsolacos (1995a), Clayton (1996), Wheaton *et al.* (1997), Pyhrr *et al.* (1999) and Barras (2009), to suggest that the commercial property market is forecastable. Although Tonelli *et al.* (2004, p.1) argued that 'numerous econometric models have been proposed for forecasting property market performance, but limited success has been achieved in finding a reliable and consistent model to predict property market movements'.

2.2.1 Classification of real estate models

Ball *et al.* (1998) presented a general overview of quantitative real estate forecasting models. According to the authors, these models fall into four major categories: (i) multi-equation models of the US office market; (ii) multi-equation models of the London office market; (iii) single equation models; (iv) and local property market forecasting models. Econometric specifications developed by Rosen (1984), Hekman (1985) and Wheaton (1987) represent the first category. Wheaton *et al.* (1997) and Hendershott *et al.* (1999) constitute the second group. Single equation models come from RICS (1994). Modelling at the local level is presented in Jones (1995).

In his survey of office market econometric models, McDonald (2002) divided the research on office market modelling and forecasting into four general categories. One is the development of general market framework, e.g. DiPasquale and Wheaton (1992) and Wheaton (1999). Second are theoretical real estate market equilibrium models, e.g. Wheaton (1990). Third are studies on office rents and the creation of rent indices, e.g. Wheaton and Torto (1994). The fourth group constitutes complete econometric models of office markets, e.g. Wheaton (1987) and Wheaton *et al.* (1997).

Tonelli *et al.* (2004) presented an overview and classification of office rent models developed over the 20 year period before the date of publication. The authors assessed model determinants as well as equations and outcomes of the modelling. It led the commentators to identify twenty different quantitative forecasting models, which were subsequently divided into three major categories according to their input variables. The first category are econometric models which use macroeconomic determinants such as employment, inflation, economic activity (e.g. Giussani *et al.*, 1993). Second group are models based on industry determinants, such as interest rates, space supply, and vacancy rates (e.g. Hendershott *et al.*, 1996; 2002a; 2002b). The third group are those which use building

determinants, such as location, lease structure, and rent level (e.g. Wheaton and Torto, 1988).

Lizieri (2009b) presented his classification of real estate forecasting methods. According to Lizieri, forecasting techniques fall into two broad categories: formal and informal (intuitive). Formal forecasting category is divided into quantitative and qualitative accordingly. Qualitative forecasting methods correspond to judgemental forecasting techniques, which include Life Cycle Analysis, Surveys, Delphi Method, Historical Analogy, Expert Opinion, Consumer Panels and Test Marketing. Quantitative forecasting methods are separated into two groups: causal and time-series. The time-series methods correspond to univariate (extrapolative) forecasting techniques. In other words, these models are not based on any underlying economic theory and produce estimates capturing empirically relevant properties of time-series itself. Causal methods equate to multivariate (explanatory) methods. These modelling techniques incorporate explanatory variables according to economic theory they correspond.

According to Barras (2009), modern commercial property market modelling studies can be separated into three major modelling traditions. One is stock adjustment models, developed in the UK. The second is rent adjustment models, developed in the US. The third is multi-equation models, which are an agglomeration of both. As Barras (*ibid.*) observed, the UK modelling studies are based on the hypothesis that major property cycles are generated by their endogenous forces. The stock adjustment process is at the core of this theory. The US based research, however, focuses on rent adjustment processes within the property market and considers exogenous impulses from the wider economy as having greater impact on property cycles. A third tradition, which is identified as multi-equation modelling, combines both adjustment processes into 'circular transmission process which propagates cyclical fluctuations across all aspects of property market behaviour' (*ibid.*, p.215).

As the discussion above suggests, there are various property forecasting models available to researchers. Subsequently, different authors classified these models into different categories, based on the object, time horizon, data, and approach being used. It all therefore resulted in development of various classification systems. Regardless of differences within property modelling classifications, according to Makridakis *et al.* (1998), Chatfield (2000), and Lizieri (2009b), forecasting methods can be grouped into three major categories, i.e. judgemental, univariate and multivariate.

The judgemental methods are based on subjective judgement, experience, intuition and any other relevant qualitative information. Univariate methods, also known as decomposition, extrapolative or time-series methods, which produce forecasts solely based on current and past values of the series being forecasted (Makridakis *et al.*, 1998; Jain and Malehorn, 2005; Brooks and Tsolacos, 2010). Multivariate methods, known as explanatory or regression methods, forecast any given variable from values of one or more variables that relate to the series of interest (Makridakis *et al.*, 1998; Chatfield, 2000). Exponential Smoothing and ARIMA are time-series methods. The Simple Regression, Multiple Regression, VAR and Econometric (also known as Simultaneous Equation model) are all regression specifications (Makridakis *et al.*, 1998; Jain and Malehorn, 2005; Brooks and Tsolacos, 2010) (Figure 2.3).

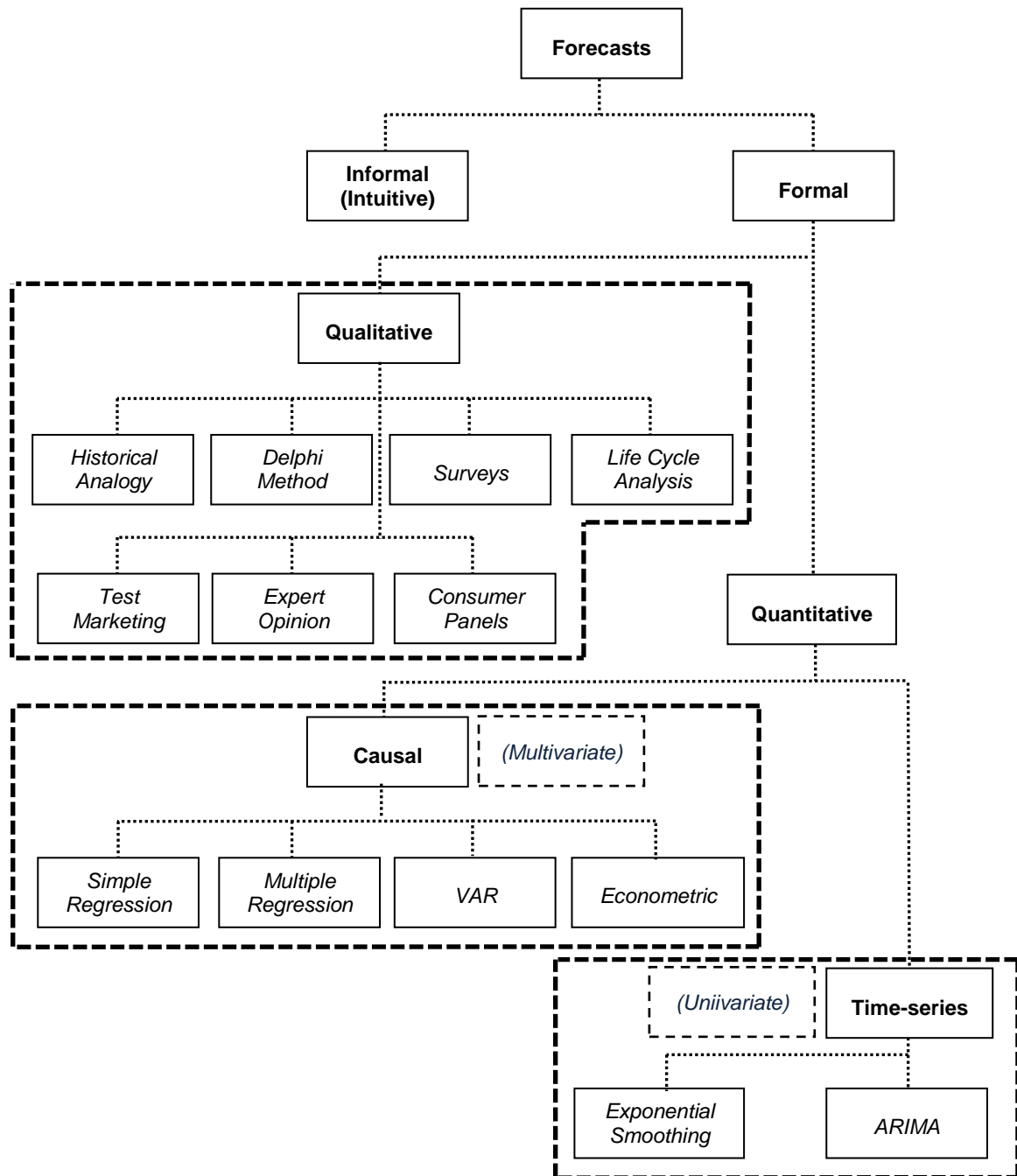


Figure 2.3 Real estate forecasting methods
Adapted from: Makridakis *et al.* (1998); Chatfield (2000); Lizieri (2009b)

Time-Series models

The Univariate time-series modelling approach is usually called atheoretical, as these models are not based upon any underlying economic or financial theory. These models produce forecasts capturing empirically relevant properties of selected series. It is suggested that these pure time-series models are of benefit when regression based models are

difficult to apply, e.g. when data on explanatory variables is not available and it is of a different frequency. According to Stevenson and McGarth (2003) and Brooks and Tsolacos (2010), these models, therefore, became popular within the commercial property market research community. Studies which employed time-series models include Tsolacos (1995), Tse (1997), Stevenson (2007) and Miles (2008).

Exponential Smoothing, as Yafee and McGee (2000) report, is a univariate modelling technique which isolates trend and seasonality from irregular variations. According to Yafee and McGee (*ibid.*) and Brooks and Tsolacos (2010), the main principle behind this methodology is the geometrically declining weighting approach. There, the most recent observations are considered as having greater explanatory power over older observations. Therefore, a greater weight is attached to them.

According to Makridakis *et al.* (1998) and Yafee and McGee (*ibid.*), Single Exponential Smoothing (SES) and Holt's Exponential Smoothing (HES) are two of the most commonly used exponential smoothing methods. Gardner (1985; 2006) maintains that there are few other alternatives to this methodology, including Brown's Linear Trend model.

Single Exponential Smoothing (SES) produces forecasts of the time-series simply by adding a forecast from the previous period with an adjustment for the error that occurred in the last forecast. The advantage of this forecasting technique is that it requires little storage of historical data and fewer computations. It is therefore useful when a large number of items need to be forecasted (Makridakis *et al.*, 1998).

Holt's Linear Trend (HLT) model, also known as Linear Exponential Smoothing, is an extension of SES. It is suggested that HLT involves smaller errors and therefore produces more accurate extrapolations (Makridakis *et al.*, 1998).

Brown's Linear Trend (BLT) model, also known as Double Exponential Smoothing, is a special case of HLT. The BLT specification is applicable when the series contains a linear trend and there is no seasonality. Here,

smoothing parameters are level and trend which are of equal weight, which makes this specification similar to an ARIMA model (PASW, 2010a).

Autoregressive Integrated Moving Average (ARIMA) specification is also known as Box and Jenkins model (Brooks and Tsolacos, 2010; PASW, 2010a). As Box *et al.* (1994) explain, if the autoregressive operator AR is of order p , the d th difference is applied, and the moving average MA operator is of order q , their combination creates ARIMA model of order (p,d,q) , or in other words ARIMA (p,d,q) process. The AR component of the specification implies that future values of the times-series can be approximated and predicted from the current and past values of the time-series itself. The MA component, instead, involves current and past effects of random shocks or error terms in the series (Barras, 1987; Stevenson and McGarth, 2003; Karakozova, 2004).

According to Makridakis *et al.* (1998), ARIMA model can have a shortened notation if an element within its framework equals 0. For example, ARIMA (1,0,0) can be rewritten as AR(1), whereas this model does not contain differencing (d) and moving average (q). Similarly, ARIMA (0,0,1) can be rewritten as MA (1), and ARIMA (1,0,1) can be modified into ARMA (1,1).

ARIMAX is an Integrated Autoregressive Moving Average model with Exogenous Explanatory Variable(s). The principle of this specification is that it incorporates Autoregressive (AR) and Moving Average (MA) components, as well as Vector of explanatory variable(s) (X) into one equation. The hypothesis behind this approach is that by incorporating relevant explanatory variable(s), a greater forecasting accuracy can be achieved (Karakozova, 2004).

A difficulty with ARIMA models, however, is that these specifications can only be used with stationary data. For non-stationary data ARIMA models are extended by incorporating differencing of the data series (Makridakis *et al.*, 1998).

The empirical evidence suggests that there can be a variety of ARIMA(X) specifications. Barras and Ferguson (1987b) used eight AR (1; 2; 3; 4; 6; 7;

8; 10) and three MA (2; 4; 8) specifications. McGough and Tsolacos (1995b) experimented with three AR (1; 2; 3), two MA (1; 2), and three ARIMA (1,2,1; 1,2,2; 1,2,3) specifications. Stevenson and McGarth (2003) compared forecasting power of two AR (1; 2), two MA (1; 2), and four ARMA (1,1; 2,1; 1,2; 2,2) models. According to Makridakis *et al.* (1998), however, this ARIMA model flexibility creates difficulty in deciding which model specification is the most appropriate. As commentators suggest, both experience and good judgement is needed in order to accurately identify the best model specification. Brooks and Tsolacos (2010) also add that visual time-series analysis, as well as assessment of both Autocorrelation Function (ACF) and Partial Autocorrelation Function (PACF) helps in deciding on appropriate model specification.

However, as Chaplin (1998; 1999), Stevenson and McGarth (2003) and Karakozova (2004) commented, visual analysis of ACF and PACF are unlikely to be helpful in identifying the most appropriate model specification. Therefore, researchers recommended using alternative techniques known as 'Information Criteria' in selecting the best ARIMA model specification. There are two common information criteria. One is Akaike Information Criterion (AIC) and other is Bayesian Information Criterion (BIC).

As the literature suggests, both AIC and BIC contain a 'penalty' for adding extra variables into the model. Accordingly, both information criteria select the most parsimonious model (Chaplin, 1999). The only caveat with these formulations however is that BIC favours lower-order models, while AIC selects higher-order specifications. Nevertheless, both techniques are considered to be superior model selection tools with lowest AIC and BIC values indicating the best model specification (Schwarz, 1978; Brooks and Tsolacos, 2010).

Regression models

Regression is an important tool for modelling and forecasting. As Koop (2006), Brooks (2008), Brooks and Tsolacos (2010) suggest, it has been

extensively used by researchers. According to the commentators, regression is easy to use, it is uncomplicated to interpret, and thus it dominates empirical modelling.

Makridakis *et al.* (1998, p.187) define **Simple Regression** as a 'regression of a single Y variable [dependent variable] on a single X variable [the explanatory or independent variable]'. Similarly, Brooks and Tsolacos (2010) indicate that this method assumes the dependence of Y on only one variable X. According to the commentators, the principle of Simple Regression is that an increase/decline in X will lead to an increase/decline in Y.

As the real estate literature suggests, the dependent variable in most cases is influenced by more than one independent variable. This is the main principle of **Multiple Regression** (Brooks and Tsolacos, 2010). The hypothesis behind this modelling tradition is that by using an equation with more than one explanatory variable, the dynamics of a dependent variable can be modelled more accurately. The advantage of Multiple Regression is that it makes the most of the interdependence of few explanatory variables to model a dependent variable (Makridakis *et al.*, 1998; Koop, 2006).

Vector Autoregressive (VAR) modelling approach, as identified by Brooks and Tsolacos (2010), is a hybrid between a Univariate time-series model and Econometric model (for a discussion on Econometric modelling approach please see the section below). The traditional VAR specification is an n -equation, n -variable linear model where every variable is explained by its past and current values, plus past and current values of the remaining $n-1$ variables. The empirical evidences of Holtz-Eakin *et al.* (1988), Sims (1989), Brooks and Tsolacos (2001; 2010), Stock and Watson (2004), advocate VARs to be powerful in data description and forecasting. VARs were employed by economists, including Sims (1989), Dungey and Pagan (2000) and Cogley and Sargent (2005), as well as

property researchers, including Eng (1994), McCue and Kling (1994) and Brooks and Tsolacos (2003).

Brooks and Tsolacos (2010) suggest several advantages of VAR models. There is no need to specify which variables are exogenous and which ones are endogenous, as all are endogenous. VARs are more flexible than AR models. In general VARs are seen as being superior to 'traditional structural' models. What is more, VARs are easy to use. They also provide a framework to test for Granger causality between variables.

However, VAR models are not without criticism. Koop (2006) and Brooks and Tsolacos (2010) comment that VARs are 'atheoretical'. Similar to univariate time-series models they utilise little theoretical information about the relationship between variables. Furthermore, there is always an issue in deciding on the lag length of the specification. The commentators also noted issues related to the level of parameterisation and stationarity.

Econometric or structural modelling approach is known as a combination of system of equations. According to Brooks and Tsolacos (2010, p.303), these models are used when the theory suggests 'that causal relationships should be bi-directional or multi-directional' and that variables incorporated into equations should be related to one another. Each equation is then estimated independently using the OLS approach.

Following Stevenson and McGarth (2003) and Barras (2009), the advantage of such an approach is that it links several equations together subsequently linking variables into one system. As Brooks and Tsolacos (2010) commented, such systems are often used within the private sector.

However, this approach is also not without criticism. According to Stevenson and McGarth (2003), large structures can limit flexibility of a whole system especially in generating forecasts. Brooks and Tsolacos (2010) also noted that the dynamic structure of a structural model may affect the ability of an individual equation to reproduce the historic series it is seeking to represent.

The difficulty with regression-based models, whether it is Simple Regression, Multiple Regression, VAR or Econometric specification, is the presence of Autocorrelation. While building a regression based model, there is always a need to assess whether Autocorrelated disturbances are present within the model. Put simply, there should be no relationship between explanatory variables within the framework. According to Brooks and Tsolacos (2010), the Durbin-Watson (DW) test provides a platform to test for Autocorrelation and it should be used when building a regression based specifications.

Another issue with regression is the presence of heteroscedasticity. As Gupta (1999, p.234) suggests, in any well formulated regression 'the distribution of the residuals should have no relation with any of the variables'. In other words, the variance of errors should always be constant across the period. However, it can be the case that regression residuals are not constant and/or they are different for every observation. It therefore causes difficulty with modelling. If variances are unequal, then the reliability of each observation is therefore unequal also. Accordingly, greater variance lowers the importance of observations. Researchers including D'Arcy *et al.* (1999) and Gupta (1999) suggest using White's test as one of the most popular checks for heteroscedasticity.

2.2.2 Accuracy of property forecasting models

The subsequent developments in property modelling and forecasting, especially with the aid of IT, resulted in a surge in the complexity of mathematical modelling. Considerable use of high technology equipment allowed researchers and particularly those within the industry to employ new and more complex quantitative property market research techniques (Ball *et al.*, 1998; Dehesh and Pugh, 2000; Barras, 2009; Lizieri, 2009a). As Brooks and Tsolacos (2000, p.1825) observed 'more sophisticated techniques are in demand as they may potentially allow a better understanding of the sources of past changes in the market environment and enable these changes to be built into the rent forecasts'. However, the

research indicates that despite advances in property market modelling and forecasting, there still remains a degree of inaccuracy between model outputs and actual property market performance (Newell *et al.*, 2002; Newell, 2006; McAllister and Kennedy, 2007; Investment Property Forum, 2012).

Direct comparison of the accuracy of property forecasting models

In their research into the short-term forecasting of the UK commercial rental values, McGough and Tsolacos (1995b) employed an Autoregressive Moving Average (ARMA) modelling approach to examine retail, office and industrial rents over a 16 year period. The accuracy of their forecasts was then examined by comparing them against actual values of the Jones, Lang & Wootton (JLW) rental values index. As the modelling results demonstrated, ARIMA models for retail and office rents were able to predict the dependent variable. The Root Mean Sum Predicted Error for Retail Rental Index, Office Rental Index and Industrial Rental Index was 0.0078, 0.0079 and 0.0320 respectively.

In a subsequent paper, Tsolacos (1995) developed a single-equation regression model of retail rents determination. The outcomes of the study demonstrated that this particular specification successfully captured the dynamics of the rental index.

Clayton (1996) developed a Vector Autoregressive model to forecast the Canadian commercial property market. The good fit of the model led him to conclude that 'market volatility is not necessarily something to fear...real estate returns are predictable to some degree, and hence market movements may be detectable in advance' (*ibid.*, p.363).

D'Arcy's *et al.* (1999) investigation into the Dublin office market suggested that a Single Equation regression rent determination model produced better results than a Double Exponential Smoothing (DES) and the Holt-Winters (HW) specifications. The error value for the econometric model for year 1997 was +3.0 percent, while it was -17.9 percent for DES and -13.6

percent for HW for the same year, suggesting that econometric model was seven times more accurate than the alternative specifications.

Chaplin (1998; 1999) in a series of papers assessed office rent prediction models. In his first study, Chaplin (1998) identified that the best fitting models exhibited poorer forecasting results than their naïve competitors. It therefore led him to conclude that 'overall the general tone of the results suggests that there is very little benefit, if any, from attempting to select a model based on best fit to the historic data' (ibid., p.35). The results of a following study (Chaplin, 1999) were similar, suggesting that naïve models outperformed econometric structures. In other words, no-change or same-change strategy generated better modelling outcomes than mathematically constructed models. Chaplin (ibid.) therefore concluded with a citation from Pant and Starbuck (1990, p.442) that 'more complex, subtle, or elegant techniques give no greater accuracy than simple, crude or naïve ones. More complex methods might promise to extract more information from data, but such methods also tend to mistake noise for information. As a result, more complex methods make more serious errors, and they rarely yield the gains they promised'.

Hendershott's *et al.* (2002a) comparative analysis of an alternative (reduced form) rental adjustment model suggested that model successfully tracked 72 percent of movements in the dependent variable with all the coefficients being significant.

A more robust examination of the forecasting ability of property econometric models was presented by Brooks and Tsolacos (2000). The study compared four UK retail rent prediction models - an unrestricted VAR model, AR model, a Long-Term Mean model, and Random Walk model. As the result of the study suggested, the greatest modelling accuracy for CBRE index was obtained from the AR model, while for LIM index VAR produced the best fitting outcomes. In their following paper, Brooks and Tsolacos (2001) suggested that VAR model produced poorer

forecasting results for real estate returns than Long-Term Mean and ARIMA models.

Wilson's *et al.* (2000) study into forecasting accuracy of Spectral Analysis (SA), ARIMA and Exponential Smoothing (ES) modelling techniques suggested that, ES, which is considered to be a basic forecasting technique, exhibited comparable forecasting results to the other two more advanced methods.

McGough and Tsolacos' (2001) assessment of the forecasting accuracy of Vector Error Correction (VECM), ARIMA, and the Regression (RM) models indicated the VECM model to be the most accurate amongst four specifications, while the ARIMA produced the poorest results.

In their panel data study on 12 European office markets, Mouzakis and Richards (2004) identified that their Fixed Effects Error Correction specification was more accurate in generating forecasts than alternative Simple Autoregressive Distributed Lag model (ARLD). According to the authors, the R-squared of their model was 66.2 percent, and Mean Absolute Error (for 2000 – 2001) was 0.067.

Karakozova (2004) examined the forecasting accuracy of three alternative office returns determination models for the Helsinki office market. The selected models were Regression Model (RM), Error Correction Model (ECM), and Integrated Autoregressive-Moving Average Model with exogenous explanatory variables (ARIMAX). The forecasting results were then compared against Double Exponential Smoothing (DES) model performance. As results of the study indicated, all three alternative forecasting techniques outperformed the DES competitor, with the ARIMAX model being the most accurate. As the author explained, ARIMAX model did not contain long-run information, i.e. error correction component, and therefore performed better at picking-up shocks and persistence effects present in the data. The MAPE for ARIMAX model in a one-year ahead forecast (1998-2000) was 2.01, while it was 2.70 and 3.05 for Error Correction and Regression models respectively.

The investigation into ARIMA model forecasting accuracy by Stevenson (2007) suggested that, in general, ARIMA models are applicable to forecast rental values. However, as the author commented, ARIMA specifications are of greater benefit for short-term forecasting purposes only, whereas they tend to over- or under-estimate key turning points in the longer-term.

More recently, Füss *et al.* (2012) compared the accuracy of non-linear Smooth Adjustment Threshold (STR) and non-linear Instantaneous Adjustment (SETAR) specifications in predicting the UK industrial, office and retail rents. The accuracy of these two specifications was compared against linear ARDL specification. As the modelling results suggested, non-linear models had overall better in-sample fit. The R-squared of the ARDL model was 63 percent, 84 percent and 75 percent for industrial, office and retail price change respectively, while it was 75 percent, 88 percent and 80 percent of STR and SETAR models for the same series.

Indirect comparison of the accuracy of property forecasting models

Studies by Newell *et al.* (2002), Gallimore and McAllister (2004), McAllister *et al.* (2005a), Newell and MacFarlane (2006), McAllister and Kennedy (2007) and IPF (2012) adopted an alternative forecasting accuracy measurement approach. The researchers assessed accuracy of already produced forecasts by comparing them against established property market benchmarks.

Newell *et al.* (2002) assessed Jones Lang Lasalle (JLL) six-months ahead forecasts against the actual property returns reported by the Property Council of Australia. As the results of the study indicated, econometric forecasts were poorer than those obtained from the naïve forecasting method. The U-statistics for the Sydney office market was 1.76, for the Perth office market it was 1.58, and for the Canberra office market it was 1.49. Accordingly, it led the authors to conclude that property forecasting accuracy has 'room for considerable improvement' (*ibid.*, p.6).

Gallimore and McAllister (2004) examined the quality of expert judgement of commercial property forecasting. The results of semi-structured interviews suggested that property professionals were inclined into 'self-censorship' or were 'censored' by their peers, as all parties were aware of the limitations of their models. Therefore, forecasters were unlikely to report sharp increase/decline in a series even if models suggested notable market corrections for the future.

Newell's (2006) subsequent study into the accuracy and the role of expert judgement within property forecasting suggested major issues. These issues were high levels of consensus amongst forecasters, uncertainty, persistence of errors, as well as inability in pick-up market turning points.

McAllister *et al.* (2005a) compared the Investment Property Forum (IPF) quarterly forecasts with actual property market performance expressed as IPD indices for rental growth, capital growth and total returns. Visual and statistical analyses indicated errors in forecasting, high levels of consensus, as well as systematic bias amongst forecasters.

Similarly, Newell and MacFarlane (2006) assessed the accuracy of commercial property forecasting in Australia. The authors compared bi-annual consensus forecasts produced by the Australian Property Institute with actual commercial property performance expressed as PCA/IPD direct property indices. The results of the study suggested that forecasters tend to display high levels of optimism, as well as they exhibit an element of inertia in their forecasts. However, the calculations suggested that property forecasters outperform naïve property forecasting strategies for both retail and industrial property. Overall Theil's U-statistics value for retail property was 0.74 and 0.52 for industrial.

Tsolacos (2006) assessed whether consensus forecasts for All Property Rents and Total Returns produce better results than simple forecasting techniques such as AR(1) and Simple Regression (SR). The findings of the study suggested that consensus forecasts were more accurate than econometric models in the short term. However, when the forecasting time

horizon increases, the explanatory power of consensus forecasts declines, e.g. in a two year horizon, IPF forecast's MAE was greater (2.97) than that of AR (1) model (2.76).

The issue of the accuracy of property forecasting was further discussed by McAllister and Kennedy (2007). Their statistical analysis of the market rental data on 13 European cities suggested that property market data contains a large degree of uncertainty, which subsequently affects property market forecasts.

More recently, IPF's (2012) investigation into the accuracy of UK commercial property forecasting suggested that forecasting accuracy varies. This variation is determined by market conditions, object being forecasted, forecasting techniques used, as well as by the forecasting period. The study also suggested that forecasters avoid predicting 'big numbers', i.e. they over-estimate a bear market and under-estimate a bull market. According to the calculations, the Long-Term Average (LTA) forecasting approach proved to be more accurate than Consensus Forecast (CF). The LTA was 80 percent accurate for one-year-ahead period, and 75 percent accurate for two-year-ahead period in generating forecasts.

This assessment of property forecasting model accuracy subsequently allowed researchers to suggest that regardless of the increase in the complexity of property market modelling and forecasting, the forecasting adequacy of alternative specifications can be improved. Accordingly, the commentators identified five major reasons which contribute to forecasting inaccuracy. These are market uncertainty, object being forecasted, modelling technique used, forecasting horizon, and data being employed (Makridakis, 1989; Newell *et al.*, 2002; McAllister *et al.*, 2005a, IPF, 2012). The researchers therefore argued that by improving any or all of the above noted elements of forecasting inaccuracy, greater forecasting performance may be achieved.

The current study therefore focuses on property forecasting accuracy improvement through modelling. The research seeks an alternative econometric approach to achieve greater predictive outcomes. It critically appraises the prevailing practice in the industry and academia of selecting a single best model based on model fit. It then assesses the difficulty in deciding which model to choose when different specifications produce different results. It then presents an alternative modelling technique which was developed by economists but has now been applied to improve UK commercial property cycle forecasting accuracy.

2.3 Summary

In reviewing the literature it was found that property cycles have been debated for more than a century (Mangoldt, 1907; Hoyt, 1933; Hakfoort, 1992; Barras, 2009). However, serious discussions and analyses on the subject emerged only during the early twentieth century. German scholars including Mangoldt (1907) and Eisenlohr (1921) were pioneers of building cycle research. In the US research on the subject started in 1933 with Hoyt's publication on the Chicago real estate cycle. Cairncross (1934) wrote one of the first studies in the UK. Since then, the subject has attracted greater attention of scholars, who investigated different aspects of property cycles. In the UK, Lewis (1965) published a historic survey of British economic growth from 1700 to 1950. Barras (1987) published a study of the UK post-war building. RICS (1994; 1999) examined the main elements of the UK property cycles. Subsequently, as Barras (2009) indicated, research into property cycles began to be conducted in private sector consultancies rather than in academia with the purpose of commercial forecasting.

As the results of the literature review indicated, the pioneering studies on the subject were particularly concerned with fluctuations in building (especially in residential), which was identified as the largest and the most volatile component of aggregate investments. These studies were inclined towards statistical data analysis and its interpretation, as there was an obvious lack of robust and consistent data. Consequently, early researchers identified both short (around 5 years) and long (around 20 years) building cycles. The prime explanation for the existence of these cycles was a relationship between population growth and the state of the economy. Moreover, building cycles were seen as local phenomena, independent from fluctuations in business.

Early modern property cycle studies in the UK were based on the hypothesis that major property cycles are generated by their endogenous forces. The key factor for these cycles to occur was an inherent production

lag within the construction industry. The minor cycles were seen as the demand-side phenomenon reacting to changes in business. Particular attention was also placed on the financial side of the phenomena. As Barras (2009) indicated, favourable financial conditions fuelled two speculative property booms, one in the early 1970s, another in the late 1980s/early 1990s, with both of them bringing the British economy into recession. According to Baum (2001), a growing property portfolio within financial institutions was another factor for cycles to occur.

The experience of the 1990s brought new perspectives into property cycles research. These studies underlined a need for a global view on property cycles and particularly their relationship with capital markets. As Herring and Watcher (1998), Davis and Zhu (2004) and Barras (2009) observed, ever closer integration of property and financial markets mean that instability in one market can be easily transmitted to another local or national market. Accordingly, financial engineering and international flows of capital connect both markets. An increasing internalisation of the property market and similar macroeconomic environment translate cycles between countries subsequently creating greater volatility within markets.

As the discussion above suggests, there has been a significant shift in understanding of property cycles as well as in the variables property cycle researchers used to explain this phenomenon. There has been a shift from more building/construction and population-oriented variables towards business/economic variables. Early property cycle researchers considered property/building cycles as a local phenomenon, mostly independent from the wider economy. It was suggested that a sudden increase in population, or migration within certain areas with greater industrial opportunities, was a major driver for property/building cycles to occur. However, later studies considered property cycles as an element of the broader economy. Researchers began analysing property markets in the context of general business and financial cycles.

The shift in the understanding of property cycles also relates to the way it relates to business cycles. Early scholars saw property cycles as a leading phenomenon. As it was noted in Section 2.1.3, property cycle researchers in the early 1930s commented that property leads general economy by around 2 years.

However, a more recent theory suggests that property market actually lags the business cycle. Although empirical estimates are inconclusive, the general suggestion is that property market lags business cycle by around 2 years. For an industrial property, this lag is around 1 year which is the time needed to build an industrial object. For an office building, it stands at around 2 to 3 year depending on the location and complexity of the project.

Additionally, the property market is now seen as a component of the general economy, and in financial centres such as New York, London and Singapore, property markets became a global asset class. This was a paramount shift in the way property is seen by industry participants. As previously noted, early commentators saw property as a local market, which related to a particular city or the region, while nowadays, property is considered as a financial instrument, which corresponds to macroeconomic dynamics.

The subsequent discussion on the subject suggested that developments within the field of property cycles research led to the construction of various mathematical models. These models were employed in order to explain the behaviour of the real property market. The study suggested that univariate and multivariate were the main quantitative modelling approaches used within the field. As it was noted, the key univariate real estate forecasting models are Exponential Smoothing and ARIMA, as well as their variations. The main multivariate or regression based models are Simple Regression, Multiple Regression, VAR and Simultaneous Equation structures.

Although these models fitted historical data, the discussion has shown, however, that these specifications can be better at forecasting. Both discussions on direct and indirect comparison of the accuracy of property forecasting models suggested that forecasting accuracy varies and that there is a set of components which result in forecasting inaccuracy. It therefore led researchers to comment that greater forecasting accuracy could be achieved if any or all of these components are improved.

The evidence presented in the literature review therefore suggests that there is scope for further analytical and empirical work in the field of commercial property market modelling and forecasting. It is apparent that current modelling techniques, which are available to property market researchers, can be improved. Consequently, it is considered that the field would benefit from the introduction of an alternative technique which could be used to improve the accuracy of commercial property market modelling and forecasting.

CHAPTER 3 RESEARCH DESIGN AND METHODOLOGY

This chapter introduces the modelling process of the research. It is divided into four sections. Section 1 discusses the use of different forecasting models and the difficulty in deciding on the modelling outcomes.

Section 2 then introduces the principle of Combination Forecasting as an alternative methodology for commercial property market cycle forecasting accuracy improvement. It starts with a discussion on Combination Forecasting. It then assesses the key methods of combination.

Section 3 discusses the process of model implementation using PASW 18 (known as SPSS) statistical package. It provides information on two key modelling functions used for this research. The first function is 'Time-Series Modeller', which is used to generate univariate time-series models including Exponential Smoothing and ARIMA specifications. The second is 'Regression' function which is used to produce OLS based models including Simple Regression, Multiple Regression and Vector Autoregression. The section then presents additional information on auxiliary functions of the statistical package. It also discusses difficulties associated with spread-sheets.

Section 4 presents each modelling technique used for this research and their formulae. It starts with the Exponential Smoothing Method and its three variations including Single Exponential Smoothing (SES), Holt's Linear Trend (HLT), and Brown's Linear Trend (BLT) models. It then presents ARIMA, ARIMAX, Simple Regression (SR), Multiple Regression (MR), and Vector Autoregression (VAR) models, as well as Combination Forecasting (CF), including Simple Averaging and OLS based Combination structures. The section also addresses statistical difficulties related to real estate model building. These are issues of autocorrelation and heteroscedasticity in regression based models, and the issue of Information Criteria whilst constructing ARIMA models.

3.1 Difficulty in choosing an appropriate forecasting method

The literature, in particular Section 2.2.3 of Chapter 2, revealed that commercial property market researchers and analysts use different forecasting methods for different forecasting purposes and horizons. Exponential Smoothing and Moving Average methods were mostly used for short-term and less often for medium-term forecasting horizon. These methods were also employed as benchmarks for alternative modelling techniques. ARIMA methods of forecasting were not used very often for any forecasting horizon. Although empirical estimates suggested that this modelling approach is useful for short-term forecasting purposes. Regression proved to be the most popular modelling approach. It was used most often for the medium-term forecasting horizon. According to Makridakis *et al.* (1998), this is consistent with theoretical reasoning which suggests that in the medium- and long-term the importance lies with understanding explanatory variables and other factors which affect the dependent variable. Subsequently, by having this understanding, the interrelationship between the dependent and explanatory variables can be quantified.

The review then identified that commercial property market researchers were selecting an appropriate method for forecasting based on the method's accuracy or its statistical complexity/sophistication. For example, D'Arcy *et al.* (1999) estimated that an Econometric model was more accurate than Double Exponential Smoothing and Holt-Winters models as it had smaller forecast errors. According to Stevenson and McGarth (2003), Bayesian VAR model produced the best forecasts in comparison to ARIMA, OLS based Single Equation and a Simultaneous Equation models in predicting CB Hillier Parker London Office index as it had smallest Mean Absolute Error. Karakozova's (2004) study suggested that of all three alternative models, i.e. Regression, Error Correction, and ARIMAX, ARIMAX model provided with the best forecasting results for office returns

in Helsinki. This particular specification had the smallest Mean Absolute Percentage Error among competing models.

This general practice in selecting a single best model based on the model's accuracy or its statistical complexity/sophistication, however, has been criticised by researchers, including Granger (1969), Wood (1976) and Wallis (2011). According to the commentators, in most cases forecasters and decision makers discover the best performing model, which is then accepted and used, thus rejecting other alternatives. However, when the aim of the research is to obtain the most accurate forecast, discarding alternative models is unproductive. Rejected methods may contain useful independent information.

Another issue is in deciding which model to choose when different specifications suggest different results. As Makridakis *et al.* (1998) questioned, what, for instance, a decision maker should do if a time series model predicts a 10 percent decline in sales while a regression model tells that sales will increase by 2.5 percent over the selected time horizon. The commentators further elaborated on this issue and presented it graphically. The Figure 3.1 displays forecasts obtained from Single Exponential Smoothing (SES), Holt's Linear Trend (HLT) and Damped Smoothing (DS) models². The statistics of this example suggest that Holt's model is the best fitting specification. Its Mean Squared Error (MSE) is 1.57 which is smaller than that of Single Exponential Smoothing and Damped Smoothing models, which are 9.37 and 17.77 respectively. However, the most accurate post-sample predictions are obtained from the Single Exponential Smoothing with its MSE being the smallest of all three models. The post-sample MSE for the Single Exponential Smoothing is 1945.98, it is 3116.47 for Holt's Linear Trend and it is 2003.52 for Damped Smoothing. This example demonstrates the dilemma researchers and decision makers are facing, i.e. that different models generate different

² The damping parameter measures the persistence of the linear trend (McKenzie and Gardner, 2010)

results and that each of these model outcomes contain useful information about an object being modelled.

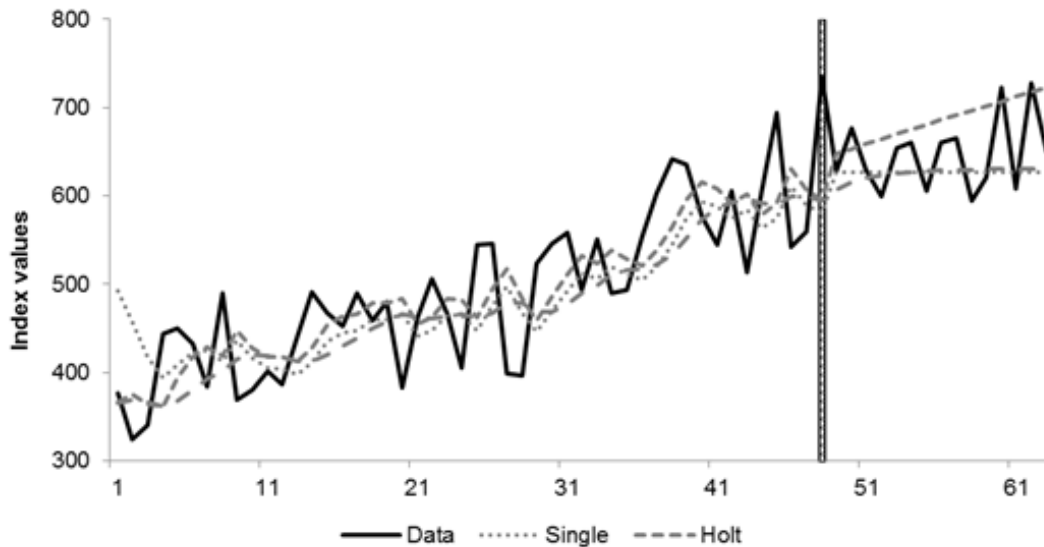


Figure 3.1 Model fit and forecasts for SES, HLT and DS models
Adapted from: Makridakis *et al.* (1998)

So what researchers should do having obtained these results? Makridakis *et al.* (1998) subsequently commented that a possible solution to this problem is to use improved, which mostly means more complex, modelling techniques. However, the solution to replace existing methods with more mathematical ones and train existing researchers so that they can work with new methods, unfortunately, does not work. According to Makridakis *et al.* (*ibid.*), this exercise tends to require more resources, greater skills and/or additional training to those already at work. What is more, the empirical evidence does not support the assumption that complexity improves modelling accuracy. This argument can be found within various fields of research, including environment, economics, and physiology, which is discussed below.

Outside the real estate discipline, the findings of Dorn (1950) and Hajnal (1955), who investigated demographics forecasting, suggested that complex population forecasting models, which typically incorporate large amounts of inputs, become overly complicated, and thus exhibit poorer accuracy. In their analytical survey, Armstrong *et.al.* (1984) assessed the relative accuracy of both complex and simple extrapolative methods. The

commentators identified that simple methods (e.g. Exponential Smoothing) exhibit a comparable degree of accuracy to more complex ones (e.g. Box-Jenkins approach). In a subsequent paper, Armstrong (1986) made a qualitative review of the forecasting methods of the period from 1960 to 1984. The author arrived at the same conclusion that forecasters should be in favour of simple forecasting techniques over the more complex Econometric structures.

Clements and Hendry's (2003) investigation into economic forecasting was also not in favour of complex forecasting models. As the authors indicated, 'although which model does best in a forecasting competition depends on how the forecasts are evaluated and what horizons and samples are selected, 'simple extrapolative methods tend to outperform econometric systems' (ibid., p.304). More recent evidence from Buede (2009) suggests that although simple models contain a large variance in their predictions, complex models still have a large probability of producing wrong results. Orrell and McSharry (2009) also observed that, as models become more complex and parameterised, the number of elements they contain increases significantly. As a result, even small changes in these parameters can have significant consequences on modelling outcomes. Certainly, more parameterised models fit historic data better, their structure can also be more flexible. However, as the authors observed, such models are less helpful at predicting the future.

In the property forecasting literature, as the evidence suggests, simple models such as Exponential Smoothing, Simple Regression, or ARIMA specifications outperform the more complex forecasting techniques, including VAR and Econometric models, or at least generate highly comparable outcomes (Chaplin, 1999; Newell *et al.*, 2002; Stevenson and McGarth, 2003). This therefore led Newell *et al.* (2002) to suggest that despite the increased complexity in property market modelling methodologies, simple methods are found to be as good as complex econometric structures.

An alternative solution to the above noted modelling issue is to use the principle of Combination Forecasting. As it was suggested above, individual models use different data and they are specified on different parameters. As such, these models represent only a partial picture of reality, regardless of their complexity. This subsequently affects their accuracy (Makridakis, 1989; Goodwin, 2009). However, theoretical and empirical findings, which date back more than four decades, suggest that Combination Forecasting is a useful methodology in achieving greater modelling accuracy (Bates and Granger, 1969; Clemen, 1989; Makridakis, 1989; Kapetanios *et al.*, 2008; Pesaran and Pick, 2011; Wallis, 2011).

It is therefore decided to adopt the principle of Combination Forecasting for the purpose of this present study. As will be discussed in the following section, Combination Forecasting is a robust methodology which can be employed to improve the accuracy of commercial property market modelling and forecasting. This modelling approach was originally developed by economists, but is now applied to the UK commercial property market. This research subsequently assesses whether combination forecasts from different forecasting techniques are better than single model outputs. It examines which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best.

The following section introduces the principle of Combination Forecasting. It presents this modelling approach in more detail, as well as discusses the key methods of combination.

3.2 Accuracy improvement through Combination Forecasting

3.2.1 The principle of Combination Forecasting

The principle of Combination Forecasting was developed within the field of economics and business research. The researchers were motivated that by combining forecasts from different methods and sources a greater predictive accuracy can be achieved (Makridakis, 1989; De Gooijer and Hyndman, 2006; Assenmacher-Wesche and Pesaran, 2008; Goodwin, 2009; Pesaran and Pick, 2011; Wallis, 2011).

According to Mahmoud (1984), Combination Forecasting is more accurate because it contains greater information on the object being forecasted. This therefore led researchers, including Clemen (1989), Makridakis (1989), Fildes (1991), and Goodwin (2009), to suggest that Combination Forecasting alleviates the weaknesses of the individual models which subsequently improves the overall forecasting accuracy. Accordingly, it was recommended that Combination Forecasting should become a standard practice within forecasting.

The efficiency of Combination Forecasting is well illustrated by Armstrong (2001, p.1): 'Assume that you want to determine whether Mr. Smith murdered Mr. Jones, but you have a limited budget. Would it be better to devote the complete budget to doing one task well, for example, doing a thorough DNA test? Or should you spread the money over many small tasks such as finding the murder weapon, doing ballistic tests, checking alibis, looking for witnesses, and examining potential motives? The standard practice in matters of life and death is to combine evidence from various approaches. Although it is not a matter of life and death, combining plays a vital role in forecasting'.

However, as Bates and Granger (1969) and more recently Kapetanios *et al.* (2008) and Banerghansa and McCracken (2010) observed, Combination Forecasting does not necessarily lead to better forecasting

performance. Bates and Granger's (ibid.) observations suggested that if unbiased forecasts are combined with biased forecasts, it is likely that this set is going to contain 'errors' rather than positively balanced forecasts. Kapetanios *et al.* (ibid.) commented that a combination forecast can reduce modelling accuracy if the correctly specified model is identified but the data generating process remains unchanged. Banternghansa and McCracken (ibid, p.65) also added that a combination approach should be used and interpreted with caution whereas '[good] past model performance does not always ensure [good] future model performance'.

Despite this criticism, theoretical and empirical findings (in fields other than commercial property), which date back more than forty years, suggest that Combination Forecasting often outperforms individual forecasts (Bates and Granger, 1969; Makridakis, 1989; Stock and Watson, 2004; Wallis, 2011). Combination Forecasting has been successfully applied within various fields of research, including business, economics and management (Bates and Granger, 1969; Stock and Watson, 2004; Kapetanios *et al.*, 2008; Pesaran and Pick, 2011), psychology (Einhorn and Hogarth, 1975; Libby and Blashfield, 1978; Langlois and Roggman, 1990).

Crane and Crotty (1967) combined Exponential Smoothing and Multiple Regression models, which subsequently increased the accuracy of their forecasts. The accuracy of correctly predicting the future trajectory of time-series increased from 55 percent to 79 percent.

Bates and Granger (1969) combined forecasts derived from Brown's Exponential Smoothing and ARIMA methods. The outcomes of the study resulted in a significant drop in variance of errors (from 170 to 122).

Deutsch *et al.* (1994) combined Switching Regression Models (Regime-Switching Models) and Smooth Transition Regression Models (STAR Models). Accordingly, this Combination Forecasting reduced forecasting error. In case of Model 1 in-sample MSE for the UK inflation rate was 7.03, while out-of-sample MSE dropped to 0.44.

Zou and Yang (2004) combined different ARIMA specifications. The cumulative model reduced error by 38 percent from that of Bayesian Information Criterion (BIC), and 49 percent from that of Akaike Information Criterion (AIC).

Assenmacher-Wesche and Pesaran (2008) averaged different Vector Error Correction with exogenous variables (VECX) model specifications. The results of the study suggested greater predictive accuracy of averaged forecasts over the best single VECX (2,2) model specification.

More recently, Pesaran and Pick (2011) assessed combination forecasts generated from a Time-Varying Regression Model over different estimation windows. The researchers concluded that averaging forecasts lowers Root Mean Square Forecasting Error (RMSFE). The RMSFE for rolling average forecast was 2 point lower than base-line post-break forecast.

In a following paper, Pesaran *et al.* (2011, p.36) estimated that Exponential Smoothing based forecasting combination for GDP growth improves forecasting accuracy. For example, the Mean Square Forecasting Error (MSFE) for equal weight forecasting for USA was 1.533, while it was 0.857 for Exponential Smoothing Forecasting Combination over a $h=2$ forecasting horizon.

Despite advantages of Combination Forecasting in producing greater modelling estimates, the application of this methodology within property has been limited (Fildes, 1991; Rapach and Strauss, 2007; Wang and Nie, 2008). Few studies have been published on the subject, with all of them investigating the residential property market (Bradley *et al.*, 2003; Pagourtzi *et al.*, 2005; Fleming and Kuo, 2007; Drought and McDonald, 2011; Gupta *et al.*, 2011).

Fildes (1991) combined forecasts obtained from the panel of construction industry experts issued in 'Construction Industry Forecasts' (now produced by Construction Products Association) and ex-ante econometric forecasts. The study identified that a combination forecast does improve forecasting

performance. The Mean Average Error (MAE) for private commercial sector (0 lags) was 3.73 from a combined model, while it was 4.18 (0 lags) from the expert predictions.

Bradley *et al.* (2003) developed a house price forecasting combination system. The system combined Repeated Sales model, Hedonic model, and Neural Network based model. First, the system computed estimates for each individual model. It then combined these models into one equation. As the authors claimed, this technique increased forecasting accuracy, whereas it is 'free of human biases and inconsistency inherent in manual appraisals' (ibid., p.10).

Pagourtzi *et al.* (2005) proposed a so called 'theta model' to forecast quarterly and monthly UK House Price Index values. The basic principle behind this methodology is that it divides an initial time-series into components, known as θ -lines. There, the θ -line, as the authors suggested, is 'local curvature of the time-series' (ibid., p.80). Subsequently, the model forecasts each of these θ -lines separately. A final forecast is obtained by simply combining θ -line forecasts into one. To forecast quarterly figures the commentators employed four modelling techniques, including Fixed Level Exponential Smoothing (Simple), Linear Trend Exponential Smoothing (HOLT), Damped Trend Exponential Smoothing (DAMPED) and a combination of HOLT and naïve methods. As this forecasting exercise suggested, the 'theta model' produced the most accurate forecast for quarterly figures.

Rapach and Strauss (2007) assessed whether a combination of individual forecasting models improves forecasting accuracy of US house price growth. The authors employed an Autoregressive Distributed Lag (ARDL) forecasting approach. Forecasts were produced for eight individual US District states for four and eight quarters ahead. The predictive ability of each model was assessed by comparing them against AR specification, which served as a benchmark. Subsequently, individual ARDL models were combined using three types of combination methods. The first was

simple combination approach. Second method used weighting principle. The final combination method was based on 'clustering', where forecasts were grouped on the basis of their Mean Squared Forecast Error (MSFE). The study estimated that 'the combining method forecast is more accurate than the AR benchmark forecast in terms of MSFE', with the cluster combining method being the most accurate (ibid., p.41). Their cluster forecasts were on average fifteen percent more accurate compared with the AR benchmark at the four quarters horizon, and thirty percent more accurate compared with the AR benchmark for eight quarters horizon.

Fleming and Kuo (2007) developed an algorithm to predict the US real estate values. The algorithm was primarily based on weighted values of at least two different forecasting models' outcomes. Forecasting methods which this algorithm comprised included Hedonic Method, the Repeat Sales method, the Tax Assessment method, and the Neural Network method. As the results of the study indicated, the combined model contained lower Proportional Prediction Error (PPE). The PPE for the four model combination was 0.0124, while it was 0.0347 for a single Neural Network model.

Wang and Nie (2008) combined Grey Dynamic (GD), BP Neural Networks, and Support Vector Machines (SVM) models, to forecast the Shanghai Real Estate Index. The authors compared individual performance of each model against an optimally weighted linear combination of all three models. The findings of the research indicated that the average forecast effectiveness of the combined method is greater than that of any single method. Forecast effectiveness of the combined model was 96.8 percent, against 66.2 percent of that of SVM-based model.

Drought and McDonald (2011) forecasted New Zealand house price inflation. The authors employed Equal Weights and Mean Squared Error Weights combination approaches. Combination Forecasts for house prices were compared against both individual model outputs and the Reserve Bank of New Zealand's (RBNZ) house price forecasts. Surprisingly, as the

results of the study suggested, forecasts from the best-performing model were more accurate than Combination Forecasts. On the other hand, the researchers suggested that Combination Forecasts had better predictive potential. It was noted that Root Mean Squared Errors (RMSE) of the Combination Forecasts and individual models were very similar and that Combination Forecasts were less biased as well as more resilient to structural breaks and misspecification biases than individual model forecasts. The subsequent comparison of the forecasting accuracy of MSE-weighted combination forecasts and the RBNZ forecasts suggested Combination Forecasts as being more accurate. For the year 2006, RMSE of the Combination Forecast was 1.99 while it was 2.79 from RBNZ's model outputs. For 2010 Combination Forecast's RMSE was 2.18, RBNZ's – 2.41. Drought and McDonald (ibid.) therefore suggested that a combination approach produces more accurate house price forecasts and it should be considered in any forecasting process.

Cabrera *et al.* (2011) employed a number of econometric specifications to forecast international securitised real estate returns. The models under study were the Autoregressive model (AR), Exponential Generalized Autoregressive Conditional Heteroscedasticity model (EGARCH), Functional Coefficient model (FC), Feedforward Artificial Neural Network (NN), and Nonparametric Regression model (NP). The authors also employed two simple combination forecasts of AR (1), NN (1,5), FC (1,200), and NP (200, 400) models, and AR (1), EGARCH (1,1), NN (1,5), FC (1,200), and NP (200, 400) models. As the empirical results suggested, Combination Forecasting improved forecasting performance for international securitised real estate returns, although an improvement was not significant. For example, Mean Squared Forecast Error (MSFE) for the UK series was 1.007 for AR (1), while it was 0.998 for both Combination I and Combination II.

In their empirical study, Gupta *et al.* (2011) assessed forecasting accuracy of alternative time-series models in predicting the dynamics of the US real house price index. The researchers employed a Dynamic Stochastic

General Equilibrium (DSGE) model and alternative time-series specifications, including VAR model, benchmark univariate BVAR model (UBVAR), small-scale BVAR model (SBVAR), large-scale BVAR (LBVAR), single-equation model (UFAVAR), multiple-equation model (MFAVAR), Bayesian single-equation VAR (BUFAVAR), and Bayesian multiple-equation VAR (BMFAVAR) model. The authors also used two Combination Forecasts. The first was based on 10 best models. Second Combination Forecast contained 10 best models and DSGE specification. The Combination Forecasts were computed simply averaging all model outcomes. As the modelling results indicated, the Combination Forecast came as the 'best forecasting method, based on the RMSE' (ibid., p.2020).

Therefore, the current research assesses whether combination forecasts from different forecasting techniques are better than single model outputs. It examines which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best.

3.2.2 The key methods of combination

Combination Forecasting can be produced by simply averaging different forecasts or employing more complex techniques (Makridakis, 1989; De Gooijer and Hyndman, 2006; Goodwin, 2009; Pesaran and Pick, 2011). The major principle of forecast averaging is simply by computing the average of two forecasts for the forecasting period (Mahmoud, 1984). Here, each variable carries equal weight, i.e. if two variables are combined, both get 50 percent, if three variables – each gets 33 percent, if four – 25 percent, et cetera. The criticism behind so called Simple Averaging, however, is that this approach disregards the historic accuracy of the models, as well as the possible relationship between forecasts (Stock and Watson, 2004; De Gooijer and Hyndman, 2006).

An alternative model combination approach is Weighted Combination Forecasting (Makridakis *et al.*, 1998; Yaffee and McGee, 2000; Armstrong, 2001). The weighting technique has two basic alternatives. One is

historical weighting, which gives weights to the forecasts based on their historic fit. In many cases, each forecast is weighted according to its Mean Squared Error (MSE). The second approach is subjective weighting, which is also known as Bayesian approach. Using this approach, weights to the forecasts are assigned by forecasters themselves based upon their personal experience and judgements as to which model fits and represents the historic data best (Mahmoud, 1984).

Despite the fact that a Weighted Combination approach appears to be popular, Armstrong (2001) highly criticised it. As he noted, one should use equal weights unless there is evidence suggesting unequal weighting of forecasts. In other words, he favoured Simple Averaging. The effectiveness of Simple Averaging over weighting was also advocated by Chan *et al.* (1999) and Kapetanios *et al.* (2008). Chan *et al.* (1999) suggested that simple Combination Forecasting worked especially well in their study. According to Kapetanios *et al.* (2008), Simple Average Combination Forecasting was more accurate in forecasting the UK GDP growth over the Weighted Combination Forecasting.

The regression, also known as Ordinary Least Squares (OLS), based combination approach, is a more advanced combination technique (Yaffee and McGee, 2000). Using this combination approach, weights to competing specifications are computed from regression (OLS) estimates. Model estimates are regressed against the dependent variable. The obtained coefficients then become weights for each specification which is to be combined.

However, as Chan *et al.* (1999) suggested, the difficulty with OLS combination is that it is not applicable when more than two forecasts are combined. Similar findings were presented by Swanson and Zeng (2001). As the researchers identified, when more than two forecasting models are combined using a regression combination approach, it increases the level of colinearity among competing forecasts which subsequently reduces the significance of the combination. De Gooijer and Hyndman (2006) also

noted that simple OLS based combination methods often perform quite poorly due to the possible presence of the serial correlation between forecasts. Goodwin (2009) also added that this approach is sensitive to extreme forecasts, which can negatively affect the combination.

Regardless of this criticism, the OLS combination technique proved to be useful. The study of Diebold and Pauly (1990, p.504) suggested that regression-based combination or as in their case 'flexible unconstrained regression-based forecast combination framework' yielded improvements for US GDP forecasting. Yaffee and McGee (2000) demonstrated the usefulness of Regression Combination forecasts in predicting the US Defence and Space Gross Product Value Index. Empirical evidences from Bunn and Oliver (1989), Weinberg (1986), Miller *et al.* (1992), and Rapach and Strauss (2007) were also in favour of OLS combination.

As such, the research adopts the principle of Combination Forecasting as a robust methodology helping to improve the accuracy of commercial property market modelling and forecasting. It examines which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best.

The following section comments on the model implementation using PASW 18 (known as SPSS) statistical package. It covers key modelling functions, as well as presents with some additional information on auxiliary functions of this statistical package. The section also covers difficulties associated with spread-sheets when employed for time-series modelling purpose.

3.3 Model implementation

3.3.1 Modelling process using PASW (SPSS) 18

The modelling is performed using the forecasting module of IBM SPSS Statistical Product 'PASW18'. PASW 18 is statistical analysis software which helps with data collation and mining. It also contains a module of advanced statistical analysis for predictive solutions (IBM Corporation, 2010).

The forecasting module of PASW 18 provides two major tools. One is 'Time-Series Modeller', which creates time-series models and produces forecasts. Second is 'Apply Time-Series Models', which applies existing time-series models onto selected datasets. The 'Time-Series Modeller' predicts future values of the dependent variable based on its past estimates. Unlike regression, it measures a single variable over time and uses its statistical properties (average, mode, trend, seasonality, etc.) to derive forecasts. There, time itself is a predictor. The forecasting module also allows for the incorporation of explanatory variable(s) if needed (PASW, 2010a).

Time-series modeller creates ARIMA, multivariate ARIMA, i.e. ARIMAX, and Exponential Smoothing time-series models. It also assesses models' major statistical properties. It measures their goodness-of-fit, Autocorrelation and Partial Autocorrelation.

The modelling procedure starts with the selection of the dependent variable. Then, the forecasting method, whether it is Exponential Smoothing or ARIMA, is defined. Subsequently, the forecasting period is specified and modelling details are indicated.

For ARIMA modelling, there are several model specification options. This involves defining of Autoregressive (AR) and Moving Average (MA) components, as well as degree of differencing. Following PASW (2010a), ARIMA modelling starts with a specification of a structure for the model. The Autoregressive order (p) specifies which previous values from the

series are used to model current values. The Differencing order (d) can be used to remove trend if it is present. Moving Average (q) order uses deviations from the series average of previous values to predict current values. The 'Dependent Variable Transformation' can be specified before dependent variables are used in modelling.

The 'Statistics and Forecast Tables' option allows displaying model fit measures. These measures are R-square, Stationary R-square, Root Mean Square Error (RMSE), Mean Absolute Percentage Error (MAPE), and Mean Absolute Error (MAE). This option also computes comparison statistics, including Goodness of fit, Residual Autocorrelation Function (ACF) and Residual Partial Autocorrelation Function (PACF), as well as statistics for individual models (Parameter estimates).

The 'Plots' tab provides an option to display the modelling results and all the above noted characteristics. The 'Output Filter' tab gives the option to choose output results according to the criteria selected (Best-fitting models or Poorest-fitting models). The 'Save' tab allows to save model specifications, confidence intervals and residuals. Finally, the 'Option' tab makes possible to set the forecasting period, specify the handling of missing values, set the confidence intervals, and set the number of lags shown for autocorrelations.

Simple Regression, Multiple Regression and VAR specifications are produced using PASW 18 Regression function (PASW, 2010b). As a standard regression module, it allows for the selection of the dependent and independent variables. It also provides an option for the modeller to introduce Weighted Least Squares (WLS) which allows estimating regression models with different weights for different cases. Functions such as 'Save' and 'Option' are the same as for the Time-Series modelling module (PASW, 2010b).

3.3.2 Difficulties working with spread-sheets

Although PASW 18 is a comprehensive software package, it is nevertheless considered a generalised statistical tool with built-in data mining and data management algorithms. For time-series analysis it is recommended to use more specialised econometric software packages such as Eviews or OxMetrics. These specialised econometric packages offer more scope for time-series analysis, as well as power to create new econometric, statistical and mathematical forms (Timberlake, 2013).

The non-availability of specialised computer packages had an effect on the capacity of the current research. The research employs all except one real estate modelling technique indicated in Figure 2.3 (Section 2.2.1). The research does not estimate an Econometric model. As the Econometric model incorporates a system of equations and combines multiple relationships and interactions within the system, it therefore becomes difficult to compute using available software. In the case of MS Excel, the input X Range (number of explanatory variables) cannot contain more than sixteen variables (Microsoft Excel, 2010). In case of PASW 18, the system finds it difficult to deal with more than fifty regressors. What is more, some equations, which are part of an Econometric system, may not be recursive. According to Brooks and Tsolacos (2010), these equations therefore cannot be estimated using Ordinary Least Squares (OLS). The commentators subsequently recommend using Indirect Least Squares (ILS), Two-Stage Least Squares (2SLS or TSLS), and Instrumental Variables as alternative approaches. PASW 18, however, does not allow for any of these options. In addition to that, PASW 18 does not estimate model fit statistics such as Mean Error (ME), Mean Squared Error (MSE), and Mean Percentage Error (MPE), as well as Akaike and Bayesian Information criteria.

Moreover, there are a number of other difficulties associated with PASW 18 as with any other spread-sheet. Koop (2006) presents a good discussion on the subject. According to the commentator, spread-sheets

are somewhat awkward in obtaining empirical results, e.g. creating lagged variables requires constant copying and pasting of data. In situations when one is working with several equations, it becomes even more difficult. Certain statistical measures and procedures such as variance decomposition, impulse response and spectral analysis are difficult to produce using spread-sheets. Accordingly, Koop recommended using more specialised statistical packages if one plans to work extensively with financial time-series.

Considering unavailability of these specialised software packages, the research continues with PASW algorithm which is used to compute five univariate time-series methods including Single Exponential Smoothing, Holt's Linear Trend, Brown's Linear Trend, ARIMA and ARIMAX, as well as three regression based models including Simple Regression, Multiple Regression and Vector Autoregression (VAR).

The next section of this Chapter presents formulae of modelling technique used for this research. It also covers statistical difficulties which are encountered when building a real estate model, including issues of autocorrelation and heteroscedasticity, and Information Criteria.

3.4 Formulation of real estate models

3.4.1 Single Exponential Smoothing model

As it was noted earlier in Section 2.2.1, the advantage of Single Exponential Smoothing is that it requires little storage of historical data and fewer computations. The principle equation of this specification which is used for the research is as follows (Makridakis *et al.*, 1998):

$$F_{t+1} = \alpha Y_t + (1 - \alpha)F_t \quad (1)$$

Where F_t is the forecast from a previous period, F_{t+1} is the forecast for the next period, Y_t is the most recent observation and α is a constant between 0 and 1. In econometrics α is also known as weighting factor. Forecasts using this formula are produced by adding a forecast from a previous period to the most recent observation with an adjustment for the error that occurred in the last forecast. This adjustment is achieved by using a geometrically declining weighting approach.

3.4.2 Brown's Linear Trend model

Brown's Linear Trend (BLT) model is similar to SES specification. However, it is rewritten in such a form that it minimises the effect of the weighting factor α . In this case, Brown's Linear forecast is the old forecast plus an adjustment for the error that occurred in the last forecast. The principle equation of BLT, which is used for the current research, is as follows:

$$F_{t+1} = F_t + \alpha(Y_t - F_t) \quad (2)$$

As it is seen from Equation 2, the weighting factor accounts for the most recent observation of the series being modelled, as well as forecast from a previous period.

3.4.3 Holt's Linear Trend model

According to PASW 18 (PASW, 2010a), Holt's Linear Trend (BLT) model, also known as Double Exponential Smoothing, is a special case of BLT. It uses two smoothing constants α and β (both being between 0 and 1) and a three-set-equation. The three-set-equation which is adopted for the research is as follows:

$$L_t = \alpha Y_t + (1 - \alpha)(L_{t-1} + b_{t-1}) \quad (3a)$$

$$b_t = \beta(L_t - L_{t-1}) + (1 - \beta)b_{t-1} \quad (3b)$$

$$F_{t+m} = L_t + b_{tm} \quad (3c)$$

Where L_t is an estimate of the level of the series at a time period t , and b_t is an estimate of the slope of the series at the same time period t .

The Equation 3a adjusts L_t to the trend of the previous period by adding b_{t-1} to the least smoothed value L_{t-1} . The Equation 3b updates this trend which is equal to the difference between two last values smoothed by β plus the trend multiplier $(1 - \beta)$. Equation 3c subsequently forecasts ahead.

3.4.4 ARIMA model

Autoregressive Integrated Moving Average (ARIMA) specification, as it has been noted in Section 2.2.1, is the combination of the autoregressive operator AR of order p , and the moving average MA operator of order q . The basic representation of Autogression (AR) is as follows (Makridakis *et al.*, 1998; Brooks and Tsolacos, 2010):

$$Y_t = \mu + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + u_t \quad (4)$$

Where Y_t is the current value of dependent variable, y_{t-p} is past values of the variable itself, μ is constant term, ϕ_j is j th order autoregressive parameter, and u_t is the error term at a time period t .

The principal representation of Moving Average (MA) process is presented in the following equation:

$$Y_t = \mu + b_1u_{t-1} + b_2u_{t-2} + \cdots + b_qu_{t-q} + u_t \quad (5)$$

Where μ is a constant term, b_j is j th moving average parameter, and u_t is the error term at a time t .

It is important to note that the Moving Average within the ARIMA framework differs from the conventional Moving Average concept. Here it is defined as a Moving Average of errors and not as an average of past values of Y_t (Johnson, 1992; Makridakis *et al.*, 1998).

Subsequently, both AR and MA processes are paired together, creating a class of time-series models ARIMA (Box *et al.*, 1994; Makridakis *et al.*, 1998; Brooks and Tsolacos, 2010). The full model specification which is adopted for this research is formulated as follows:

$$Y_t = \mu + \phi_1y_{t-1} + \phi_2y_{t-2} + \cdots + \phi_py_{t-p} + b_1u_{t-1} + b_2u_{t-2} + \cdots + b_qu_{t-q} + u_t \quad (6)$$

As the empirical studies on the subject suggested, ARIMA models can have any AR and MA orders (Makridakis *et al.*, 1998; McGough and Tsolacos, 2010). However, the current research uses maximum of the order 4. This comes from the discussion on property cycles which suggested the existence of a minor property cycle of 4 years duration (RICS, 1999; Barras, 2009). For annual time-series it is assumed that a greater order is not relevant as fifth and subsequent orders are likely to capture dynamics of the previous business/property cycle.

Information Criteria

The ARIMA model flexibility creates a difficulty in deciding which model specification is the most appropriate. As such, measures known as 'Information Criteria' are recommended in selecting the best ARIMA model

specification. As it was identified in Section 2.2.1, Akaike Information Criterion (AIC) and Bayesian Information Criterion (BIC) are two common ones used by property market researchers. Whereas AIC and BIC are two competing specifications and each has its strengths and weaknesses, the current study therefore employs both specifications for the research.

According to Akaike (1973), AIC formulation chooses the correct dimensionality of a model amongst n th order models. The AIC is computed following Burnham and Anderson (2002):

$$AIC = n * \ln(\hat{\theta}) + 2 * K \quad (7)$$

Where K is the number of free parameters in the model, n is the length of the time-series, and $\hat{\theta}$ is likelihood. Likelihood is subsequently estimated using the following equation:

$$\hat{\theta} = RSS/n \quad (8)$$

Where RSS is Residual Sum of Squares obtained from the regression.

In situations when sample size is relatively small, i.e. $n/K < 40$, AIC requires a bias-adjustment. In this case, the size of the data set n increases in weight in comparison to the number of parameters K . Accordingly, the bias adjustment term becomes less important (Burnham and Anderson, 2002):

$$AIC_c = AIC + 2K(K + 1)/(n - K - 1) \quad (9)$$

The principle equation of the Bayesian Information Criterion (BIC) is as follows:

$$BIC = n * \ln(\hat{\theta}) + (K + 1) * \ln(n) \quad (10)$$

Where n and K are the same estimates as for AIC.

3.4.5 ARIMAX model

The formulae for an Integrated Autoregressive Moving Average model with an Exogenous Explanatory Variable(s), also known as ARIMAX specification, is expressed as follows:

$$Y_t = \mu + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \sum_{i=0}^n \gamma_i X_{t-i} + b_1 u_{t-1} + b_2 u_{t-2} + \dots + b_q u_{t-q} + u_t \quad (11)$$

Where Y_t is the current value of dependent variable, μ is constant term, y_{t-p} is past values of the variable itself, ϕ_j is j th order autoregressive parameter, b_j is j th moving average parameter, u_t is the error term at a time t and X_t is a vector of explanatory variable(s).

3.4.6 Simple Regression model

The fundamental equation which describes Simple Regression presented in the equation below (Koop, 2006; Brooks and Tsolacos, 2010):

$$y = \alpha + \beta x \quad (12)$$

Where y is the dependent variable, x is an explanatory variable, α is intercept and β is the slope.

As was suggested in Section 2.2.1, the principle of Simple Regression is that an increase/decline in x will lead to an increase/decline in y . However, evidence suggests that this model may be difficult to apply in reality. It is impossible to determine with certainty that given any value x , value of y will be estimated accurately. To make it more realistic, a random disturbance term, or so called 'error' e is added into the equation. Subsequently, the model becomes (Brooks and Tsolacos, 2010):

$$y = \alpha + \beta x + e \quad (13)$$

However, even with an ‘error’ element, a linear regression model is only an approximation of reality (Koop, 2006). Therefore, in order to fit the model, it is recommended using an Ordinary Least Squares (OLS) approach (Brooks and Tsolacos, 2010). Here, the actual value of y_t at a period t is denoted with a fitted value \hat{y}_t , which is predicted by the model. Accordingly, α and β are replaced by OLS fitted estimates $\hat{\alpha}$ and $\hat{\beta}$:

$$\hat{y} = \hat{\alpha} + \hat{\beta}x + e \quad (14)$$

For the purpose of the current research, the model is rewritten as follows:

$$\hat{y}_t = \hat{\alpha} + \hat{\beta}x_t + e_t \quad (15)$$

The Equation 15 accounts for time-series data, where \hat{y}_t is a dependent variable at a period t , x_t is an explanatory variable at a period t , and e_t is an error term at the same period t .

3.4.7 Multiple Regression model

In many cases the situation that the dependent variable is influenced by only one explanatory variable is unrealistic. In property, business and economics, dependent variables are often influenced by more than one independent variable. This relationship is at the core of the Multiple Regression. Accordingly, a model with k number of regressors becomes:

$$y = \alpha + \beta_1x_1 + \beta_2x_2 + \cdots + \beta_nx_n + e \quad (16)$$

For the purpose of the research, time-series Multiple Regression becomes:

$$y_t = \alpha + \beta_1x_{1t} + \beta_2x_{2t} + \cdots + \beta_nx_{nt} + e_t \quad (17)$$

Where set of $x_{1t}, x_{2t}, \dots, x_{nt}$ represent group of explanatory variables, and set of $\beta_1, \beta_2, \dots, \beta_n$ is a group of regression coefficients at the time period t .

In this case, however, each coefficient represents only a limited impact the explanatory variable has on the dependent variable. It means that a certain regression coefficient measures the effect a corresponding variable has on the dependent variable, after eliminating the effects of the remaining variables. The advantage of multiple regression is that it makes the most of the interdependence of the explanatory variables to model a dependent variable (Makridakis *et al.*, 1998).

Durbin-Watson test

As it was noted in Section 2.2.1, when building any regression specification, there is always a need to assess whether Autocorrelated disturbances are present within the model. It was suggested that Durbin-Watson (DW) test is a standard in testing for Autocorrelation. Following Stevenson and McGarth (2003), the DW specification is expressed as:

$$DW = \frac{\sum_{t=2}^n (\varepsilon_t - \varepsilon_{t-1})^2}{\sum_{t=1}^n \varepsilon_t^2} \quad (18)$$

Where e_t is an error of at the period t .

Gujarati (2005) suggests that the Durbin-Watson statistics ranges from 0 to 4 with a value around 2 indicating non-autocorrelation. In case of modelling with PASW 18, if Durbin-Watson value is between 1.5 and 2.5, it indicates that values are independent (PASW, 2010b).

White's test for heteroscedasticity

The discussion in Section 2.2.1 also suggested a need to test for the presence of heteroscedasticity. It was identified that White's test (WT) is one of the most popular checks in assessing whether errors are constant across the sample. The difficulty with PASW, however, is that it does not test directly for heteroscedasticity. Therefore, White's test using PASW package is performed following a particular algorithm: first, squares of regression residuals (unstandardised) and explanatory variables are computed. Then, cross product of the explanatory variables is created by

multiplying all explanatory variables. Following on from this, regression is performed with squares of residuals being the dependent variable and squares of explanatory variables and the cross product being independent variables:

$$R^2 = \beta_1 + \beta_2 x_{1t} + \cdots + \beta_k x_{kt} + \beta_{k+1} (x_{1t})^2 + \cdots + \beta_{k+n} (x_{kt})^2 + \beta_{k+n+1} (x_{1t} * \dots * x_{kt}) \quad (19)$$

Here β_k is regression estimates and x_{kt} is explanatory variables. Subsequently, WT value is calculated by multiplying n , which is the number of observations, and R^2 obtained from the regression. Finally, the obtained value is compared with χ^2 (chi-square):

$$WT = n * R^2 < \chi^2 \quad (20)$$

Accordingly, if χ^2 is greater than the WT value, then the hypothesis is rejected. It implies that the test did not find a problem (Gupta, 1999).

3.4.8 Vector Autoregression model

The simplest case of this method is VAR with two variables (Koop, 2006; Brooks and Tsolacos, 2010). There one variable depends on p lags of itself and q lags of the other variable. The mathematical representation of this interdependence is as follows:

$$y_t = \alpha_1 + \delta_1 t + \phi_{11} y_{t-1} + \cdots + \phi_{1p} y_{t-p} + \beta_{11} x_{t-1} + \cdots + \beta_{1p} x_{t-p} + e_{1t} \quad (21a)$$

$$x_t = \alpha_1 + \delta_1 t + \phi_{11} x_{t-1} + \cdots + \phi_{1p} x_{t-p} + \beta_{11} y_{t-1} + \cdots + \beta_{1p} y_{t-p} + e_{1t} \quad (21b)$$

This set of equations results in a model known as VAR (p). The model has two variables, intercept, deterministic trend and p lags of each of the

variables. VAR (p) models with more variables are obtained in the comparable way (Koop, 2006).

As Koop (ibid.) maintains, once all variables selected for the model are stationary, modelling, model estimation and testing is performed in the standard way. Estimates for each equation are then obtained using OLS. Acquired figures for P-values and t -statistics indicate whether variables are significant.

3.4.9 Combination Forecasting

As it was established in Section 3.1, the current research adopts the principle of Combination Forecasting as a robust methodology helping to improve the accuracy of commercial property market modelling and forecasting. It uses two combination approaches, i.e. Simple and Regression (OLS) based averaging. These two particular combination techniques have proved to be useful in improving the accuracy of modelling and forecasting within business and economics (Makridakis, 1989; Pesaran and Pick, 2011; Wallis, 2011).

The difficulty with OLS based Combination Forecasting, however, is that previous empirical studies estimated that it is not applicable when more than two forecasts are combined. Findings presented by Swanson and Zeng (2001), De Gooijer and Hyndman (2006) and Goodwin (2009) suggested that a combination of more than two models reduces the significance of the combination, it results in the presence of serial correlation between forecasts, as well as the combination becomes sensitive to extreme forecasts. Therefore, the current study combines only two competing forecasts at a time.

Considering a **Simple Combination** forecast, a combination of two forecasts is formulated as follows (Yaffee and McGee, 2000):

$$CF_t = (F_{1t} + F_{2t})/2 \quad (22)$$

Where CF_t is Combination Forecasting, F_{1t} is first model outcome and F_{2t} is second model outcome.

In case of **Regression Combination**, the function comprises intercept and two regression coefficients plus an error term (Yaffee and McGee, *ibid.*; Landram *et al.*, 2009):

$$CF_t = \beta_0 + \beta_1 F_{1t} + \beta_2 F_{2t} + e_t \quad (23)$$

Where β_0 is intercept, β_1 and β_2 are regression coefficients, and e_t is an error term (Yaffee and McGee, *ibid.*).

3.4.10 Further steps in formulating a real estate models

Stationarity and Unit-Root testing

In order to proceed with time-series modelling, there is a need to transform non-stationary data into stationary. The concept of stationarity is important for time-series analysis (Koop, 2006; Brooks and Tsolacos, 2010). In general, the term 'stationarity' implies that data does not exhibit growth or decline, i.e. time-series fluctuate around its constant mean through the whole period (Makridakis *et al.*, 1998). As Box *et al.* (1994, p.23) explains, 'stationary processes is based on the assumption that the process is in a particular state of statistical equilibrium'.

Non-stationarity, on the other hand, results in a positive autocorrelation, which, according to Koop (2006, p.143), means that time-series is highly correlated with past values of itself, i.e. it 'remembers the past'. As Koop suggests, non-stationary or unit-root variables should not be included into any regression model. According to the author, 'if Y and X have unit roots then all the usual regression results might be misleading and incorrect' (*ibid.*, p.167). He also adds that most of the statistical packages like Excel implicitly assume that all selected variables are stationary when they calculate P-values. If the explanatory variables are non-stationary, the regression results become automatically invalid. Brooks and Tsolacos (2010) also add that non-stationary data can generate spurious

regressions. Accordingly, if non-stationary variables are used for the regression modelling, then standard assumptions for asymptotic analysis become violated. Subsequently, Koop (ibid., p.167) suggests that one 'should never run a regression of Y on X if variables have unit roots'.

In order to proceed with time-series modelling, non-stationary data must be converted into stationary. Non-stationarity in a time-series is achieved through 'differencing'. The differenced series is defined as a change between current and previous values of time-series itself. Accordingly, this arithmetic transforms data into stationary series. However, in some cases there might be a necessity to difference the series a second time (Makridakis *et al.*, 1998). The major notation of differencing is as follows (Makridakis *et al.*, 1998):

$$y'_t = y_t - y_{t-1} \quad (24)$$

Accordingly, this simple calculus transforms data into stationary series. However, in some cases there might be a necessity to difference the series a second time. If the mean of the series wanders and the variance is not reasonably constant over time, then series is differences one more time. Second-level differencing is performed as follows (Makridakis *et al.*, 1998):

$$\begin{aligned} y''_t &= y'_t - y'_{t-1} = (y_t - y_{t-1}) - (y_{t-1} - y_{t-2}) \\ &= y_t - 2y_{t-1} + y_{t-2} \end{aligned} \quad (25)$$

One way of assessing stationarity is by looking at the time-series itself. As Makridakis *et al.* (1998) suggest, if the time-series shows no evidence of change in its mean and change in the variance over time, then it all indicates that the series is stationary. Both Autocorrelation (ACF) and Partial Autocorrelation (PACF) plots can aid additional information as to whether the time-series is stationary or not. According to Makridakis *et al.* (ibid.), if Autocorrelations drop to zero relatively quickly, it indicates that series are stationary. If, however, Autocorrelations decrease slowly, it is a

clear sign of non-stationarity. If Partial Autocorrelation graph spikes in a first lag and is outside 95 percent limits, it indicates that series are non-stationary.

A more robust way for examining stationarity is by testing for a unit root. The most widely-used is Dickey-Fuller test (Brooks and Tsolacos, 2010). Using PASW 18 statistical package, this test is performed following the algorithm suggested by Koop (2006). First, AR(1) specification is created to examine ϕ value of series. Then, first difference Δy_t values are computed. Following on from this, Δy_t is then regressed on lagged values of time-series itself, i.e. y_{t-1} . Accordingly, regression estimates of t -statistics and ρ are compared against Dickey-Fuller critical values.

Testing for Granger causality

Another important step in formulating a real estate model is testing for Granger causality. The principle of Granger causality is in the way explanatory variables influence dependent variables. Here, if past values of an explanatory variable affect current values of the dependent variable, then it means that the explanatory variable Granger causes dependent variable.

In his original paper, Granger (1969, p.428) identified causality as 'the relationship between two (or more) variables when one is causing the other(s)'. According to Kirchgassner and Wolters (2007, p.100) this assumption is at the core of the general equilibrium theory which assumes that 'everything depends on everything else'.

As Koop (2006, p.184) suggests, the principle of Granger causality implies that 'events in the past can cause events to happen today'. More specifically, if past values of variable X explains variable Y, it then suggests that X Granger causes Y. Certainly, this relationship does not constitute an ultimate causality, this is why it is called 'Granger causality'. Nevertheless, the hypothesis is that if past values of an explanatory variable influence current values of a dependent variable, then the explanatory variable can cause the dependent variable.

Hendry and Mizon (1999) suggest that Granger causality is pervasive and highly important for econometric modelling. The authors identified ten aspects of econometric modelling in which Granger causality plays an important role. One of these aspects is so called ‘model marginalising with respect to unwanted variables’, which states that certain variables can be excluded from the equation based on the statistics of their lagged values (ibid., p.103).

The current study adopts a two-step algorithm to test for Granger causality suggested by Koop (2006). Koop’s algorithm is universally applicable and easy to adopt. First, the maximum possible lag length q_{max} is selected. Then, Distributed Lag Model (DLM) is estimated. The major representation of the model is as follows:

$$Y_t = \alpha + \beta_1 X_{t-1} + \dots + \beta_{q_{max}} X_{t-q_{max}} + e_t \quad (26)$$

If P-value for variable(s) is less than significance level chosen, then this lag should be selected. Otherwise, a further regression analysis is performed with Distributed Lag Model estimated for lag q_{max-1} .

$$Y_t = \alpha + \beta_1 X_{t-1} + \dots + \beta_{q_{max-1}} X_{t-q_{max-1}} + e_t \quad (27)$$

If P-value of this equation is significant, this lag length is chosen. Otherwise, lag length is shortened by one.

In general, Koop (2006) proposed a simple rule in determining whether a variable is significant or not. According to the author, ‘if you find any or all of the coefficients $\beta_1 \dots \beta_q$ to be significant using t -statistics or the P-values of individual coefficients, you may safely conclude that X Granger causes Y . If none of these coefficients is significant, it is probably the case that X does not Granger cause Y ’ (ibid., p.186).

Measuring model accuracy

Following Makridakis *et al.* (1998) and Brooks and Tsolacos (2010), accuracy measurement is an important issue in modelling property market.

According to Makridakis *et al.* (ibid.) in many instances, 'accuracy' is referred to 'goodness of fit', with both terms indicating how well the model is able to reproduce the data that is already known. As Brooks and Tsolacos (ibid., p.115) suggest, these measures assess 'how well does the model...that was proposed actually explain variations in the dependent variable?'.

The issue here, however, is, as De Gooijer and Hyndman (2006, pp.457) comment, 'a bewildering array of accuracy measures [which] have been used to evaluate the performance of forecasting methods'. Mahmoud's (1984) survey of relevant literature identified a number of accuracy measures available, including Mean Error (ME), Mean Absolute Deviation (MAD), Mean Squared Error (MSE), Mean Percentage Error (MPE), Mean Absolute Percentage Error (MAPE), Adjusted Mean Absolute Percentage Error (AMAPE), Theil's U-statistics (U), Root Mean Squared Error (RMSE), the Coefficient of Variation (CV), the Coefficient of Determination (CD), R-Squared, Adjusted R-Squared, Turning Points (TP's), and Hits and Misses (HM). Tsolacos (2006) added few more accuracy measures including Bias Proportion, Variance Proportion, Covariance Proportion, and Gain in Forecast. De Gooijer and Hyndman (2006) suggested using as they call 'a novel alternative measure of accuracy' which is 'Time Distance' developed by Granger and Jeon (2003a; 2003b). Alternative approaches in testing accuracy of competing forecasts are Diebold and Mariano's (1995) test, Clements and Hendry's (2003) 'Generalised Forecast Error Second Moment' (GFESM) criterion, as well as 'Tracking Signal' method, also known as 'Trigg's technique' (Trigg, 1964; Cembrowski *et al.*, 1975).

Although there is no universally accepted forecasting accuracy measure, it is nevertheless possible to identify those which are coming before all others in importance. As the literature on the subject suggests, there are three components which help in selecting the accuracy measures. One accounts for modelling technique which has been employed. Following Mahmoud (1984), for the linear structure the most applicable are Mean Error (ME), Mean Absolute Error (MAE), Mean Absolute Percentage Error

(MPAE), Mean Squared Error (MSE) and similar accuracy measures, as they measure model deviations from a stationary time-series. According Mahmoud (ibid.), if used in different settings, e.g. with non-linear structures, these accuracy measures will produce inappropriate results. The second component suggests using so called 'Standard Statistical Measures'. According to Makridakis *et al.* (1998), Mean Error (ME), Mean Absolute Error (MAE), and Mean Squared Error (MSE) are all standard statistical measures with Mean Percentage Error (MPE) and Mean Absolute Percentage Error (MPAE) being relative but frequently used measures. The third factor recommends looking across the literature on the subject and selecting the most frequently used accuracy measures. An analysis of publications on property market modelling, including Tsolacos (1995), Chaplin (1998; 1999), D'Arcy *et al.* (1999), Brooks and Tsolacos (2000; 2001), Stevenson and McGarth (2003), Karakozova (2004), Pekdemir (2009), to name a few, suggests that Mean Absolute Error (MAE), Mean Absolute Percentage Error (MAPE) and Mean Squared Error (MSE) are the most frequently used accuracy measures within the field.

However, Makridakis *et al.* (1998) argued that these accuracy measures assess only the goodness of fit of the model to historical data. Although this statistic is important in estimating the model behaviour, as well as its goodness to fit, it does not necessarily imply good forecasting performance. The authors therefore suggested that the series being modelled should be divided into two time periods normally called 'initialisation' set and 'holdout' set. The model should then be parameterised and tested on the initialisation set and forecasts made on the holdout set. It is suggested that whereas model is not parameterised on holdout set, forecasts produced on this period can be considered as being genuine. Accordingly, accuracy measures computed from the holdout sample indicate actual forecasting performance of the model. In the property literature, initialisation and holdout sets are sometimes called 'ex-ante' and 'ex-post' periods respectively (Chaplin, 1998; 1999; Tsolacos, 2006).

Following Chaplin (1998; 1999) and Makridakis *et al.* (1998), the out-of-sample forecasts can successfully be assessed using Theil's second inequality coefficient U . This statistical measure also allows for a relative comparison of selected forecasting methods with naïve approach. Naïve modelling approach means no-change or forecast obtained by guessing. As both Makridakis *et al.* (ibid.) and Chaplin (1999) identify, if U is equal to zero, then predictions are perfect. If it is equal to one, then the forecasts are the same as those that would be obtained using naïve forecasting approach. If, however, U is greater than 1, then there is no point in using formal forecasting method. In such a case a naïve approach would produce better results.

Accuracy measurement starts first by estimated forecasting error e_t . Here, it is simply calculated by subtracting forecast F_t at the period t from the actual observation Y_t of the same period. The formula for this equation is as follows:

$$e_t = Y_t - F_t \quad (28)$$

The Mean Absolute Error (MAE) and Mean Squared Error (MSE) are then obtained from the following equations:

$$MAE = \frac{1}{n} \sum_{t=1}^n |e_t| \quad (29)$$

$$MSE = \frac{1}{n} \sum_{t=1}^n e_t^2 \quad (30)$$

To compute MAPE, however, there is a need to additionally estimate Percentage (sometimes called Relative) Error (PE). The formula for PE_t is as follows:

$$PE_t = \left(\frac{Y_t - F_t}{Y_t} \right) \times 100 \quad (31)$$

Once Percentage Error is estimated, MAPE is computed as follows:

$$MAPE = \frac{1}{n} \sum_{t=1}^n |PE_t| \quad (32)$$

However, as it was noted above, these accuracy measures assess only the goodness of fit of the model to historical data. The recommendation was to split time-series into 'initialisation' and 'holdout' sets and compute Theil's second inequality coefficient ' U_2 '. The literature concerning modelling and forecasting commented that this particular accuracy measure indicates actual forecasting performance of the model. Mathematically Theil's U-statistics is expressed as follows:

$$U = \sqrt{\frac{\sum_{t=1}^{n-1} (FPE_{t+1} - APE_{t+1})^2}{\sum_{t=1}^{n-1} (APE_{t+1})^2}} \quad (33)$$

Where FPE_{t+1} is forecast relative change and APE_{t+1} is actual relative change. There:

$$FPE_{t+1} = \frac{F_{t+1} - Y_t}{Y_t} \quad (34)$$

and

$$APE_{t+1} = \frac{Y_{t+1} - Y_t}{Y_t} \quad (35)$$

Here F_t is forecast and Y_t is observation at the time period t .

3.5 Summary

The chapter discussed the difficulty in using different forecasting methods. It was established that, as a standard procedure, property market researchers are selecting the single best model based on its accuracy or statistical complexity. However, this model selection process has been criticised as being unproductive, whereas rejected models may contain useful independent information.

Accordingly, the chapter introduced the principle of Combination Forecasting. This methodology has been successfully employed by economists to improve the overall forecasting accuracy. Even though research on Combination Forecasting has been marginal within property research with most of the studies being produced for residential property, the existing empirical results indicated a benefit of this procedure. Various authors used different forecasting techniques which produced Combination Forecasting using a range of combination principles. However, Simple and OLS based averaging were established as being the key combination techniques. The overall conclusion supported the usefulness of Combination Forecasting and suggested further research in this area. Given the gap in the UK commercial property market cycle modelling and forecasting knowledge, the current research project employs Simple Averaging (SA) and Regression (OLS) based combination to achieve greater predictive outcomes. The research subsequently assesses whether combination forecasts from different forecasting techniques are better than single model outputs. It examines which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best.

Following on, this chapter presented the modelling process of the current study. It first covered the general principles of model implementation using statistical software package PASW 18. It also assessed the issue of modelling using spread-sheets. Following on from this, the chapter presented each modelling technique used for the research, including

Single Exponential Smoothing (SES), Holt's Linear Trend (HLT), Brown's Linear Trend (BLT), ARIMA, ARIMAX, Simple Regression (SR), Multiple Regression (MR), and Vector Autoregression (VAR). It presented the principal formulae for Simple Averaging and OLS based Combination Forecasting (CF). Subsequently, the chapter addressed statistical difficulties related to the construction of real estate models, including autocorrelation, heteroscedasticity, as well as the issue of Information Criteria, and Granger causality.

Statistical package PASW 18 is commonly known as SPSS. There are two modelling functions within the system, which were used for the research. One is 'Time-Series Modeller', which allows computing time-series models. The other one is 'Regression' function which is used to compute regression specifications. PASW 18 is a popular software package commonly used within business and academia. However, it is considered as being less useful than specialised econometric packages, as its scope in creating econometric, statistical and mathematical forms is very limited.

As the discussion above suggested, Exponential Smoothing, whether it is Single Exponential Smoothing, Holt's Linear Trend, and/or Holt's Linear Trend, are all univariate models which require little storage of historical data and few computations. Both Single Exponential Smoothing and Holt's Linear Trend are expressed as single equations requiring only most recent observations of the dependent variable, a forecast and a constant. Brown's Linear Trend is a more complex smoothing algorithm expressed as a three-set-equation incorporating two smoothing constants, as well as estimates of the level of the series at a certain period of time.

Both ARIMA and ARIMAX models were identified as being more advanced modelling structures. The principle behind this approach is that it incorporates an autoregressive operator AR of order p , and the moving average MA operator of order q . In case of ARIMAX, it also contains a vector of an explanatory variable(s) X .

The study however encountered two difficulties with ARIMA(X) models which come from their flexibility. Issue one is that AR and MA components can have any order. They can range from 0 to any number. It was therefore decided to use a maximum order of 4 as for the annual series as greater order may capture dynamics of an earlier business/property cycle (Section 3.4.4). Issue two is in deciding which model specification is the most appropriate. The econometric literature suggests using techniques known as 'Information Criteria' helping to assess the best specified ARIMA structure. Two of the most common information criteria are Akaike Information Criterion (AIC) and Bayesian Information Criterion (BIC). Whereas these measures have their own strengths and weaknesses, it is decided to use them both.

Simple Regression, Multiple Regression and VAR models were estimated using PASW 18 'Regression' function. In the case of Simple Regression, the dependent variable is modelled with only one explanatory variable. In the case of Multiple Regression, the dependent variable is modelled with more than one explanatory variable. VAR model is constructed using p lags of the dependent variable and q lags of explanatory variables. All specifications are estimated using OLS approach.

As with univariate models, the study identified two issues related to the regression model building. One is presence of Autocorrelation, and another is presence of Heteroscedasticity. In the case of Autocorrelation, it was decided to use Durbin-Watson (DW) test to assess whether Autocorrelated disturbances are present within the models. To check for Heteroscedasticity, White's test was selected.

The study also employed Granger causality to assess the significance of the explanatory variables. The study adopted the algorithm proposed by Koop (2006), which suggested estimating the maximum possible lag length of an explanatory variable and checking for its significance. In case the variable is insignificant, lag length is shortened by one period and the

test is performed again. In case neither of the lags is significant, the explanatory variable is indicated as being irrelevant.

Finally, the chapter presented accuracy measures used for the research. To estimate in-sample accuracy, the study selected Mean Absolute Error (MAE), Mean Absolute Percentage Error (MAPE) and Mean Squared Error (MSE) accuracy measures. To assess an ex-post accuracy of each modelling structure, Theil's U-statistics is computed.

Having presented the methodology for the current research, the next chapter will discuss the data needed for building a forecasting model for the commercial property market.

CHAPTER 4 DATA AND ITS ACQUISITION

This chapter presents the data which was acquired for the research and examines its inherent characteristics. It is divided into four sections. Section 1 discusses the importance of historic data for the analysis of the commercial property market. It establishes that long-term series are necessary to build robust and reliable statistical models.

Section 2 assesses difficulties related to UK property data and its acquisition. The UK and especially London commercial property market data is considered as probably the best documented in Europe. However, as the evidences presented in this section suggest, it is not without criticism.

Section 3 presents the principle of Chain-linking as the statistically robust solution for time-series combination. This method is considered as being an effective time-series combination approach which is used by major organisations.

Section 4 evaluates properties of the dependent and explanatory variables. The research uses IPD All Property Rental Value Growth Index for the UK as the dependent variable. The subsequent analysis of the data-sets of seventeen organisations and thirteen publications enables to collect data on twenty-seven of explanatory variables. The chapter then presents five variable reduction techniques used for the research to determine the key variables. These variable reduction techniques are 'What Others Do', 'What Experts Advise', Stepwise Regression (Forward), Stepwise Regression (Backward), and Granger Causality. This combination of variable reduction techniques enables to produce the final 'Short List' of explanatory variables, which are Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment, and GDP. Accordingly, the latter seven variables are further used for the modelling.

4.1 The importance of historic data

In order to create a robust and reliable property market model, it is of great importance to use historic data. As noted by Solomou (1998), an historical perspective is essential in order to assess what generates cycles and how they have evolved. The long-term time-series analysis helps to understand important changes over time.

As Yaffee and McGee (2000, p.3) suggest, for proper parameter estimation and model building, time-series should contain 'enough observations'. Although there is no general agreement as to what 'enough observations' is, Yaffee and McGee recommend that if a series is cyclical or seasonal, then it should be long enough to cover several cycles or seasons to allow researchers to specify them. In the literature (Section 2.1.2, Chapter 2), it was commented that there are a few types of property cycles. These are so called 'short cycles' of 4 to 5 years of duration, and 'major cycles' of 7 to 9 years of length. Following this classification and Yaffee and McGee's (2000) recommendation that series should cover several cycles, it can therefore be suggested that selected time-series should contain more than 20 data-points (years) in order to successfully capture the cyclical nature of the dependent variable.

What is more, long time-series are necessary for mathematical reasons. Yaffee and McGee (2000) and Brooks and Tsolacos (2010) also noted the importance of statistical methods being used in determining the sample size. For univariate time-series models, authors, including Holden *et al.* (1991), McGough and Tsolacos (1995b) and Tse (1997) argued the need for at least 50 sample observations to produce a well parameterised ARIMA model. Although, Weiss and Andersen (1984) suggested that 30 observation are enough. The property studies, which were using univariate time-series modelling techniques (e.g. McGough and Tsolacos, 1995; 2001; Wilson *et al.*, 2000; Brooks and Tsolacos, 2001; Crawford and Fratanoni, 2003; Stevenson, 2007) employed more than 50 observations. However, in cases where such a large sample was not available (e.g.

Stevenson and McGarth, 2003; Karakozova, 2004), the univariate models were still able to capture the dynamics of the dependent variable.

In the case of regression model building, the length of time-series being used varied significantly. Hekman (1985) used only 5 observations. Tsolacos (1995) estimated his structural equation using 69 data points. D'Arcy's *et al.* (1999) study covered 28 years' data. Brooks and Tsolacos' (2000) sample period included 88 data points. White *et al.* (2000) used 29 observations. Stevenson and McGarth (2003) employed 39 observations. Mouzakis and Richards' (2004) data was of 22 observations. Qun and Hua (2009) used 10 observations only. As it is seen, various authors used different data sets of differing lengths, with some of the studies employing ten and less data points. However, Mouzakis and Richards' (2004) study estimated that at least 20 observations are required to build a reliable regression based model.

The following section discusses difficulties related to the UK property data and its acquisition. As it shows, although the UK and especially London commercial property market data is considered as probably the best documented in Europe, it is however not without criticism.

4.2 The UK property data

The UK and especially London commercial property market data is considered as probably the best documented in Europe (Barras, 1984; Ball and Tsolacos, 2002; McGough and Tsolacos, 2002; Lizieri, 2009a; Devaney, 2010). As McGough and Tsolacos (2002, p.35) observed, 'in some senses, researchers seem spoilt for choice'. According to the commentators, the UK property data goes back for several decades. It is available at national and local levels, as well as in various frequencies. All that makes it possible to produce detailed and robust property market analytics.

However, as the publications on the subject suggest, UK data is not without criticism. Crosby (1988a; 1988b) reflected on the issue by identifying difficulties associated with the quality and quantity of the UK data. According to Crosby (1988a), the non-availability of data is partly related to the barriers within the public domain. As he observed, institutions such as the Valuation Office (now Valuation Office Agency) and Inland Revenue (now HM Revenue and Customs) deposit large amounts of the property data which could be analysed and successfully used for research. However, there is limited access to it. The other difficulty which Crosby identified is associated with substantial costs involved in collecting property data. What is more, data which could be obtained from private sources is often restricted by confidentiality and secrecy. Therefore, as Crosby (1988b) observed, the likelihood in obtaining the details off all property market transactions is very unlikely.

More recently, Ball and Grilli (1997) identified that commercial property market data is too 'soft' for robust statistical analysis. What the researchers meant was that 'the aggregate data on commercial property output are relatively smooth compared to housing and to many other goods' (ibid., p.282).

Similarly, Ball and Tsolacos (2002) stressed the issues with the way UK construction data is drawn up. As the researchers identified, the length of

project implementation, index deflation, and missing information do affect the data. The authors therefore commented that forecasting errors may occur if too much reliance is placed on the data. Accordingly, in agreement with Crosby (1988a), they called for the Government to play a greater role in producing more accurate data.

RICS (1999) also addressed this issue. As the research identified, historic data is often highly aggregate and inaccessible. What is more, it is difficult to assess its reliability whereas there are almost no other independent sources of information against which the data could be cross-referenced.

Gruneberg and Hughes' (2005) assessment of the consistency between different construction data sources identified lack of uniformity amongst data sources. The researchers used correlation analysis as a measure of consistency. As their findings suggested, correlation coefficient of only two series was greater than 0.5. Accordingly, Gruneberg and Hughes hypothesised that this inconsistency arises from the way data is collected, what it contains, and what it measures. It therefore led them to conclude that 'it is not practically possible to develop a consistent predictive model of construction output using construction statistics gathered at different stages in the development process' (ibid., p.83). It was therefore suggested that historic data should be treated with caution.

In their modelling study, McGough and Tsolacos (2002) suggested that property related data is specific and thus hard to obtain. The non-availability of and difficulty to obtain property data was also commented on by Brown and Matysiak (1995), Wyatt (1996), Dunse *et al.* (1998), Knight *et al.* (1998), Ge and Harfield (2007) and Francesca *et al.* (2010). An early observations of Brown and Matysiak's (1995) suggested that historical property data is relatively short because there was no need for it. As the authors indicated, property was considered as a long term investment with minimum management required. What is more, it was anticipated that its financial value will always be growing. Therefore, there has been no perceived need to keep long-term series. According to Wyatt (1996, p.67)

reliable property data is not available 'because of legislative restrictions on data release to the public, confidentiality constraints and conservative attitudes'. Similar suggestions were presented by Dunse *et al.* (1998), who commented that historical property data is somewhere of 30 years of length and access to the information is restricted by the confidentiality clauses. What is more, private-sector organisations are usually reluctant to openly publish the information they collect. As Knight *et al.* (1998) observed, although virtually all areas of empirical research faces data availability problems, real estate research encounters this issue in particular. Francesca *et al.* (2010) discussed the issue of costs involved in obtaining primary property data from specialised organisations.

The current study encountered the same issues as noted in the literature. Estimates for floor-space, take-up, and vacancy rate are collected by major property consultancies (e.g. CBRE, JLL, DTZ) and published in their reports (e.g. McCauley, 2009; JLL, 2010a; Clarke, 2011). However, this data is somewhat fragmented and are not available over a long period of time. In situations when data is available, a special subscription is required. Datastream International (2012), which is a global financial and macro-economic data-base, Building Cost Information Service (BCIS, 2012), which provides cost information for the built environment, Global Financial Data (2012), which is a provider of historical financial data, and organisations such as Cambridge Econometrics (2012), Lombard Street Research (2012), Oxford Economics (2012), Capital Economics (2012) as well as specialised property information providers including EGi (2012), Experian Goad (2012), and Landmark Information Group (2010), all charge for access to their data-sets and reports.

Certainly, the UK property market data is rich and diverse. It is considered as being particularly well documented with some of the indicators going back for several decades. However, it is not without criticism. Difficulties with data, which Crosby indicated in 1988, still do exist in 2014.

The next section of this Chapter presents the principle of Chain-linking. Chain-linking has been commented as being a statistically robust method for time-series combination especially in situations when available data-sets are of short duration.

4.3 Annual Chain-Linking

Availability of a long-term series, as noted above, is an important issue for commercial property market modelling and analysis. In situations when time-series are of limited length, a possible solution is a combination of several data-sets. The difficulty is, however, on deciding how the various series should be combined.

The simplest solution came from Liesner (1989). In her study, Liesner (*ibid.*, p.271) 'used simple average estimates as the central point to construct national accounts'. A more robust approach was employed by Gruneberg and Hughes (2005) and Vivian (2007), who used correlation analysis to detect which of the series had greater statistical relationship. For Vivian correlation analysis helped to check validity of the data and select time-series which were subsequently combined to produce longer-term indicators.

As theoretical and empirical findings suggest, however, the technique, known as 'Chain-Linking' is considered as a better series combination approach (OECD, 2007). According to the OECD (*ibid.*, p.97), an advantage of chain linking is that it is 'joining together two indices that overlap in one period by rescaling one of them to make its value equal to that of the other in the same period, thus combining them into a single time-series'. This time-series combination technique has been used by major organisations, including the Scottish Government (2007), ONS (2011) and the World Bank (2011b). McKenzie (2006) indicated that in year 2006, 14 out of 29 OECD countries used some sort of linking methodology for index combination.

Following Tuke (2002) and Robjohns (2006), there are two major principles of a chain-linking methodology: fixed base year chain-linking and annual chain-linking. Fixed base year chain-linking uses a set of weights which are applied on each component to produce an aggregate measure. This method revises weights every 5 years. However, in a changing economy, it may not be adequate, as this approach does not

reflect the current state of the market. Therefore, annual chain-linking is recommended to measure aggregate figures more frequently. As the name suggests, rebasing is performed every year.

The annual chain-linking process is expressed in the equation below:

$$CLV_t = BYA_{t+1}/1 + \left(\frac{BYR_{t+1} - BYR_t}{BYR_t} \right) \quad (40)$$

Where CLV_t is chain-linked value, BYA_t is actual base year value, BYR_t is base year which is to be rebased value, and t is time period. The Equation 40 is used when the most recent time-series is established as being the base with, an older data-set being that which is to be rebased.

If, however, the base series is that from the past and most recent series is to be rebased, then formula is as follows:

$$CLV_t = BYR_{t-1} * \left(1 + \frac{BYA_t - BYA_{t-1}}{BYA_{t-1}} \right) \quad (41)$$

Equation 41 allows the chain-linking of a time-series based on older data-set, which is then extended by rebasing the newer time-series.

The following section presents dependent and explanatory variables which were used for modelling. The section discusses rationale behind these variables and their significance to property market. It also presents key properties of selected series.

4.4 Method of selecting variables

4.4.1 The dependent variable

The literature has shown (Section 2.2) that the use of the dependent variable within the field of commercial property market modelling and forecasting varied. McGough and Tsolacos (1995b) examined retail, office and industrial rents. Tsolacos (1995) assess retail rents determination factors. D'Arcy *et al.* (1999) investigated dynamics of Dublin office rental market. Karakozova (2004) appreciated office returns in Helsinki. Brooks and Tsolacos (2010) developed an econometric model to assess future value of office yields.

The research, however, employs a rental series as the dependent variable. This comes from Barras (1984), Scott (1996), Ball *et al.* (1998), and Baum and Crosby (2008) who argued that rent is of particular importance for investors and analysts. Following Barras (1984), rent level determines the profitability for developers and investors which as a result affects the level of supply of new developments. Ball *et al.* (1998) documents that in the user market, rent is a payment an organisation makes in order to use commercial property. In the capital market, rent is used to estimate the value of the property. Subsequently, rent plays a very important role in bringing four inter-related property markets (user, financial, development and land market) into simultaneous equilibrium. In mathematical terms, rent constitutes actually income stream that an asset generates. What is more, it is used to derive value of the commercial property. Here the value is estimated by dividing rent, which is a rental income received from letting an asset to occupiers, from capitalisation rate.

Accordingly, Hendershott *et al.* (2002a, p.165) suggested that rent, the price of space, is 'the most important variable in property economics'. As

such, rent determination has been an object of empirical studies over the last few decades.

Following on from this, the current research uses IPD All Property Rental Value Growth Index for the UK as the dependent variable (IPD, 2011). Certainly, IPD is not the only UK property index provider. Property consultancies including JLL (2010) and CBRE (2011) also produce UK commercial property benchmarks. Nevertheless, IPD indices are considered as being reliable property market benchmarks in the UK. They are well regarded within the UK property investment community, as well as being regularly used by property researchers (Baum, 2001; Ball, 2003; McAllister et al., 2005a; 2005b).

IPD provides real estate benchmarking and portfolio analysis services internationally. According to its recent press release (IPD, 2014), IPD's database incorporated more than 1,500 funds containing nearly 77,000 assets, with a total capital value of over USD 1.9 trillion. Each year, IPD produces more than 120 indexes and around 600 benchmarks for client portfolios, making it one of the best property information providers. In terms of UK Annual Property Rental Index, the benchmark tracks performance of 21,175 property investments, with a total capital value of over £152.7 billion as at December 2013. The market coverage is estimated to be around 60% - 70% with results dating back to 1980 (IPD, 2011), which is greater than JLL, CBRE or any other competing dataset in the UK.

Regarding time-series frequency, all data is annual. There may be a suggestion to use quarterly or monthly figures. Certainly, in both cases, series will be longer. Rather than having only 47 annual data point over the 1963-2010 period, quarterly figures would give 188 data-points and monthly figures would provide with 564 data-points. This would therefore be an improvement for modelling purposes. However, it should be remembered that real estate is a long-term asset (Ball et al., 1998; Shiller, 2014). An annual data is more important whereas an impact of exogenous

factors such as business cycle can only be detected at annual intervals (Baum, 2009). Therefore, yearly data represent market better than the higher frequency series. What is more, Denton (1971) commented on difficulty in adjusting monthly or quarterly series to annual totals. More recently, EUROSTAT (n.d.) observed issues related to quarterly national accounts. In addition to that, series dating back several decades are available only in annual figures. As such, series in annual numbers are selected for the current research.

The original IPD series is available from 1976, which up to year 2010 gives 35 data-points only (IPD, 2011). Section 4.1. considered the issue of the minimum number of observations required to produce time-series and regression based models. It was suggested, that for an ARIMA model at least 50 sample observations are needed. For the regression specification, it should be more than 20. As such, for the purpose of this study, the IPD index is extended by chain-linking it with Scott's (1996) rental series. Scott's rental series has been chosen following study of the RICS (1999) and statistical estimates. RICS (1999) reported that IPD's rent series can be extended by combining it with Scott's (1996) dataset. RICS (ibid.) study successfully combined two series which extended the dependent variable for several decades. The subsequent visual and statistical analysis suggests high compatibility between the two time-series (Figure 4.1; Figure 4.2). The correlation coefficient over the period 1976-1993, when the two series overlap, is 0.999 (it is 0.997 for 1st.dif. series) which indicates almost perfect positive correlation. It therefore suggests that both series can be successfully linked together.

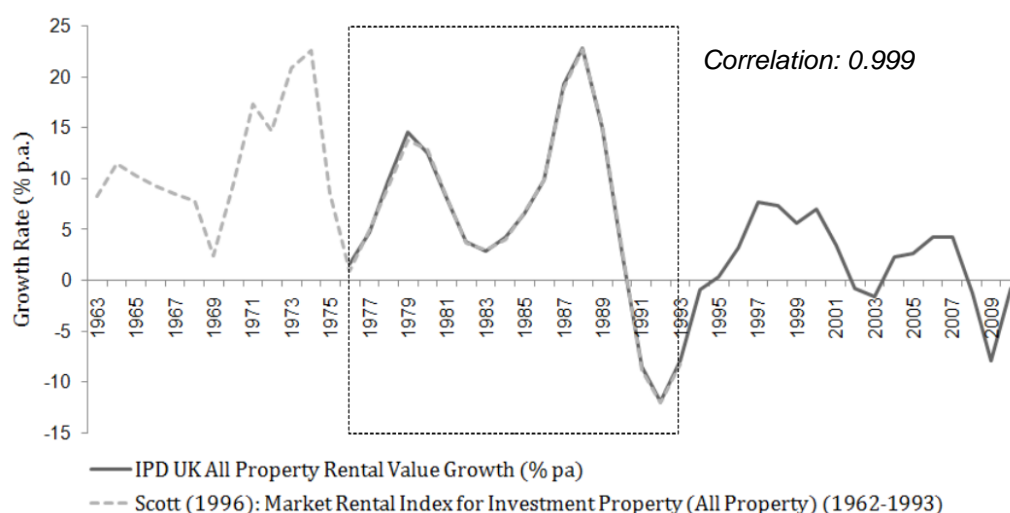


Figure 4.1 Chain-linked UK All Property Rent Index
Source: Scott (1996); IPD (2011)

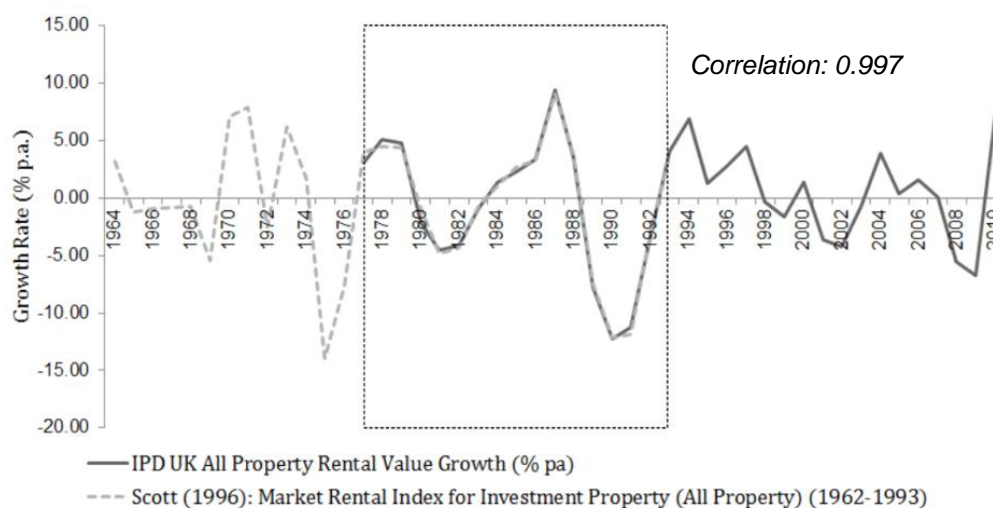


Figure 4.2 Chain-linked UK All Property Rent Index (1st.dif)
Source: Scott (1996); IPD (2011)

The subsequent combination of both IPD and Scott's series extends the rental series for an extra 13 years. As a result it gives 48 data points which is considered to be substantial for both univariate and regression time-series modelling. The study therefore continues with the extended time-series with year 1963 being a starting point. Accordingly, data on all explanatory variables is collected for the same time period (see Section 4.4.2, Chapter 4). What is more, all explanatory variables are acquired

following Arthur's (2003) recommendations, i.e. time-series are regular, representative, homogenous (comparable), continuous (unchanging description), and of the same length and frequency.

Following on from this, the time-series are divided into initialisation and hold-out periods. As it was noted in Section 2.2.2., all models must be parameterised and tested on initialisation set and forecasts made on holdout set. The issue here, however, is that the literature does not suggest the length of initialisation and hold-out periods. Various authors within property forecasting used different ex-ante and ex-post periods. Chaplin (1998) tested his models by producing one step ahead predictions for five years. In a subsequent paper, Chaplin (1999) estimated model fit and produced one-step ahead forecasts for ten years (from 1985 to 1994). D'Arcy *et al.* (1999) used time-series over the 1970-1997 period. Then, forecasting adequacy of the estimated rent model was assessed by producing sample forecast for 1996 and 1997. Hendershott *et al.* (1999) in their empirical study employed a series for the period 1977-1996 with model being dynamically simulated yearly from 1986 to 1996. Matysiak and Tsolacos (2003) employed a monthly series for the December 1986 – April 2001 period and produced out-of-sample forecasts for two three-month time horizons, i.e. February 2001 - April 2001 and February 2000 - April 2000. Stevenson and McGarth (2003) used bi-annual data from May 1977 to May 1996 for model construction and the following three years for out-of-sample performance assessment. Similarly, Orr and Jones (2003) employed a bi-annual series for the 1979-2000 period. Accordingly, the authors produced four 1-step ahead forecasts for 1998 (half 1 and half 2) and 1999 (half 1 and half 2). Mouzakis and Richards's (2004) data was available from 1980 to 2001 annually with two final years being the test years. Tsolacos (2006) generated ex-ante forecasts for one- and two-year horizons on a rolling basis over the period from 1999 to 2004.

As can be seen from the discussion above, there is no general agreement as to how long the holdout period should be. The findings suggest that it can range from two (as in Mouzakis and Richards, 2004) to ten periods

(as in Chaplin, 1999). In this research it was therefore decided to divide the data set into initialisation period from 1964 to 2000 and holdout period from 2001 to 2010. The ten year ex-post forecasting accuracy period will be sufficient to assess the forecasting performance of each model, as well as to examine the existence of two short 4-5 years property cycles driven by the classical business cycle (Barras, 1994; RICS, 1994; Ball *et al.*, 1998) and one longer 9-10 years major property cycle (Barras, 1994). It will also allow assessing the forecasting accuracy of each model for short- and long-run horizons.

An examination of the general trends in commercial rental values over the sample period produces observations, which corroborate those of Fraser (1984), Scott (1996), RICS (1999; 1994) and Barras (2009). As it is seen from Figure 4.3, over the 1963-2010 period, there were five major corrections in the series, i.e. early 1970s, mid-1980s, early 1990s, early 2000s and that of 2008. It also suggests high volatility of the rental index over 1974-1977, 1988-1992 and 2008-2010 periods in particular.

The subsequent analysis of HP cycle of the combined rental property index (Figure 4.4) suggests that the average period of UK rental cycle is 9 years. The average period between turning points is 4.5 years. It is also apparent that cycles are getting shorter and more volatile over time.

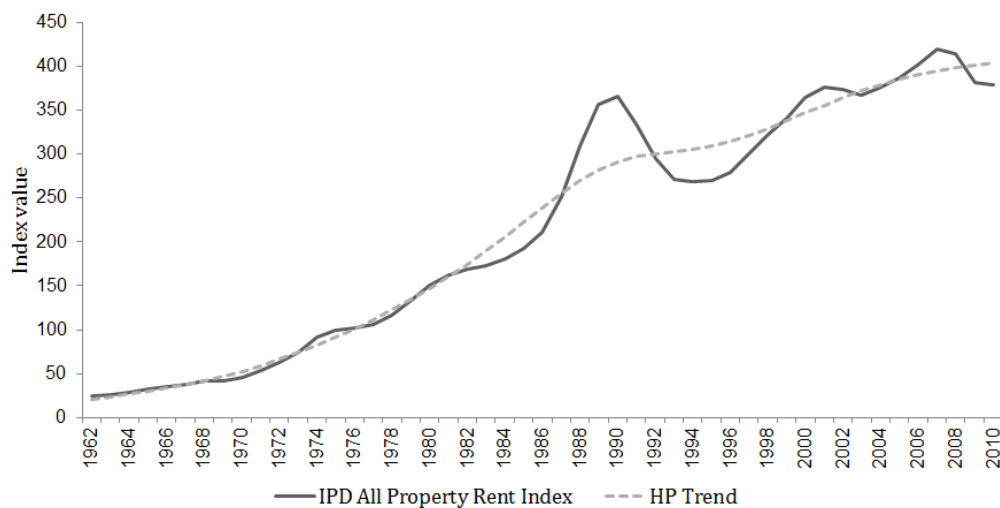


Figure 4.3 Chain-linked UK All Property Rent Index and HP Trend

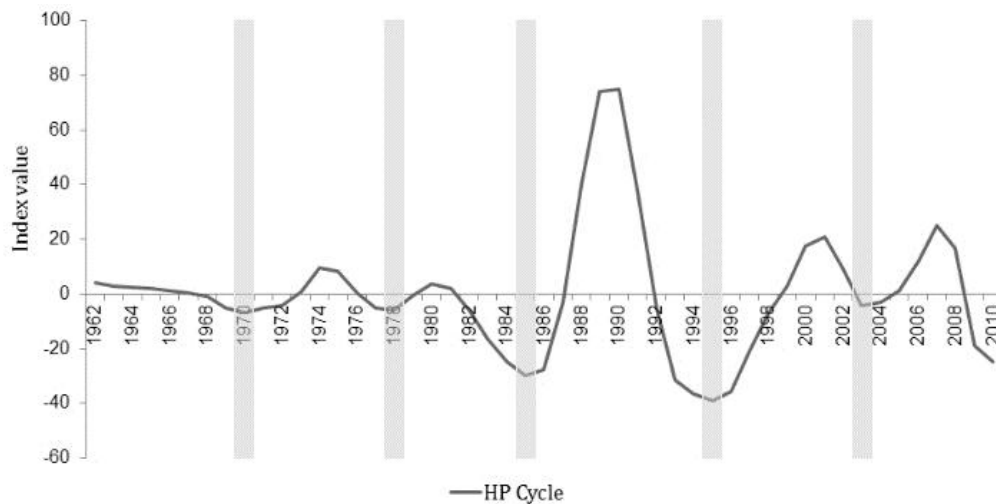


Figure 4.4 The HP Cycle for Chain-linked UK All Property Rent Index

4.4.2 Explanatory variables

The examination of the literature on the subject³ enabled the identification of thirty-six variables which were used by various property researchers to model commercial property rents. However, not all series identified were available for the 1963-2010 research period. Business Orders, Consumer Confidence, Floor-space, Index of Services, Retail Sales, Take-up, Business Turnover, Risk Premium and Vacancy Rate were variables for which data was not available for such a long period of time. In most of the cases, data on these variables was not collected before late 1980s/early 1990s. Other variables, which were used within studies on commercial property market rent determination, were subject specific. Table 4.1 provides details on all explanatory variables, their availability, original name and code where applicable, as well as sources of information where they were obtained.

³ Publications include Hekman (1985), Frew and Jud (1988), Glascock *et al.* (1993), RICS (1994), Tsolacos (1995; 2006), Hendershott (1996), Wheaton *et al.* (1997), Chaplin (1998; 1999; 2000), Hendershott *et al.* (1996; 1999; 2002a; 2002b; 2008), D'Arcy *et al.* (1999), Mueller (1999), Robertson and Jones (1999), Wheaton (1999), Brooks and Tsolacos (2000), White *et al.* (2000), McDonald (2002), Matysiak and Tsolacos (2003), Orr and Jones (2003), Stevenson and Mcgarth (2003), Mouzakis and Richards (2004), and Qun and Hua (2009).

The data on explanatory variables was obtained from various sources. The author's intention was to collect as many explanatory variables as possible so that so called 'omitted variable bias' could be controlled for. However, a number of important limitations were in play during this process. The most notable one was access to data. As noted in Section 4.2., the UK commercial property market is well documented; series go back for several decades. Unfortunately, it is not without criticism, with the inaccessibility of property specific series being the key limitation. As such, the data for this research project was compiled from web-based data sources such as ONS, World Bank, OECD, as well as from print-copies of various statistical tables available in the archives of the National Library of Scotland.

Analysis of the data-sets of seventeen organisations and thirteen publications made it possible to collect statistical data on only twenty-seven of these variables. Organisations whose datasets were used include the Bank of England (2011), Corporation of London (2011), the UK Debt Management Office (2011), the Department for Communities and Local Government (2011), Department for Transport (2011), Global Financial Data (GFD) (2012), HM Revenue & Customs (HMRC) (2011), Ingleby Trice (2011), Investment Property Databank (IPD) (2011), London Stock Exchange (LSE) (2011), Nationwide Building Society (2011), the NHS Information Centre (IS.NHS) (2011), the Office for National Statistics (ONS) (2010), the Office of the Deputy Prime Minister (ODPM) (2006), the Organisation for Economic Co-operation and Development (OECD) (2011), the University of Groningen (Maddison-Project) (2008), and the World Bank (2011a).

Publications which were used to support, cross-reference and extend existing time-series include Feinstein (1972), London & Cambridge Economic Services (LCES) (1973), Building Societies Association (1982), Liesner (1989), Mitchell (1992), Council of Mortgage Lenders (1995), Scott (1996), Hicks and Allen (1999), Twigger (1999), Bond *et al.* (2001), O'Donoghue *et al.* (2004), and Holmans (2005).

| Variables | Availability | Name and code | Source |
|--------------------------|--------------|---|--|
| Bank Rate | 1963-2010 | Annual average rate of discount, 3 month Treasury bills, Sterling (IUAAAJNB) | Bank of England (2011) / Liesner (1989) |
| Business Output | 1963-2010 | Financial intermediation and real estate, renting and business activities (EWAY) | ONS (2010) |
| Business Orders | 1998-2010 | Turnover and Orders in Production and Services Industries - TOPSI: Manufacturing and Services Turnover (JT) | ONS (2010) |
| Car Registrations | 1963-2010 | Motor vehicles registered for the first time by tax class | Department for Transport (2011) |
| Construction Orders | 1964-2010 | Value of construction new orders by contractors (£ mill) | ONS (2010) |
| Construction Completions | 1963-2010 | Volume of construction output by contractors | ONS (2010) |
| | 1963-2010 | House building completions | Council of Mortgage Lenders (1995) / the Department for Communities and Local Government (2011) / Building Societies Association (1982) |
| Construction Cost | 1963-2009 | Price of construction output | Holmans (2005) / ONS (2010) |
| Construction Starts | 1963-2009 | Building starts | Council of Mortgage Lenders (1995) / the Department for Communities and Local Government (2011) / Hicks and Allen (1999) / Building Societies Association (1982) |
| Consumer Confidence | 1974-2010 | Consumer survey | OECD (2011) |
| Consumer Expenditure | 1963-2010 | Household final consumption expenditure (national concept) (ABPB) | ONS (2010) |
| Depreciation Rate | 1963-2010 | Total real estate, renting & business activities (GRRD) | ONS (2010) |
| Disposable Income | 1963-2010 | Real household disposable income per head | ONS (2010) / IS.NHS (2011) |
| Employment | 1963-2010 | Employment (services) (JWT8) | Liesner (1989) / ONS (2010) / Feinstein (1972) |
| Floor-Space | 1986-2010 | Office (use classes order B1) stock estimates | Corporation of London (2011) / Ingleby Trice (2011) / ODPM (2006) |
| Foreign Funds | 1964-2010 | Foreign direct investment (net inflows) (BX.KLT.DINV.CD.WD) | World Bank (2011a) / ONS (2010) |
| FTSE All Share Index | 1963-2010 | FTSE All-Share Index value | LSE (2011) / Global Financial Data (2012) / Bond <i>et al.</i> (2001) / London & Cambridge Economic Services (1973) |
| GDP | 1963-2010 | Gross Domestic Product (ABMI) | ONS (2010) / Maddison-Project (2008) / Liesner (1989) / Hicks and Allen (1999) |
| ONS Leading Indicator | 1996-2010 | Index of services (total) (D8ZW) | ONS (2010) |
| | 1963-2010 | Index of production (total) (CKYW) | |

| Variables | Availability | Name and code | Source |
|---------------------------------|--------------|--|--|
| Inflation | 1963-2010 | The value of the pound (CZBH) | ONS (2010) / Twigger (1999) / O'Donoghue <i>et al.</i> (2004) / Hicks and Allen (1999) |
| Lagged Dependent Variable | 1964-2010 | IPD All Property Rental Value growth series | IPD (2011) / Scott (1996) |
| Money Supply | 1963-2010 | Money stock (M4 - end period) (ATTD) | ONS (2010) / Bank of England (2011) / Mitchell (1992) |
| | 1969-2010 | Money stock (M0 - end period) (ATTC) | |
| Number of Property Transactions | 1963-2010 | Number of property transactions -England and Wales (FTAP) | ONS (2010) / HM Revenue & Customs (2011) |
| Profitability | 1965-2010 | Rates of return of service sector (BGYK) | ONS (2010) / Liesner (1989) / Feinstein (1972) |
| Property Value | 1963-2010 | UK House Price Index | Nationwide (2011) |
| Retail Sales | 1988-2010 | Retail sales (all business index) (J3UU) | ONS (2010) |
| Risk Premium | 1967-2009 | Risk premium on lending (prime rate minus treasury bill rate, %) | World Bank (2011a) |
| Take-Up | 1997-2010 | Take-up floor-space in the city of London | ONS (2010) / Corporation of London (2011) |
| Turnover | 2000-2010 | Turnover and orders in production and services Industries - rental & leasing services (JT3M) | ONS (2010) |
| Unemployment | 1963-2010 | Unemployment (LF2Q) | ONS (2010) / Liesner (1989) / Hicks and Allen (1999) |
| Vacancy Rate | 2001-2010 | Vacancy rate | Corporation of London (2011) / ONS (2010) |
| Yields on Government Securities | 1963-2010 | 2.5% Consolidated Stock Average Yield | UK Debt Management Office (2011) |
| | 1963-2010 | Par yield on long-dated British Government Securities (20 years - percent per annum) (AJLX) | ONS (2010) / Bank of England (2011) |
| Capital Formation | 1963-2010 | Gross fixed capital formation: business investment (NPEK) | ONS (2010) / World Bank (2011a) |
| Job Vacancies | 1963-2010 | UK Employee Jobs - total (thousands) (BCAJ) | ONS (2010) |
| Land Value | 1963-2010 | Index of land prices | Holmans (1995) / the Department for Communities and Local Government (2011) |
| Net Investment | 1963-2010 | Investment by insurance companies, pension funds and trusts: UK buildings, property, land & new construction work (RLKD) | ONS (2010) |
| Total Returns | 1963-2010 | IPD Total Returns | IPD (2011) / Scott (1996) |

Table 4.1 Time-series employed to model commercial property rents

Bank Rate

The use of interest rates to model the commercial property market was argued by RICS (1994), Wheaton *et al.* (1997), Chaplin (1998), Orr and Jones (2003), Stevenson and McGarth (2003), and Qun and Hua (2009). According to researchers, interest rates do affect the commercial property, with higher interest rates depressing rental levels and *vice-versa*.

The 'Annual Average Rate of Discount, 3 Month Treasury Bills, Sterling' (IUAAAJNB) is selected for the research. The series was obtained from the Bank of England database. Whereas Bank of England's series is available only from 1976, it was extended by chain-linking with Liesner's (1989) 'Treasury bills ave.3months tender rate (%)' series. The latter is available from 1900 to 1988. The correlation analysis over the 1976-1988 period when both series overlap indicate almost perfect positive correlation with correlation coefficient being 0.999. From the statistical and visual analysis (Figure 4.5) it is seen that both datasets are almost identical. Accordingly, by chain-linking both series, the original Bank of England's series were extended for the period needed (Figure 4.6).

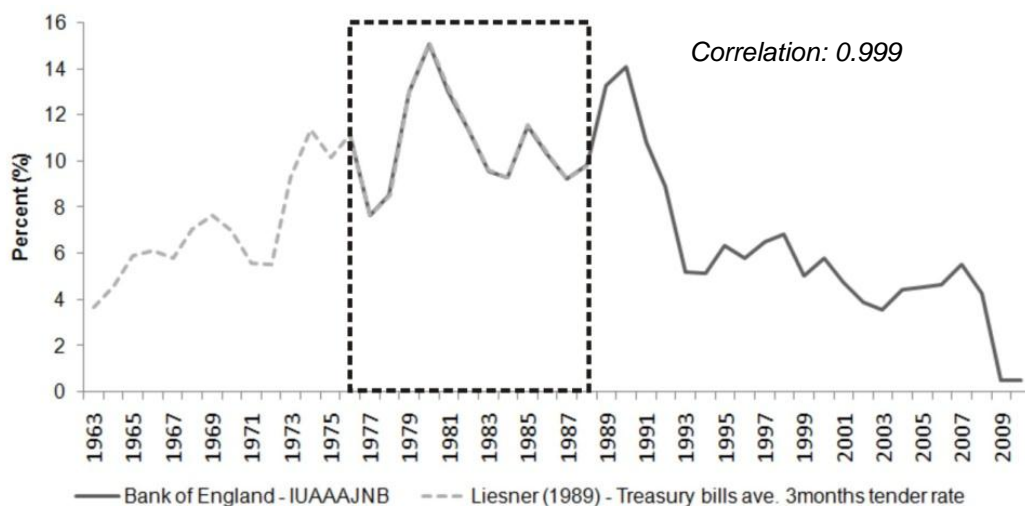


Figure 4.5 Liesner's and BOE's Annual Average Rate of Discount
Source: Liesner(1989); Bank of England (2011)

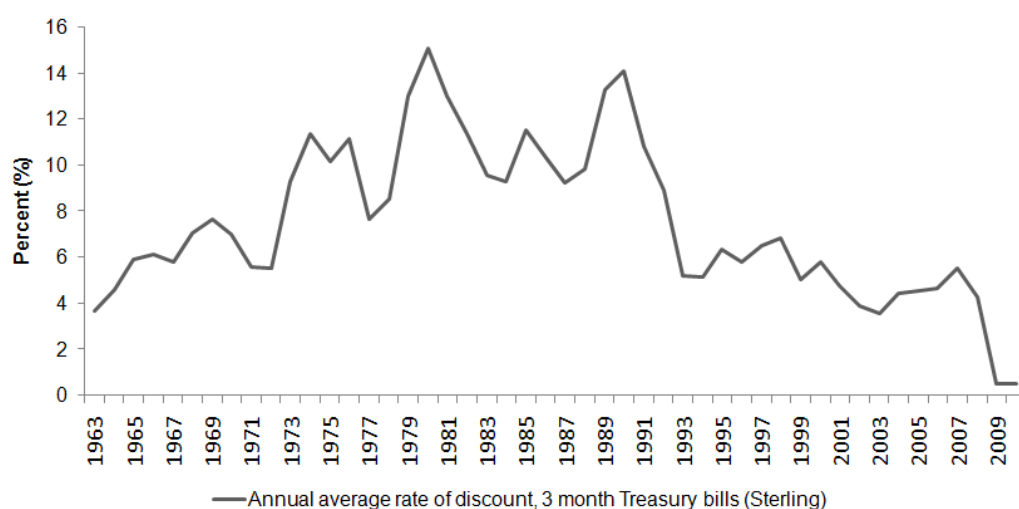


Figure 4.6 Chain-linked Annual Average Rate of Discount

Business Output

The use of business output as an explanatory variable was argued by Chaplin (1999). In his research Chaplin first referred to McGough and Tsolacos (1994, cited in Chaplin, 1999) paper where researchers employed change in Real Output of Business Services and change in Real Output of Financial and Business Services for their Vector Autoregressive (VAR) framework. McGough and Tsolacos' (ibid.) statistical modelling results suggested Business Output to be of particular importance to model the property market. Subsequently, Chaplin (ibid.) selected Output of the Financial and Business Service Sector as an explanatory variable to model the UK real office rents.

The EWAY series, which is one of GVA's Detailed Output Indices, is selected for the research. The full specification of this data-set is ESA95 Output Index: SIC92 Section J & K (excluding Div 79), which contains data on Financial Intermediation and Real Estate, Renting and Business Activities. The series is available from 1948 in yearly and quarterly figures from the ONS.

Car Registrations

The use of this data-set comes from Matysiak and Tsolacos (2003). The authors employed Car Registrations as a real economy variable. They estimated that Car Registrations is a leading indicator for the commercial property market.

The transport statistics series, i.e. 'Motor Vehicles Registered For the First Time' (thousands), is obtained from the Department for Transport (2011). The series is available from 1954 in annual figures.

Construction Orders

The use of Construction Orders as an explanatory variable was argued by Wheaton *et al.* (1997) and Matysiak and Tsolacos (2003). For the current research, Value of Construction New Orders by Contractors (by sector) (£ Million) is obtained from the ONS. The selected series is for 'Private Commercial', which excludes infrastructure and housing. The series is available from 1964 annually.

Construction Completions

The use of construction completions as an explanatory variable was argued within various studies. D'Arcy *et al.* (1999) employed New Office Completions in their econometric analysis of the office rental cycle in the Dublin area. Wheaton (1999) argued importance of Completion Rate in his analytical paper. Orr and Jones (2003) used Construction Completions to analyse and predict urban office rents. Hendershott *et al.* (2008) employed Completions for Office Space to model London office market. Qun and Hua (2009) also selected Office New Completions as a determinant of the office rents in China.

Although Construction Completions as an explanatory variable was used by numerous researchers, long-span historic data for this particular variable is not available. D'Arcy's *et al.* (1999) series went back to 1970. Wheaton's (1999) data was from 1968. Orr and Jones' (2003) series was

from 1979. Hendershott's *et al.* (2008) data-set was only from 1987. Qun and Hua (2009) use data from 1998 only. It was therefore decided to use 'Volume of construction output in Great Britain' (index numbers) as a proxy for Construction Completions. This variable is available from the ONS starting from 1955 in annual and quarterly figures. The series is for 'other new work' which excludes infrastructure works and new house building. It is also for 'private commercial' which eliminates public and private industrial elements.

An alternative variable selected for the research is 'House building completions'. Certainly this particular series is for residential property and may not be applicable for the analysis of the commercial real estate market dynamics. Nevertheless, it is decided to employ this data-set as a representative variable of the UK construction activity. The 'House Building: Permanent Dwellings Completed' (nominal numbers) series is available from the Department for Communities and Local Government from 1949 annually. This data-set was also cross-referenced with Council of Mortgage Lenders' (1995) 'Building Completions for Great Britain' series. The correlation coefficient over 1955-1994 period when both series overlap is 0.993, which indicates that both series are highly compatible.

Construction Cost

The importance of Construction Costs for commercial property rents modelling was empirically proven by Wheaton *et al.* (1997) and Orr and Jones (2003). However, as with Construction Completions, Construction Costs long time-series is not publically available. One of the major construction costs data providers in the UK is Building Cost Information Service (BCIS) and the ONS. The ONS' data is available from 1997 only. In the case of BCIS, a special subscription is required.

An alternative to Construction Costs series is Holmans' (2005) Price Index of Construction Output. The researcher compiled long series for the general construction price level for 1861-2001 period. However, this

Holmans' series is for all construction only. It therefore can serve only as a proxy for Construction Costs series.

The visual and correlation analysis of Holmans' (2005) and ONS' series indicate close relationship between two series, despite the difference in their levels (Figure 4.7). As it is seen, both series follow the same trajectory. Correlation coefficient over the 1997-2001 period, when two series overlap, is 0.995. It thus suggests that both series can be successfully chain-linked together in order to produce a long-term Construction Costs Index. Figure 4.8 shows final chain-linked Construction Costs Index series.

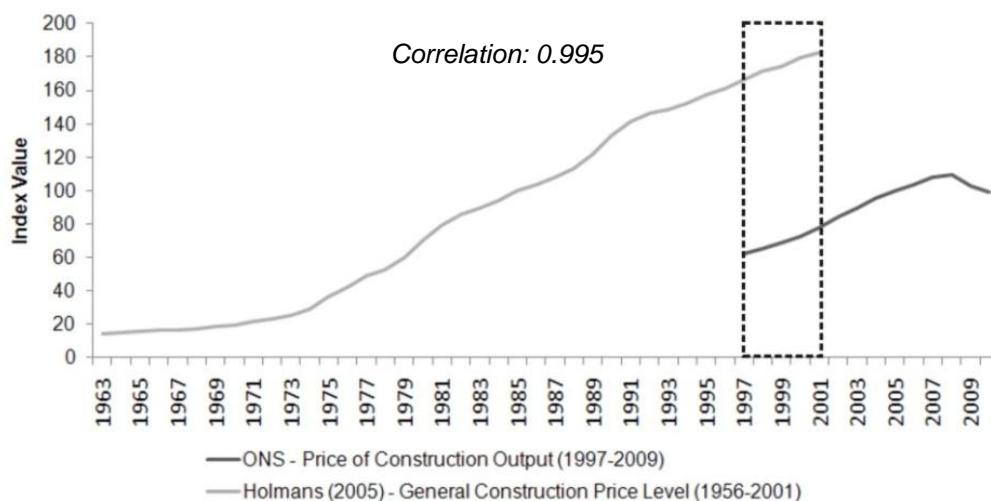


Figure 4.7 ONS' and Holmans' (2005) Construction Costs series
Source: Holmans (2005); ONS (2010)

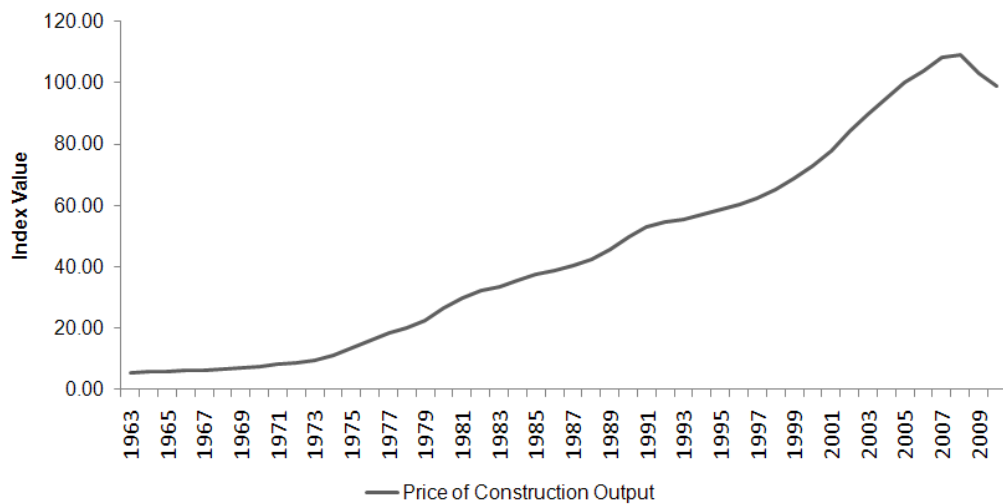


Figure 4.8 Chain-linked Construction Costs series
Source: Holmans (2005); ONS (2010)

Construction Starts

The importance of Construction Starts was noted by the RICS (1994) and Hendershott *et al.* (2008). However, as with Construction Costs and Completions, the data for this series is not available over the long period of time. The alternative here is to use chain-linked House-Building Starts series those of Council of Mortgage Lenders (1995) and the Department for Communities and Local Government as a proxy, whereas direct measure of commercial property Construction Starts is publically not available. The Council of Mortgage Lenders' (1995) data for House-Building Starts (Total - Private and Public) (Nominal Numbers) is for 1955-1994 period. The Department for Communities and Local Government's data is for 1990-2010 period. Visual and correlation analysis indicate that both series are highly compatible. Correlation coefficient is 0.999 which suggests almost perfect positive correlation. Figure 4.9 shows the primary series and a period where both series overlap. Figure 4.10 shows chain-linked Building Starts series for 1963-2010 period.

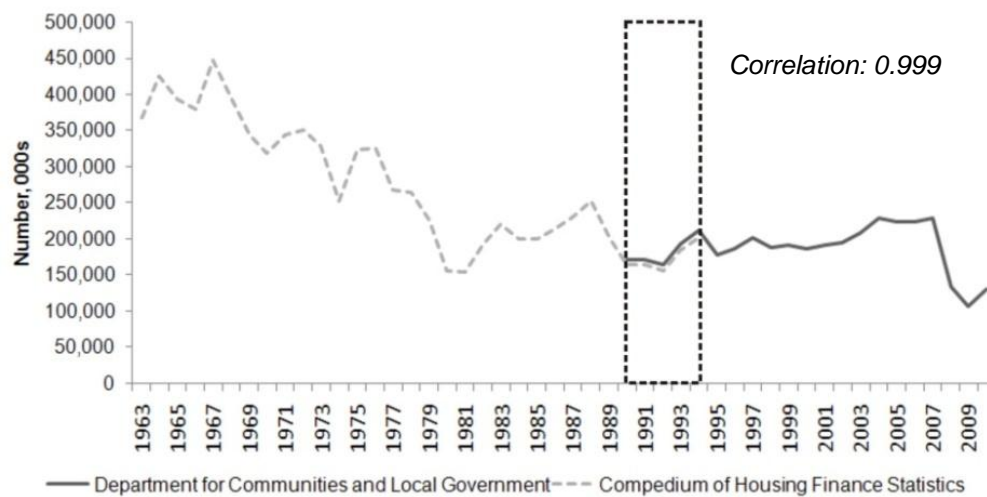


Figure 4.9 The CML's and DCLG's House Building Starts series

Source: The Council of Mortgage Lenders(1995); the Department for Communities and Local Government (2011)

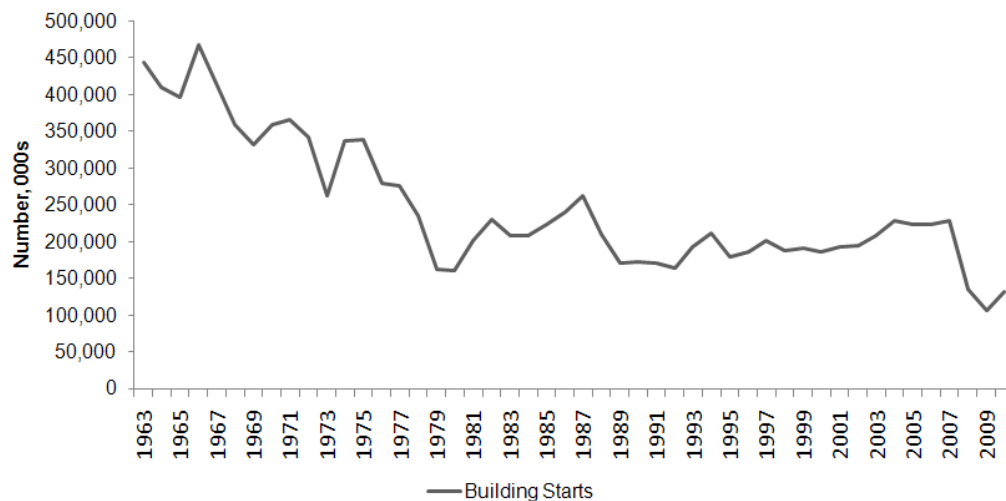


Figure 4.10 Chain-linked House Building Starts series

Source: The Council of Mortgage Lenders (1995); the Department for Communities and Local Government (2011)

Consumer Expenditure

The need to incorporate Consumer Expenditure into the property market modelling was argued by the RICS (1994), Tsolacos (1995), Hendershott (1996), Brooks and Tsolacos (2000), and Hendershott *et al.* (2002a; 2002b). The significance of this variable was particularly emphasised within retail property studies. ONS' database contains 'Household Final

Consumption Expenditure' (HFCE) series (£ thousand). It is available from 1948 in annual figures. Additional information about this variable is available from the OECD (2011) and the World Bank (2011a).

Depreciation Rate

Depreciation Rate or Consumption of Fixed Capital and its effect on the property market was discussed by Hendershott (1996), McDonald (2002) and Orr and Jones (2003). The time-series, which is selected for the current research, is Consumption of Fixed Capital for 'Total Real Estate, Renting & Business Activities' (GRRD) (£ million). The series is available from 1948 in annual figures from the ONS. It is considered that this particular dataset suits the current study better than general depreciation rate series for 'Consumption of Fixed Capital: All Fixed Assets: Whole Economy' (NQAE). The GRRD series is subject specific. What is more, tracks the dynamics of the property market better.

Disposable Income

The use of Disposable Income as an explanatory variable was suggested by Tsolacos (1995) and Brooks and Tsolacos (2000). According to the ONS, 'Real Household Disposable Income' is the amount of money people have available to spend after taxes and other deductions. In the UK, this indicator is often compared against GDP, what commonly indicates the state of the living standards. The ONS database contains Disposable Income index series which is available from 1948 annually. The selected data-set was cross-referenced with that of the Health and Social Care Information Centre (2011). The correlation analysis indicated almost perfect positive correlation between two series (0.999).

Employment

The importance of employment has been argued by a number of researchers. Employment figures were used in various studies starting from an early publication of Hekman (1985) to those published more

recently, e.g. Hendershott *et al.* (2008) and Qun and Hua (2009). In his research, Wheaton *et al.* (1997, p.78) identified employment as 'the primary instrument driving office space demand'.

It is important to note, however, that property researchers were not using employment figures *per-se*, but narrower and more specific measures of the employment, such as Service Sector Employment (D'Arcy *et al.*, 1999; Orr and Jones, 2003), Employment in Banking, Finance and Insurance (Chaplin, 1998; Stevenson and McGarh, 2003), or Financial and Business Services Employment (Hendershott *et al.*, 2002a; 2002b; 2008). It was considered that these specific series capture activity within the property sector better (Stevenson and McGarh, 2003).

The ONS produces Employment figures for the Total Service Sector Employment (JWT8), Financial & Insurance Activities (K) (JWS7) as well as Real Estate Activities (L) (JWS8). However, all three employment series are available from 1978 only. Alternative Employment data sources are those of Feinstein (1972) and Liesner (1989). Feinstein produced data for Total Employment as well as for Employment in Insurance, Banking and Finance. The former series is for 1855-1965 period, while the latter is for 1920-1965 period with a gap in series over the 1939-1947 period. Liesner produced Total and Service Sector Employment figures for 1890-1987 period with the same data gap as in Feinstein (*ibid.*). A correlation analysis of both Feinstein's and Liesner's total employment figures indicates a strong interdependence between the two series with the correlation coefficient being 0.997. Subsequently, Liesner's longer Service Sector Employment time-series are combined with that of ONS. The correlation analysis over the 1978-1988 period, when both series overlap, indicate almost perfect positive correlation (0.969). Figure 4.11 shows the primary series. Figure 4.12 presents the final chain-linked Service Sector Employment figures for period 1963-2010.

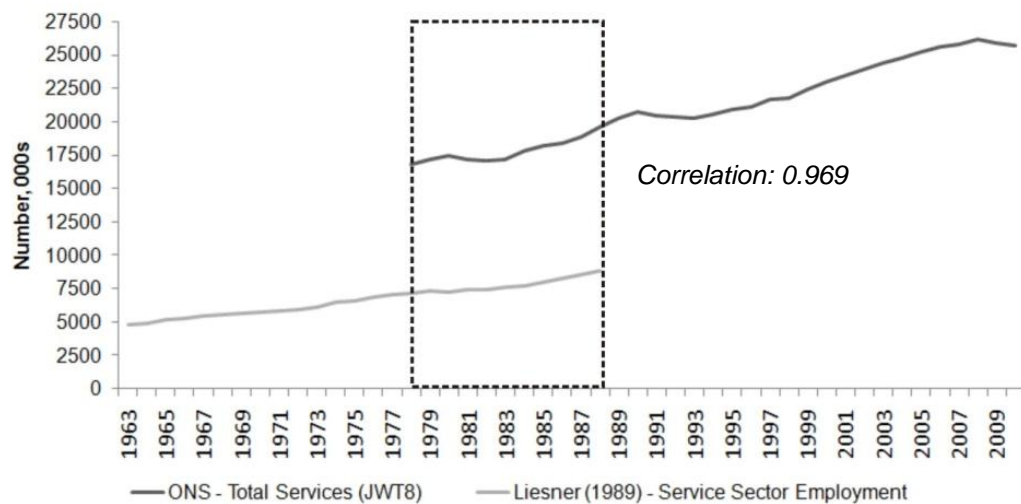


Figure 4.11 Liesner's (1989) and ONS' Service Sector Employment series
Source: Liesner (1989); ONS (2010)

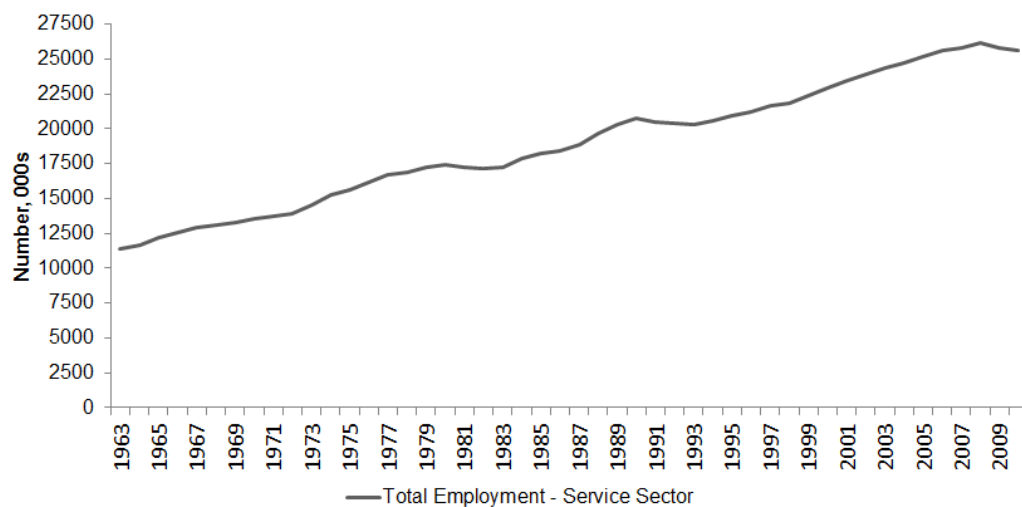


Figure 4.12 Chain-linked Total Service Sector Employment series
Source: Liesner (1989); ONS (2010)

Foreign Funds

In their empirical study, Qun and Hua (2009) identified that an increase in the use of Foreign Funds has a positive effect on the office rents in China. The authors identified that 'use of foreign funds' is a demand side variable which translates into office rents via its effect on the general economy and demand for office space. The high demand for office space comes from foreign companies establishing their presence in Mainland China.

In the UK a comparable variable is Foreign Direct Investment (FDI) series. The FDI for the UK is available from the ONS with 'Total Net Investment' (HJYU) (£ million) series starting from 1964. The ONS' series was also cross-referenced with that of the World Bank (BX.KLT.DINV.CD.WD). Correlation coefficient over the 1971-2008 period, when both series overlap, indicated almost perfect positive correlation (0.996). It therefore suggested high compatibility between two series with that of ONS thus being selected for the research.

FTSE All Share Index (FTAS)

The empirical evidences suggest that stock market data can be successfully used for commercial property market modelling. McGough and Tsolacos (1995a) included a share price index in their model to assess property cycles in the UK. Tsolacos (1995) used stock market data as an explanatory variable for industrial building investment. Chandrashekaran and Young (2000) employed S&P 500 index as a proxy for the rate of return on equities. Brooks and Tsolacos (2001) employed dividend yield data of the FTSE 100 for their comparative study. Karakozova (2004) selected stock market total returns as one of the explanatory variables to forecast office returns in the Helsinki area. Krystalogianni *et al.* (2004) used FTSE All-Share Index as a leading indicator to forecast UK commercial property cycle phases. According to McGough and Tsolacos (1995a, p.48), 'share price movements reflect the investors' expectations as well as conveying information about future economic conditions' which subsequently translate into the property market. Although, as Tsolacos (1995) noted, stock market price information can be misleading due to its medium-term volatility.

For the current research, however, the FTSE All-Share Index (FTAS) rather than FTSE 100 Index is selected. There are few major reasons why this particular index is chosen. First, FTAS is considered as the best performance measure of the London equity market since 1962 (FTSE, 2010). The Index represents 98-99 percent of UK market capitalisation

with the vast majority of UK-focused money, an increase from 93.9 percent in 2002 as indicated in Brealey (2002). What is more, this index is preferred over the FTSE 100 index, because FTSE 100 index comprises only the 100 most highly capitalised companies listed on the London Stock Exchange. FTSE 100 index represents approximately 81% of the UK market, far less than FTAS. It is also suggested that most of the companies from FTSE 100 derive a large part of their earnings from overseas investment activities rather than UK (MacGorian and Thompson, 2002; Hussain, 2010). It is therefore considered that FTSE All-Share Index represents sentiments of the UK business environment better.

Data on the FTSE All-Share Index was obtained from the Global Financial Data (GDF) (2012) and London Stock Exchange (2011). The series were then cross-referenced with those of Liesner (1989), the London and Cambridge Economic Service (1973), and Bond *et al.* (2001). An initial data analysis (visual inspection and correlation analysis) suggests that both Barclays Equity Price Index and FTSE All-Share Index are identical, i.e. the correlation coefficient over the 1963-2000 period when both series overlap equals 1. What is more, both series have a positive perfect correlation with GDF's data. Correlation coefficient is 1 over the same period. In addition to that, the correlation estimates suggest perfect positive correlation between GDF and Bond *et al.* (2001), i.e. correlation coefficient equals 1 for 1899-2000 period when both series overlap. These findings therefore allow concluding that historic series those of Bond *et al.* (2001) and GDF are reasonable representations of FTAS index. Whereas GDF data goes back farther than that of Bond *et al.* (2001) and with both series being perfectly correlated, GDF's series is subsequently used to extend FTAS series. Figure 4.13 and Figure 4.14 present the original and chain-linked FTSE All Share Index Growth series.

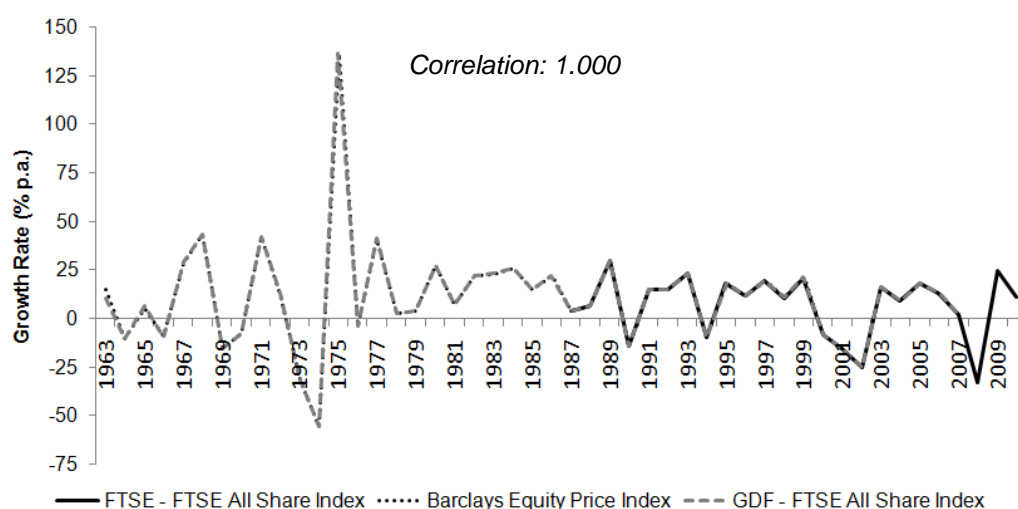


Figure 4.13 FTSE All Share Index Growth series
Source: Bond *et al.* (2001); GDF (2010); LSE (2011)

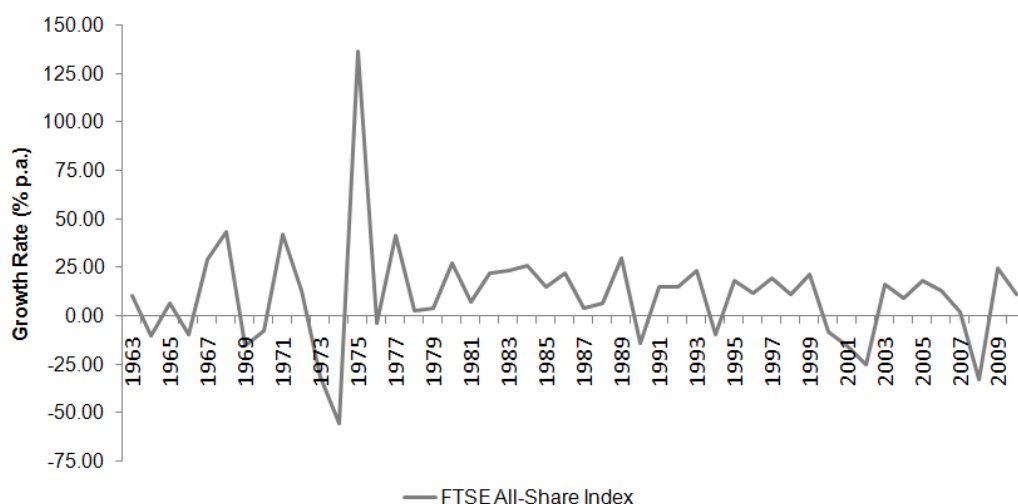


Figure 4.14 Chain-linked FTSE All Share Index Growth series
Source: Bond *et al.* (2001); GDF (2010); LSE (2011)

GDP

Gross Domestic Product was used in the number of studies, including Tsolacos (1995), Chaplin (1998), and Stevenson and McGarth(2003), as a measure of economic activity. As Stevenson and McGarth (2003) noted, GDP embodies economic growth in the whole economy which has a direct effect on the property market.

The GDP growth series is obtained from the ONS (2010), which is available from 1948 annually (ABMI).The series was also cross-referenced

with Liesner (1989) and the University of Groningen (Maddison-Project) data-sets. The correlation analysis was performed for 1961-1987 period where all three datasets overlap. The statistics indicated almost perfect positive correlation between ONS's and Maddison's series (0.999). Liesner's GDP figures were least correlated with those of the ONS (0.821).

ONS leading indicators

The Central Statistics Office (CSO) (now ONS) Leading Indicators (both Longer and Shorter) were used by Stevenson and McGarth (2003) to model the London office market. According to the authors, these two series contain a set of independent variables, which capture the dynamics of the UK business and economic conditions.

The difficulty with both series, however, is that they are no longer available. What ONS produces now is a set of Economic Indicators, which fall into five major categories, including 'Prices and Inflation', 'Labour Market', 'National Accounts Economic Activity', 'Balance of Payments and Trade', and 'Short Term Indicators'. The latter group of variables comprises Retail Sales, Index of Production, Labour Productivity, and Index of Services.

Retail Sales Index contains average sales of British retailers. However, the index is available from 1989 only. Index of Production goes back as far as 1948. However, it comprises output of production industries including, mining & quarrying, manufacturing, electricity, gas & water supply, food, drink & tobacco, machinery & equipment, and other manufacturing industries. This information is be useful in assessing the trajectory of the general economy. However, its usefulness for the property market analysis is questionable. Index of Labour Productivity, i.e. 'Output per Filled Job (Whole Economy)' (LNNP) is available from 1961. More specific 'Output per Filled Job (Services)' (GG5J) indicator, which suits the current research better, unfortunately is available from 1979 only. Finally, Index of Services, i.e. 'Total Services' (D8ZW), or more specific 'J&K Business

Services and Finance' (D92P), which shows movements in Gross Value Added for the service industries is available from 1996 only.

Inflation

Property, as equities (ordinary shares), represent ownership of tangible assets. It means that both investment types are performing well during inflationary times (Baum and Crosby, 2008). Various studies (Limmack and Ward, 1988; Matysiak *et al.*, 1996; Miles, 1996; Tarbert, 1996; Barber *et al.*, 1997; Bond and Seiler, 1998; Hoesli *et al.*, 2008) investigated this issue with most of them providing evidence that property could be a hedge against inflation. If to follow Collin (2007, pp.112) it implies that property investment 'will rise in value faster than the increase in the rate of inflation'. As Collin (*ibid.*, p.112) also noted (author has borrowed this quotation from Investors Chronicle) 'during the 1970s commercial property was regarded by investors as an alternative to equities, with many of the same inflation-hedge qualities'. The same is argued by Baum and Crosby (2008). The authors identified that the period from 1950s to 1990s, when significant inflation was witnessed in the UK, it was a major cause of a rise in property prices. Accordingly, Inflation, or Retail Price Index (RPI), was used as one of the explanatory variables in property rent modelling studies, including Chaplin (1998), Chandrashekar and Young (2000), and Stevenson and McGarh (2003).

Data on RPI is obtained from the ONS (CZBH). The series is available from 1949 to-date in annual figures. To check the significance of the selected series, it was cross-referenced with that of Twigger (1999) and O'Donoghue *et al.* (2004). The correlation coefficient between ONS and O'Donoghue *et al.* (*ibid.*) over the 1949-1998 period is 1, and between ONS and Twigger (1999) is 0.992. It indicates that both ONS and O'Donoghue *et al.* (*ibid.*) series are identical. It thus suggests that ONS' data is reliable.

Lagged Dependent Variable

Studies, including Chaplin (1998; 1999; 2000) and White *et al.* (2000), just to name a few, suggested that past values of the dependent variable may contain useful information which could be utilised in predicting its future behaviour. Accordingly, lagged values of UK All Property Rent series are employed in the current research.

Money Supply

In their paper, Matysiak and Tsolacos (2003) identified Broad Money Supply (M4) and Narrow Money Supply (M0) as prospective financial leading indicators to forecast property market rents. The cycles of these two indicators were expected to positively affect rental series.

For the current research, both money supply series are obtained from the ONS. Money Stock M4 (ATTD) (£ billion) is available from 1963 annually. However, Money Stock M0 (ATTC) (£ billion) is available from 1969 only. Accordingly, M0 series were chain-linked with Mitchell's (1992) 'Banknote Circulation' series. The visual inspection (Figure 4.15) and statistical analysis (correlation coefficient over the 1969-1988 period is 0.996) indicate that ONS' data is highly correlated with that of Mitchell (*ibid.*).

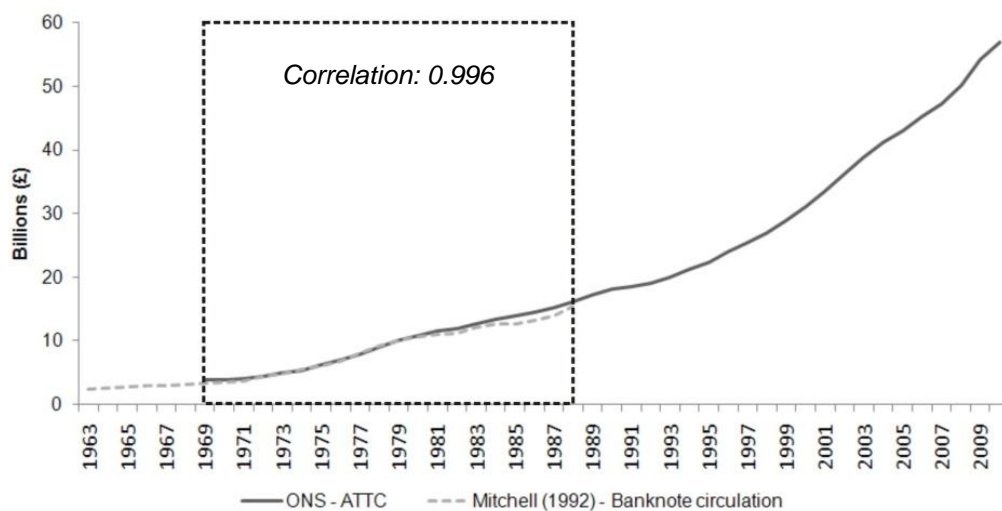


Figure 4.15 ONS' and Mitchell' (1992) Narrow Money Supply (M0) series
Source: Mitchell (1992); ONS (2010)

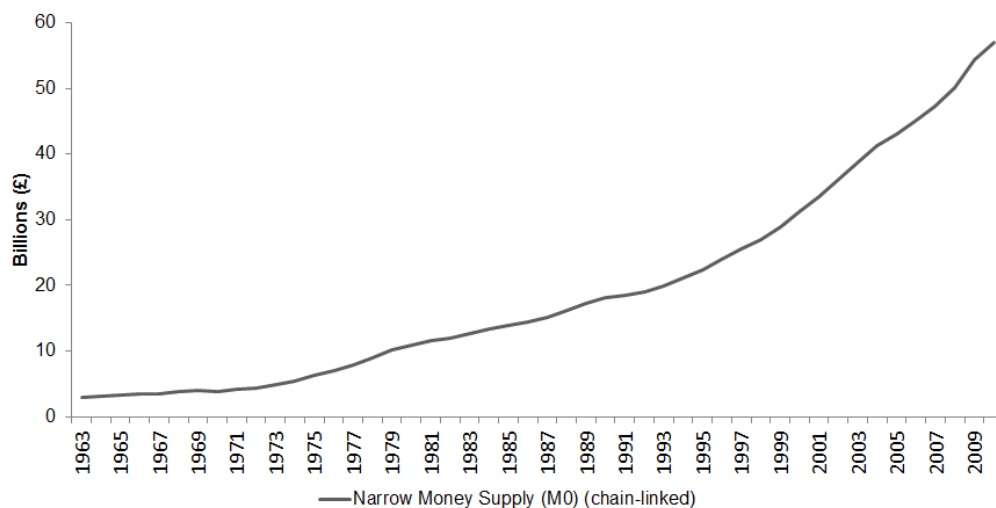


Figure 4.16 Chain-linked Narrow Money Supply (M0) series
Source: Mitchell (1992); ONS (2010)

Number of Property Transactions

According to Stevenson and McGarth (2003), the Property Transactions variable is positively correlated with the market sentiment. As the authors observed, the growing market sentiment turns property transactions upwards, while decreasing market sentiments turns property transactions downward.

The difficulty with this variable, however, is its availability. The publically available series for 'Number of Property Transactions' (thousands), those from the ONS and HMRC, are available for England and Wales from 1959 and for England, Wales and Northern Ireland from 1978 only. Long-term series, however, are not available for the whole of the UK. What is more, both series are for all (both residential and non-residential) property market. Neither ONS, nor HMRC produce separate long term commercial and residential transaction series.

Nevertheless, it is decided to select 'Number of Property Transactions for England and Wales' series as a proxy variable. The complete series for 1963-2010 period was compiled from ONS's FTPA series for 1963-2005 period and HMRC's 'UK Monthly, Quarterly and Annual Property Transactions Count' for 2006-2010 period (Figure 7.17 and Figure 7.18).

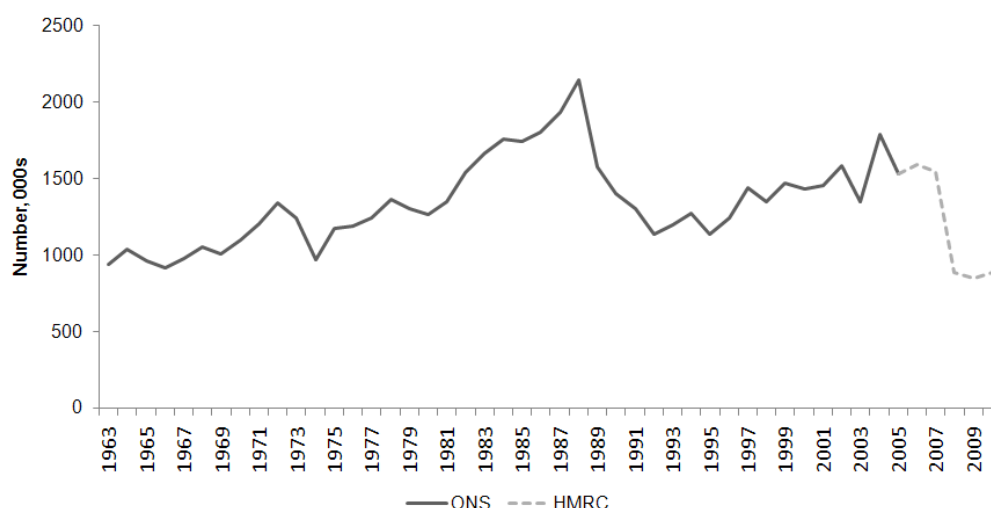


Figure 4.17 ONS' and HMRCs Number of Property Transactions series
Source: ONS (2010); HMRC (2011)

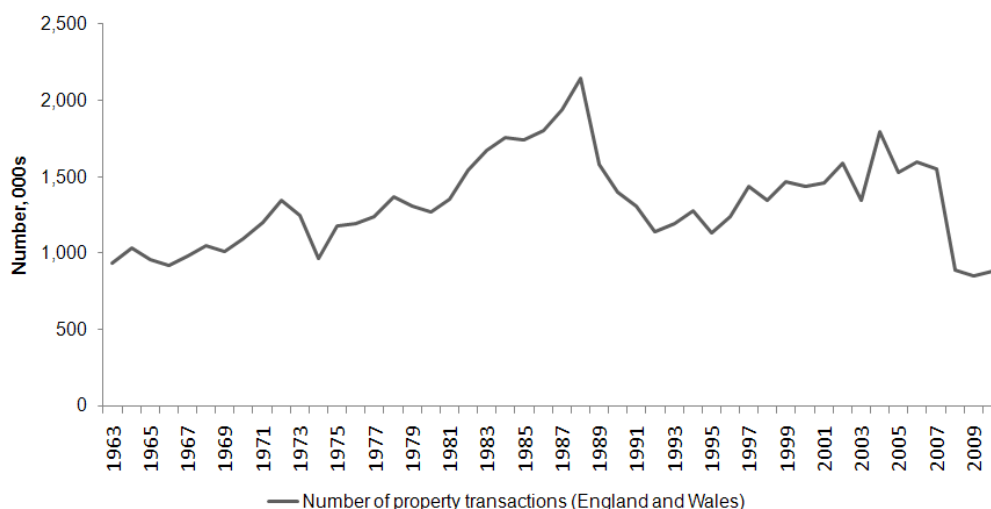


Figure 4.18 Chain-linked Number of Property Transactions series
Source: ONS (2010); HMRC (2011)

Profitability

According to Stevenson and McGarth (2003), Profitability, or Profits of the UK Companies, is a useful indicator which captures demand side effects of the commercial property market. Chaplin (1998) earlier identified it as one of the major explanatory variables to model office rents. Profitability measures were particularly used within retail property research. As RICS (1994) and Tsolacos (1995) suggested, retail profits can be used as an alternative measure for the demand for retail space.

The statistics of the Rate of Return of UK companies is available from the ONS. In its statistical bulletin ONS supplies figures for Manufacturing companies' Net Rate of Return, Service Sector companies' Net Rate of Return, the Net Rate of Return of companies other than United Kingdom Continental Shelf (UKCS), and the Net Rate of Return of United Kingdom Continental Shelf (UKCS) companies. The Service Sector data, which is the most applicable for the current research, however is available from 1989 only. A compatible longer data-set is the Annual Rate of Return of Private Non-Financial Corporations (PNFC) (percent), which is available from 1965 annually. According to the ONS, this series represents Gross trading profits of PNFC from United Kingdom operations plus rentals received less inventory holding gains. PNFC comprises UK Continental Shelf, manufacturing, non-financial service sector and other companies, including construction, electricity and gas supply, agriculture, mining and quarrying. Although this series is not property market specific, it nevertheless contains relevant statistical properties.

Property Values

In his empirical study Chaplin (1998) identified House Prices as one of the major explanatory variables to model the property market. For the UK, there are a number of house price information providers, including commercial companies such as Nationwide (2011) and Halifax (Lloyds Banking Group, 2012), as well as public organisations such as the ONS (2010), Communities and Local Government (2011), the Office of the Deputy Prime Minister (ODPM) (2006), and the Land Registry (2012). As Thwaites and Wood (2003) observed, the list of house price information providers increased with the housing web sites Hometrack (2012) and Rightmove (2012) introducing their Housing Indices. In addition to that, the RICS (2011) and the House Builders Federation (2011) also monitor the housing market.

However, as the comparative analysis suggests, different sources provide information in different formats and of different duration. ONS supplies

'Average Property Prices' (£ thousand) which are available from 1982. Communities and Local Government provides 'Average Dwelling Prices' (£ thousand) from 1970. Halifax (now part of Lloyds Banking Group) produces House Price Index for the whole country going back to 1983. Nationwide Building Society's database contains housing data for the UK since 1952 both in nominal (£ values) and index numbers.

Regardless of the number and availability of house price indices, the study uses Nationwide's House Price Index. First, it spans over the whole research period. Second, empirical evidences those of Thwaites and Wood (2003) suggest that this index tracks the typical house prices more closely than other indices. The index is volume-weighted, which means it is less sensitive to price movements in certain region. It uses a definition of a typical house that changes periodically, usually each year, to reflect for changing market conditions.

Unemployment

The local Unemployment rate was used by Hekman (1985) to model office rental values. Hekman's two-stage investment model identified Unemployment as one of exogenous demand for property measures. Hekman's regression analysis established Unemployment as significant (although negatively related) variable.

The Total Unemployment series for the UK is available from the ONS (LF2Q). However, this particular data-set is available from 1971 only. An alternative unemployment series are available from Liesner (1989) and Hicks and Allen (1999). The visual and statistical analysis indicate that both ONS' and Liesner's series are highly compatible. The correlation coefficient over the 1971-1987 period when both series overlap is 0.997, which indicates almost perfect positive correlation. Accordingly, both series were chain linked, which enabled to extend ONS' series over several decades. Figure 4.19 indicates dynamics of both series. Figure 4.20 shows final chain-linked UK Unemployment series.

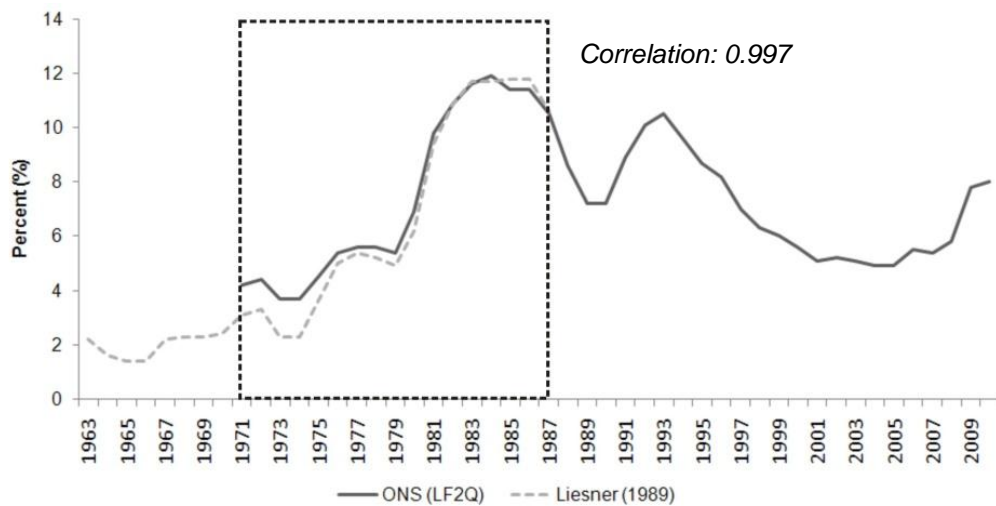


Figure 4.19 ONS' and Liesner's (1989) UK Unemployment series
Source: Liesner (1989); ONS (2010)

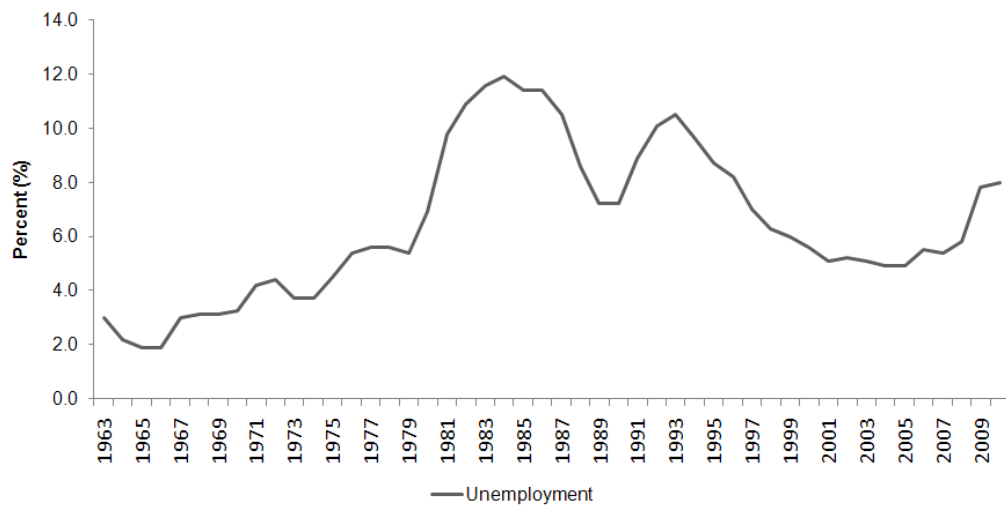


Figure 4.20 Chain-linked UK Unemployment series
Source: Liesner (1989); ONS (2010)

Yields on Government Securities

The performance of UK Government Debt Obligations was acknowledged by Hendershott (1996), Hendershott *et al.* (2002b), and Matysiak and Tsolacos (2003). According to Matysiak and Tsolacos (2003), both the Treasury Bill Rate and the Gilt Yields can be successfully employed to capture anticipated rental movements. The researchers suggested to use these variables as leading indicators for short-term commercial real estate market forecasting.

Two series are collected for the research. One is 2.5% Consolidated Stock Average Yield. The second is Par yield on long-dated British Government Securities (BGS) (20 years). The first series is obtained from the UK Debt Management Office (2011) which is available from 1900 annually. The 20-year British Government Securities (BGS) yield series is obtained from the Bank of England (2011) and the ONS (2010). ONS's series (AJLX) is available for period 1963-2007. The Bank of England (IUMALNZC) produces series for the 1993-2010 period. Visual and statistical analysis (correlation coefficient over the period 1993-2007 is 0.998) indicate that the series are highly compatible and can be linked together (Figure 4.21). The extended BGS (20 years) series are presented in Figure 4.22.

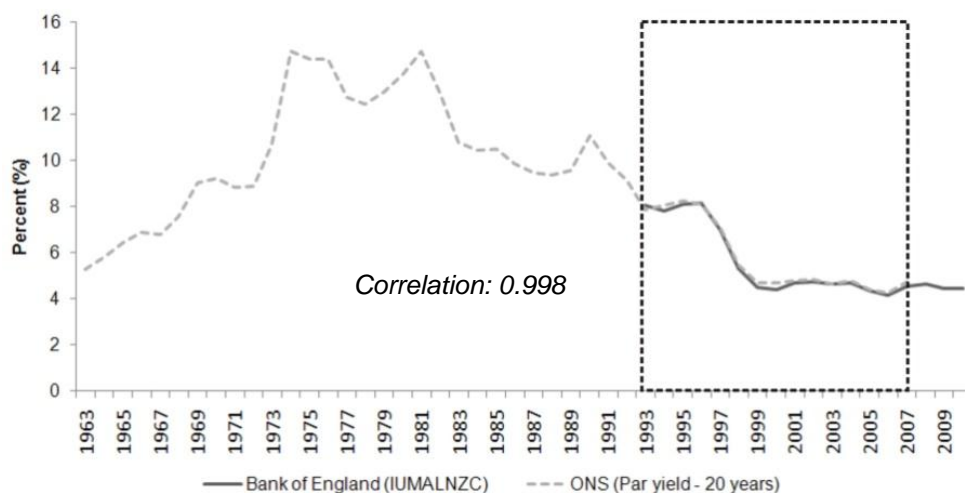


Figure 4.21 ONS' and BOE's 20-year BGS yield series
Source: ONS (2010); Bank of England (2011)

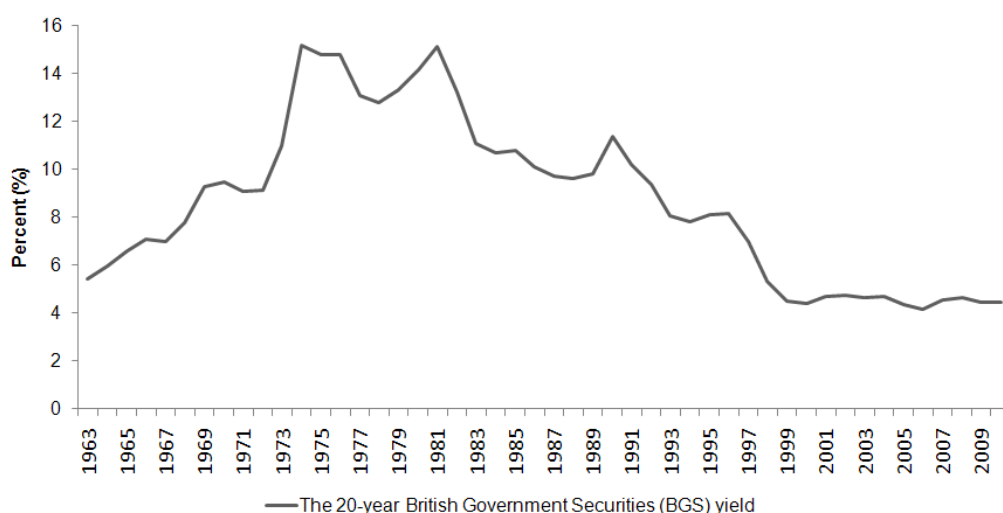


Figure 4.22 Chain-linked 20-year BGS yield series
Source: ONS (2010); Bank of England (2011)

Capital Formation

Capital Formation (CF), as Friedman (2000) defines is a creation (expansion) of capital (buildings, machinery, equipment) through savings that produces other goods and services. According to the World Bank (2010a), it consists of 'outlays on additions to the fixed assets of the economy plus net changes in the level of inventories', where fixed assets consist of land improvements, equipment purchases as well as construction. In general terms, Capital Formation is a component of GDP. This macroeconomic concept is therefore considered to be more useful for property market analysis than broader GDP, whereas it measures (in general terms) the level of investment in the economy, and therefore tracks the dynamics of the property market better.

As Statistics Canada (2008) identifies, capital formation is one of the key variables in any macroeconomic system. What is more, capital formation tends to be cyclical. When economy is growing, businesses expand and thus increase their capacity by building new plants, acquiring new equipment or occupying new space to meet growing demand. However, before new capital can be injected, there is a construction, planning or relocation time lag. Depending on the nature of the business, this lag can vary from a few months to years. This cascading lag, as Statistics Canada

suggests, is thus the major element of the cyclical nature of investment, which in turn is a major determinant of the cyclical nature of the whole economy.

The ONS' data-base contains various series for the Gross Fixed Capital Formation (GFCF). The most applicable for the current research are YGPB series, which is for Real Estate, renting and business (£ billion), and YGNG series, which is for financial intermediation. Unfortunately, neither of series is available for a long time-period. YGPB is available from 1989 only. YGNG is available from 1986 only. As such, a more general series is selected for the current research. The ONS structures GFCF series by sector and by asset. Sector-wise GFCF is divided into business investment, general government, dwellings and transfer costs of non-produced assets. Asset-wise GFCF is for transport equipment, other machinery and equipment, dwellings, other building and structures and intangible fixed assets.

Business Investment (NPEK) sector specific GFCF series is considered to be the most applicable for the current research. It represents an element of Total Business Investment within GFCF and is the longest series available, starting from 1965. Its statistical analysis with three GFCF series (NE.GDI.FTOT.ZS; NE.GDI.FTOT.KN; NE.GDI.FTOT.CN) produced by the World Bank (2011a) indicates almost perfect positive correlation with correlation coefficient between NPEK and NE.GDI.FTOT.KN series being 0.992. Accordingly, NPEK series were extended for several years by chain-linking it with World Bank's NE.GDI.FTOT.KN series which is available from 1960 (Figure 4.23 and Figure 4.24).

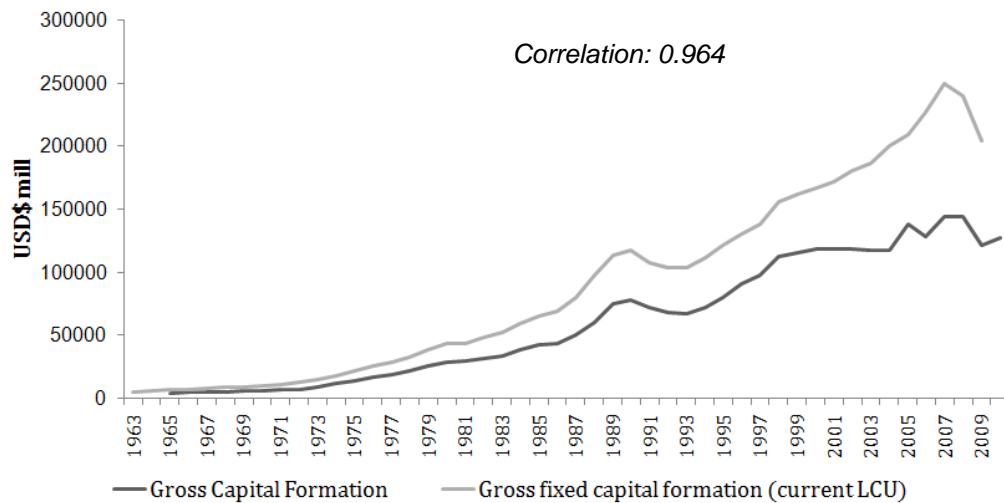


Figure 4.23 ONS' and World Bank Capital Formation series
Source: ONS (2010); World Bank (2011a)

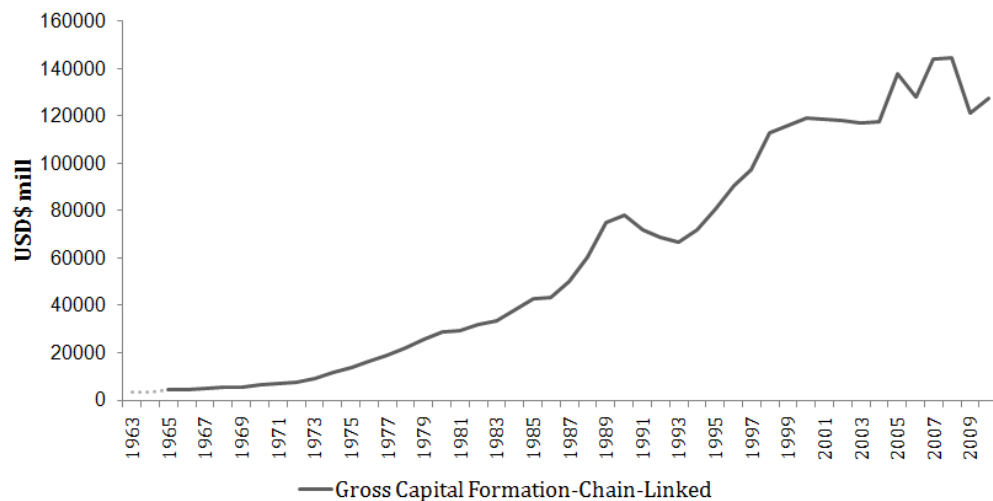


Figure 4.24 Chain-linked Capital Formation series
Source: ONS (2010); World Bank (2011a)

Job Vacancies

The Job Vacancies or more specific 'Number of Employee Workforce' (BCAJ) (thousand) series represents available vacancies in the country. In contrast to Employment and Unemployment, the BCAJ series indicates potential employment opportunities. It implies the possible future employment for unemployed population or for those willing to change their current employment. It also indicates the level of employment businesses are willing to provide. As a result, the growing number of vacancies implies a growing demand for new employees, which as a result translates into a

greater demand for space. The longest series is that of 'All Industries' (BCAJ), which is available from 1959.

Land Value

The importance of land value was argued by the number of researchers (Fraser, 1984; Capozza and Helsley, 1989; Stone and Ziemba, 1993, Ball *et al.*, 1998). Fraser (1984) regarded land and its fixtures as a single element which constitutes the concept of real estate. Ball *et al.* (1998, p.58) argued that 'the land market had a key role in determining the equilibrium quantities of commercial property supplied and demanded'. Same as Fraser (*ibid.*), Ball *et al.* (*ibid.*) regarded land as a factor input for the production process (economic activity of firms) to commence. What is more, land was identified as being inelastic. According to Ball *et al.*, land market is not fully competitive, whereas each site is unique in terms of its location. Moreover, the number of sites suitable for commercial activity in general is restricted.

Despite the obvious significance of the land for the commercial property market, land variable has not been largely employed to model commercial property rents. Hendershott (1996, p.65) used Land Price series as an indicator 'of a speculative bubble' in the Sydney Office market. However, this variable was more of an indicative nature. As the author noted, value of land can generate miss-measurements in replacement-cost ratio. Therefore, in his valuation model, Hendershott did not use Land Value series separately, but incorporated it into the total value of the property. Wheaton *et al.* (1997) estimated that land accounts for around two-thirds of commercial property value in London. However, as the authors noted, 'little reliable data is available on land prices' (*ibid.*, p.84).

The Land Value series for the UK are obtained from Holmans (2005) and the Department for Communities and Local Government (2011). Holmans (*ibid.*) in his publication produced an index of land prices at current and constant prices for the UK for 1963-2002 period. The Department for Communities and Local Government database contains table for 'Average

Valuations of Residential Building Land With Outline Planning Permission' (table 563) for 1994-2010 period. The correlation analysis over 1994-2002 period when two series overlap indicates almost perfect positive correlation between both Holmans' and Communities' data-sets. Correlation coefficients between Holmans (current prices) and Communities series, and Holmans (constant prices) and Communities are 0.994 and 0.986 respectively. To make series comparable, Communities' nominal land values were converted into index numbers with 1994 being a base rate. Correlation coefficients between all series remained unchanged (Figure 4.25). Accordingly, both series were chain-linked together. Final series is presented in Figure 4.26.

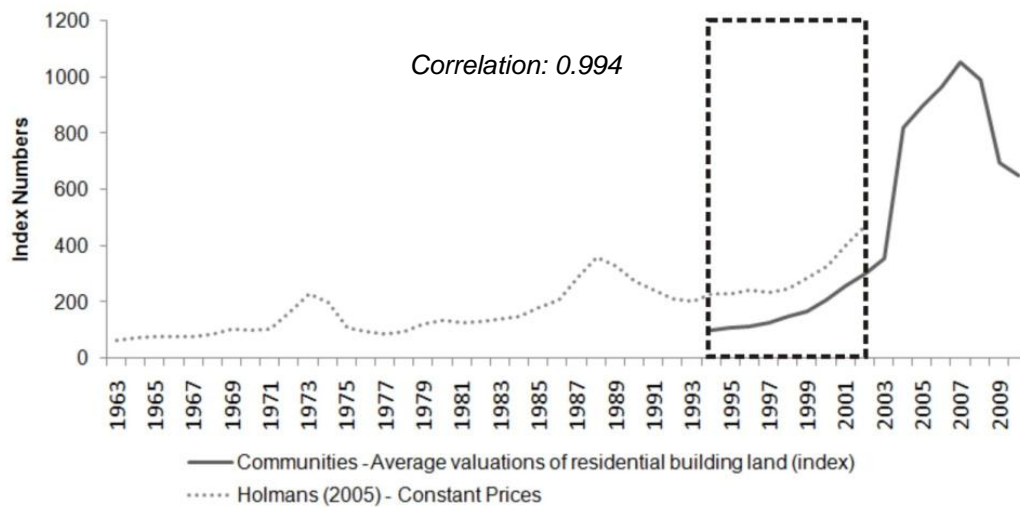


Figure 4.25 Holmans' and Communities' UK Land Value Index series
Source: Holmans (2005); Communities (2011)

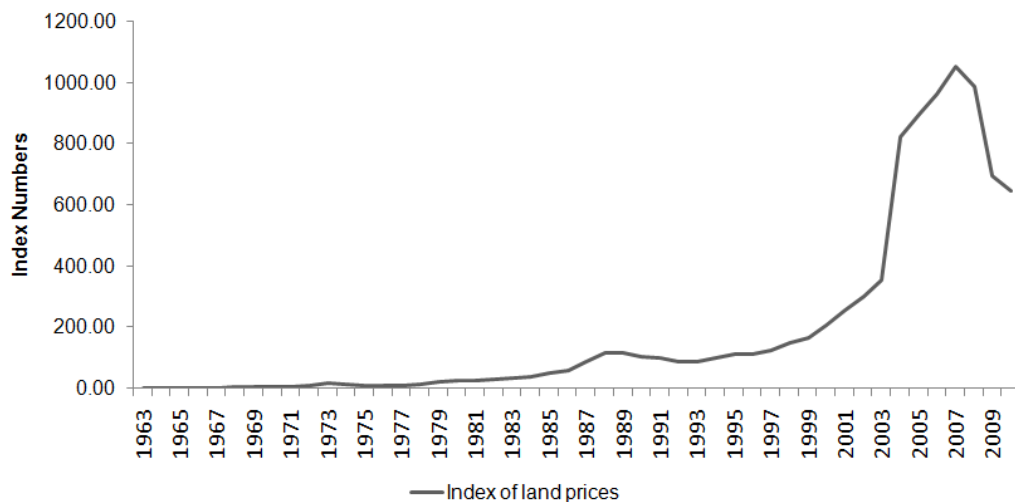


Figure 4.26 Chain-linked UK Land Value Index series
Source: Holmans (2005); Communities (2011)

Net Investment

Net Investment by Insurance Companies, Pension Funds and Trusts (MQ5) series contains important information on the activities of these financial entities. Being an important component of UK's GDP, this series is also of great significance in assessing how key investor groups are investing their funds. It provides information on whether they are buying or selling shares, fixed-income securities, or they are moving into longer-term assets. The value of their holdings at the end of the year is subsequently recorded in the annual ONS' balance sheet survey.

The significance of this variable can also be argued by emphasising the importance of the financial service sector to the UK economy and the property market. Lizieri (2009a) argued that concentration of the financial activity within the City of London leads to the concentration of specialist labour which in turn triggers financial and business service sector employment, which consequently has significant property market implications. His estimates suggest that the City of London financial and business service employment increased by 41 percent over the 1971-2006 period. This significant increase had important ramifications for the City of London office market, as well as for the UK economy as a whole. Earlier hypotheses by Fraser (1984) suggested that changing demand for

banking and insurance activities, which are dominant industries within the City of London, explains the changing demand for commercial property.

Haldane's *et al.* (2010) publication stressed the significance of the Financial Sector (FS) to the UK economy. The statistics authors provided indicates that 'growth in financial sector value added has been more than double that of the economy as a whole since 1850' (*ibid.*, p.4). These findings corroborated Turner's *et al.* (2010) observation, that over the previous 20 to 30 years, the financial service sector grew much faster than the general economy. According to Haldane *et al.* (*ibid.*), the financial intermediation, measured by its real value added, has more than trebled over the 1980-2008 period, while the output of the whole economy doubled over the same period. Their calculations indicated that in 2007 financial intermediation accounted for around 8 percent of the total GVA. Profits gained from this activity (of the whole economy) increased to 15 percent by 2008 from 1.5 percent over 1948-1978 period. Haldane *et al.* (*ibid.*) therefore suggested that FS industry 'has undergone, at least arithmetically, a 'productivity miracle' over the past few decades' (*ibid.*, p.3).

In their report, PWC (2010) estimated, that FS as a whole made Total Tax Contributions of £53.4 billion for 2010, which is 11.2 percent of total government tax receipts from all taxes for the same year. This led PWC to suggest that FS is 'a major contributor to UK public finance', greater than the oil and gas industry (*ibid.*, p.3). What is more, FS was identified as a major employer in the UK with over a million employees working in the sector, which is around 3.5 percent of the total UK workforce. PWC' employment figures match those of the Financial Services Skills Council (FSSC) (2010). In their report FSSC estimated that there are more than 34,000 FS companies operating in the UK and employing around a million individuals. FSSC also estimated that the insurance sector contribution (net) to UK balance of payments is around £10 billion.

Europe Economics' (2011) report also indicates the great role FS plays for the major European Financial Centres and European Union as a whole. As the report identifies, 17 percent of all global equity trading and 11 percent of global funds management take place in London. It therefore suggests that 'financial services are of enormous social value' for the EU (ibid., 77).

In addition to that, the research published by the Oxford Economics (2011) for the City of London Corporation suggests that in 2009-2010 London financial services contributed £1.4 billion in taxes, which is around 21 percent of the UK's total GVA. The report also expects this contribution to the UK's fiscal position to rise in the forthcoming years.

Seeing the role Financial Services play within the UK economy and its subsequent implications to the property market, it can thus be suggested that introduction of variable, which reflects the dynamics of FS, is of benefit for the current research. The variable considered is 'Investment by insurance companies, pension funds and trusts - UK buildings, property, land & new construction work (RLKD)' (£ million). This particular variable represents a volume of investment by financial institutions into building, property, land and new construction. The series is available for the whole research period annually.

Total Returns

Property Total Returns, as noted, was used by various property researchers as a measure of the dynamics of the property market. However, neither Total Returns were used to model property rents, nor rents were used to model Total Returns. Therefore, the research assesses whether Total Returns has any statistical connections with rents. The Total Returns series comes from IPD data-base and Scott's (1996) statistical tables. Both series were already successfully combined by RICS (1999). As statistical (correlation coefficient is 0.999 for 1971-1993 period) and visual analyses (Figure 4.27) indicate, the two series are highly compatible. Final series are presented in Figure 4.28.

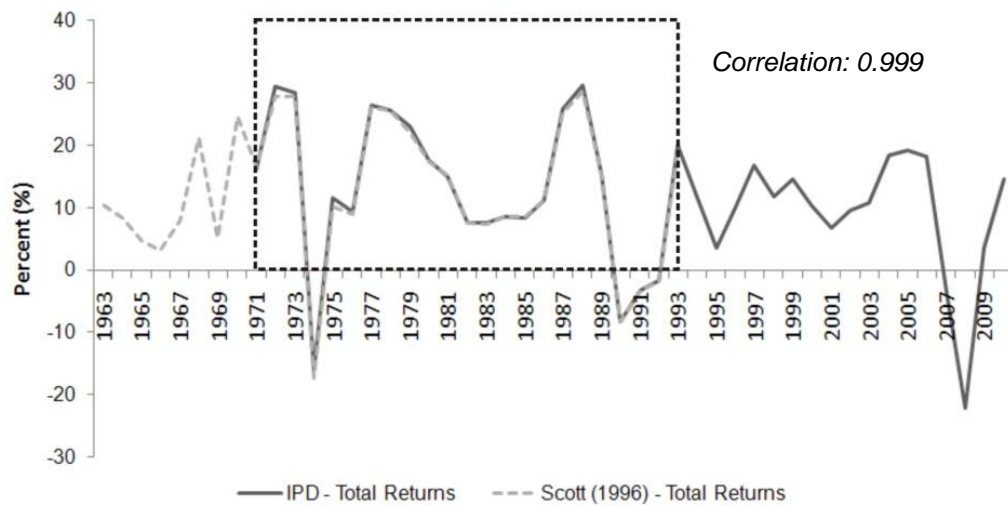


Figure 4.27 Scott's (1996) and IPD's All Property Total Returns series
Source: Scott (1996); IPD (2011)

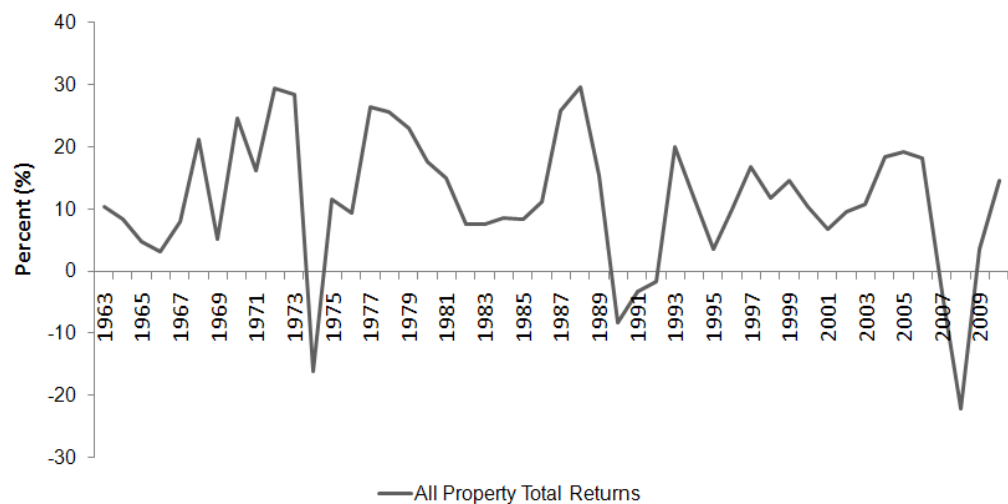


Figure 4.28 Chain-linked All Property Total Returns series
Source: Scott (1996); IPD (2011)

Details of the full time-series of each variable are included as Appendix 1.

4.4.3 Variable reduction

Following Makridakis *et al.* (1998), it would then be desirable to create a model based on all of these explanatory variables whatever their number. However, as the commentators suggest, it is not be feasible to compute a model incorporating all possible variables due to costs involved as well as the level of computation it may require. Koop (2006) also notes statistical

issues it may encounter, including omitted variables bias and multicollinearity.

Therefore, a combination of both simple and more complex variable reduction techniques is used to determine which the key variables are. These variable reduction techniques are 'What Others Do', 'What Experts Advise', Stepwise Regression (Forward), Stepwise Regression (Backward), and Granger Causality.

According to Armstrong (2001, p.365), 'What Others Do' approach means that variables are selected based on findings from a similar study on the subject. Following Ball *et al.* (1998) and Barras (2010), variables which came as being significant to model commercial property rents were Bank Rate, Construction Orders, Employment, GDP, and Inflation.

What 'experts advise' approach employs expertise from a given subject area (Armstrong, 1980). Following this procedure and examining studies on commercial property rent determination, including McGough and Tsolacos (1995b), Tsolacos (1995), D'Arcy's *et al.* (1999), Chaplin (1998; 1999), Brooks and Tsolacos (2000) and Füss *et al.* (2012), it was established that Bank Rate, Construction Costs, Construction Orders, Employment and GDP were amongst the key explanatory variables.

Stepwise Regression, according to Draper and Smith (1998), Makridakis *et al.* (1998) and PASW 18 (PASW, 2010b), is a statistical tool which sorts out the relevant explanatory variables from a large set of candidate variables. Backward elimination removes variables with the largest probability of F-test value at each step. Forward entry adds variables with the smallest probability of F-test value to the equation one at a time. The Forward elimination estimated that only Construction Output and GDP are the key variables. The Backward elimination suggested that Construction Costs, Construction Orders, Construction Output and GDP are significant in explaining the dependent variable.

Granger Causality, as Koop (2006) suggests, uses t-statistics and P-values of individual coefficients to determine whether a variable is

significant. In this case, only Bank Rate and Construction Costs had any relevant statistical properties to model the dependent variable.

This combination of variable reduction methods enabled the production of the final ‘Short List’ of explanatory variables. These variables are as follows: Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment, and GDP (Table 4.2). Accordingly, these seven variables were further used for the research.

One interesting observation arises from this exercise – a prominence of construction based series. While GDP and Employment series were well document in the commercial property modelling literature, construction based variables were less discussed. A good account of that presented GVA (2009) in their report. According to GVA, rental growth (decline) is linked not only to economic growth (decline), but also to the development situation. Certainly, strength of the economy has a dominant effect on the need for property. However, the consultants also suggest that interplay between demand and supply for property and a lag in bringing new projects into the market is now becoming even more significant. Their suggestion is that if supply side of the equation does not correspond to customer needs, it will make customers look for alternatives, thus having effect on property development market and subsequently on rents. Which is why construction related series should be incorporated into the modelling process of the commercial property market.

| Variable | ‘What Others Do’ | ‘What Experts Advise’ | Stepwise Regression (Forward) | Stepwise Regression (Backward) | Granger Causality |
|--|------------------|-----------------------|-------------------------------|--------------------------------|-------------------|
| Bank Rate (BR) | X | X | | | X |
| Construction Costs (CCs) | | X | | X | X |
| Construction Orders (CO _r) | X | X | | X | |
| Construction Output (CO _u) | | | X | X | |
| Construction Starts (CSt) | | | | | |
| Employment (E) | X | X | | | |
| Gross Domestic Product (GDP) | X | X | X | X | |

Table 4.2 The summary table of variable importance

Before that, all variables were tested for stationarity following the methodology discussed in Section 3.4.10. Unit-root test results are presented in Table 4.3.

| Variables | | t-stat (y_t) | t-stat (y'_t) | t-stat (y''_t) |
|--------------------------|----------------------|-------------------|-------------------|--------------------|
| Bank Rate | | 1.393 (0.170) | -5.890 (0.000) | |
| Business Output | | 2.446 (0.018) | -3.623 (0.001) | |
| Car Registrations | | -1.795 (0.079) | -4.886 (0.000) | |
| Construction Orders | | -1.623 (0.112) | -4.243 (0.000) | |
| Construction Completions | Construction Output | -0.856 (0.397) | -4.533 (0.000) | |
| | Building Completions | -0.541 (0.591) | -6.229 (0.000) | |
| Construction Cost | | 1.165 (0.250) | -1.616 (0.113) | -5.845 (0.000) |
| Construction Starts | | -2.081 (0.043) | -6.683 (0.000) | |
| Consumer Confidence | | -3.241 (0.003) | | |
| Consumer Expenditure | | 6.115 (0.000) | -2.243 (0.002) | -9.747 (0.000) |
| Depreciation Rate | | 6.662 (0.000) | -2.153 (0.037) | -7.134 (0.000) |
| Disposable Income | | 0.646 (0.522) | -4.289 (0.000) | |
| Employment | | -0.904 (0.371) | -3.734 (0.001) | |
| Foreign Funds | | -6.481 (0.000) | | |
| FTSE All Share Index | | -0.300 (0.766) | -6.384 (0.000) | |
| GDP | | -4.613 (0.000) | | |
| ONS Leading Indicator | Index of Production | -2.268 (0.028) | -5.331 (0.000) | |
| Inflation | | -2.303 (0.026) | -6.772 (0.000) | |

| Variables | | t-stat (y_t) | t-stat (y'_t) | t-stat (y''_t) |
|---------------------------------|-------|-------------------|--------------------|--------------------|
| Lagged Dependent Variable | | -2.019 (0.050) | -4.0945 (0.000) | |
| Money Supply | M4 | 10.984 (0.000) | -1.817 (0.076) | -9.257 (0.000) |
| | M0 | -2.199 (0.033) | -7.460 (0.000) | |
| Number of Property Transactions | | -2.199 (0.033) | -7.460 (0.000) | |
| Profitability | | -1.618 (0.113) | -4.951 (0.000) | |
| Property Value | | 1.744 (0.088) | -3.533 (0.001) | |
| Risk Premium | | -4.206 (0.000) | | |
| Unemployment | | -1.431 (0.159) | -3.793 (0.001) | |
| Yields of Government Securities | Short | -0.955 (0.345) | -4.859 (0.000) | |
| | Long | -0.887 (0.380) | -4.708 (0.000) | |
| Capital Formation | | -0.131 (0.897) | -6.914 (0.000) | |
| Job Vacancies | | -0.362 (0.719) | -3.621 (0.001) | |
| Land Value | | -0.471 (0.640) | -4.832 (0.000) | |
| Net Investment | | -0.914 (0.366) | -5.136 (0.000) | |
| Total Returns | | -4.851 (0.000) | | |

Table 4.3 OLS estimation results for AR(p) model in testing for a unit-root
(P-values in parentheses)

NB: Model Estimated for $\Delta y_t = \alpha + \rho y_{t-1} + e_t$, $\rho = 0$; Critical Value at 5% is -2.89

The following table reports estimates for persistence and cross correlation. The low values of AR(1) term suggests that series do not contain memory. It implies that time-series values at a certain period of time are not related to their previous estimates. In other words, high (low) volatility in the past will not translate into high (low) volatility in the future. This low level of autoregression is evident within all explanatory variables. The largest AR (1) value is 0.552 which is for Construction Costs (Table 4.4).

| Variable | Cross correlations with HP Cycle (Rents) at time t | | | | | | | Persistence |
|-----------------------------|--|--------------|--------------|--------------|--------------|--------|--------|--------------|
| | t-3 | t-2 | t-1 | t | t+1 | t+2 | t+3 | AR (1) |
| HP Cycle (Rents) | | | | | | | | 0.663 |
| HP Cycle (BR) | -0.182 | -0.029 | 0.236 | 0.471 | 0.446 | 0.148 | -0.182 | 0.219 |
| HP Cycle (CCs) | -0.378 | -0.301 | -0.099 | 0.185 | 0.403 | 0.416 | 0.249 | 0.552 |
| HP Cycle (CO _r) | 0.418 | 0.760 | 0.810 | 0.551 | 0.101 | -0.353 | -0.543 | 0.401 |
| HP Cycle (CO _u) | -0.091 | 0.307 | 0.717 | 0.902 | 0.737 | 0.244 | -0.257 | 0.371 |
| HP Cycle (CSt) | 0.421 | 0.246 | 0.019 | -0.147 | -0.274 | -0.241 | -0.080 | 0.140 |
| HP Cycle (E) | 0.244 | 0.581 | 0.731 | 0.731 | 0.627 | 0.308 | -0.046 | 0.547 |
| HP Cycle (GDP) | 0.400 | 0.734 | 0.835 | 0.633 | 0.261 | -0.179 | -0.379 | 0.348 |

Table 4.4 Cross correlation and persistence estimates for HP cycles

The subsequent statistical analysis suggests that Construction Output and Employment cycles coincide with the Rental cycle. This is evident from the large value of correlation coefficients between dependent and the explanatory variables. The correlation coefficient between Rental cycle and Construction Output and Employment is 0.902 and 0.731 respectively.

Construction Orders and GDP cycles lead by one and two periods. However, neither of explanatory variables lead at the three period level. The only variable which lags the Rental cycle is Construction Output.

The high level of cross-correlation between HP Rental Cycles and Construction Orders (0.810) and GDP (0.835) series is seen from Figure 4.29 and Figure 4.30. Certainly, there are periods when series exhibit different dynamics especially in early 1970s and during late 2000s. However, the general pattern suggests that series follow the same trajectory. Interestingly, property consultancies, including GVA (2009), also related New Construction Orders and GDP growth to the dynamics of the commercial property rental cycle.

The following section summarises the key findings of the Chapter 4.

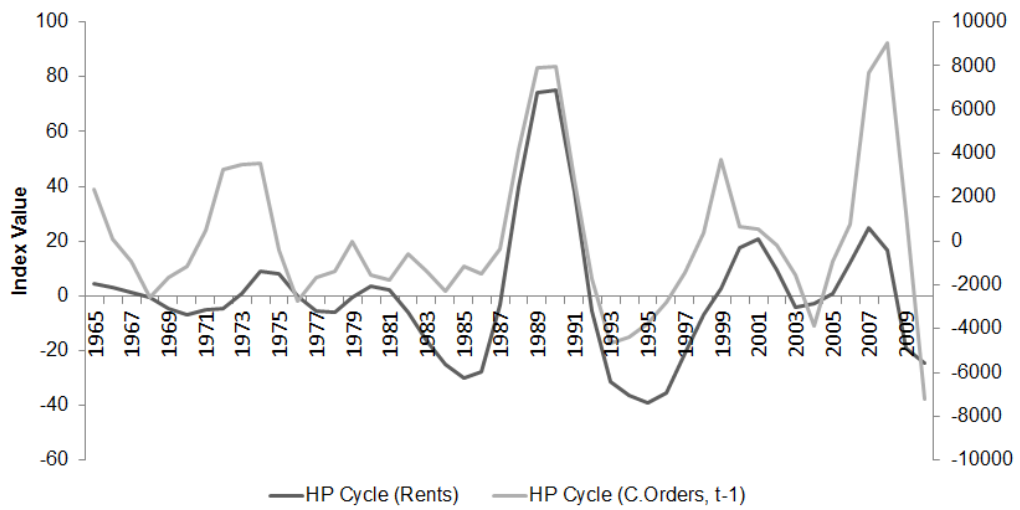


Figure 4.29 Cross-correlation of HP cycles for Rent Index and C.Orders

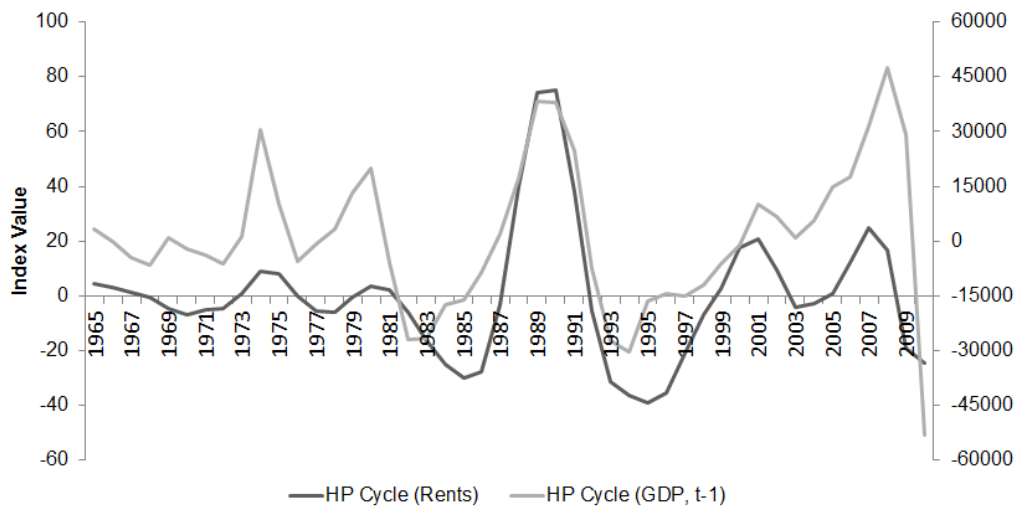


Figure 4.30 Cross-correlation of HP cycles for Rent Index and GDP

4.5 Summary

This chapter discussed the importance of long-term series in analysing property cycles. It assessed difficulties related to UK property data and its acquisition. It then presented the principle of chain-linking as the statistically robust solution for time-series combination. Following on from this, it evaluated the properties of the dependent and explanatory variables, as well as presented five variable reduction methods which were employed to estimate the key variables to model the dependent variable. These variable reduction techniques were 'What Others Do', 'What Experts Advise', Stepwise Regression (Forward), Stepwise Regression (Backward), and Granger Causality. Explanatory variables, which were selected for further modelling, are Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment, and GDP.

The importance of long-term series, as the research suggests, comes from two main reasons. First, it allows researchers to assess what generated cycles and how they have evolved. The long-term series analysis helps to appreciate important changes which occurred over time. Second, long term-series are necessary for model building purposes. In the literature it was identified that the longer the series, the better the model estimates can be obtained. Previous research has suggested that for a univariate time-series model there is a need for at least 50 observations. To build a reliable regression based model, at least 20 observations are required.

The discussion above suggested that the UK data is probably the best documented in Europe. The commentators commented that it goes back for several decades, it is available at national and local levels, as well as in various frequencies. It therefore makes it possible to produce sound market analytics. However, as the prior studies on the subject have noted, the UK data is not without criticism. The difficulties related to the UK data, which were discussed almost a quarter century ago, were also commented on within more recent publications. Certainly, researchers

appreciate that the UK market data is rich and diverse. However, it was suggested that there are many challenges related to data quality and quantity, access to it, as well as the costs involved in obtaining the data, with all that limiting the scope of any research.

Subsequently, the principle of chain-linking was presented as an alternative time-series combination tool. It was suggested that chain-linking is a robust series combination approach which is used by major organisations.

For the dependent variable, the study employed IPD All Property Rental Value Growth Index. It was suggested that IPD provides the most reliable property market benchmarks in the UK. Regarding rental series, the discussion noted that rent is an important variable in analysing the property market. It was commented that rent brings the occupier, lender, developer, and land markets into one equilibrium state. As such, some commentators noted that rent is the most important variable in property economics.

The current study subsequently extended the original IPD series by chain-linking it with an alternative rental series following previous empirical studies. It then assessed cyclical properties of the dependent variable. The estimates suggested that an average period of UK rental cycle is 9 years of length and that cycles are getting shorter and more volatile over time.

Following on from this, the current study acquired series on twenty-seven explanatory variables by analysing data-sets of seventeen organisations and thirteen publications. It also employed twelve alternative sources of data to support, cross-reference and extend selected time-series. Accordingly, simple and more complex variable reduction techniques were employed to determine the key explanatory variables. It estimated that Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment, and GDP are the main variables to

model rental series. The subsequent cross-correlation analysis supported these findings.

These estimates were in line with the literature on the subject. GDP, Employment and construction related series in particular were estimated as being significant for commercial property market analysis. The significance of Construction Orders, for example, was commented by the major property consultancy. It related dynamics in construction orders to the commercial property rental cycle. As such, it heightened the importance of selected variables and their use for the current research study.

Having identified variables that will be used to model the commercial property market in the UK, the next chapter presents modelling estimates, together with the analysis of results.

CHAPTER 5 EMPIRICAL RESULTS

Previous chapters have introduced the objectives and scope of the present research. Chapter 2 discussed the subject of property market modelling and forecasting. Chapter 3 presented Combination Forecasting as an alternative forecasting accuracy improvement technique. Chapter 4 dealt with dependent and explanatory variables used for the research.

This chapter presents modelling estimates. It details the statistical analysis carried out with respect to the stated aims of the research. It then analyses and interprets results. The chapter transforms the modelling estimates obtained into credible evidence about UK commercial property market modelling and forecasting, and its accuracy improvement through Combination Forecasting. Although a number of research constraints played a role in the research process, the estimates obtained confirmed the usefulness of Combination Forecasting.

Chapter 5 is divided into six key sections. Section 1 explains in-sample modelling results obtained from Exponential Smoothing, ARIMA/ARIMAX, Simple and Multiple Regression specifications, and VAR specifications. Section 2 assesses out-of-sample accuracy of these models. Section 3 presents estimates of the Combination Forecasting. Section 4 comments on forecasting accuracy. Section 5 analyses the usefulness of Combination Forecasting. Section 6 summarises the main findings.

5.1 In-sample forecasting estimates

5.1.1 Exponential Smoothing model estimates

Single exponential smoothing, Holt's Linear Trend and Brown's Linear Trend modelling is performed using PASW 18 'Time Series Modeller' algorithm. For Single exponential smoothing, algorithm uses Equation 1 explained in Section 3.4.1. Holt's Linear Trend model is computed from Equation 2, which was presented in Section 3.4.2. Brown's Linear Trend model is estimated using three-set equation established in Section 3.4.3.

As both statistical (Table 5.1) and visual (Figure 5.1; Figure 5.2; Figure 5.3) analyses suggest, none of the Exponential Smoothing models fit the stationary rental series. The R-squared of each of the specifications is less than 0. Other statistical measures, including MSE and AIC, are also insignificant.

| Model Specification | Model Fit statistics | | | | | |
|------------------------------|----------------------|-------|---------|--------|--------|--------|
| | R-squared | MAE | MAPE | MSE | AICc | BIC |
| Single exponential smoothing | -0.027 | 4.399 | 109.271 | 31.078 | 130.87 | 134.97 |
| Holt's Linear Trend | -0.027 | 4.390 | 110.324 | 31.101 | 131.15 | 135.26 |
| Brown's Linear Trend | -0.001 | 4.358 | 100.327 | 30.289 | 131.23 | 135.33 |

Table 5.1 SES, HLT and BLT model fit statistics

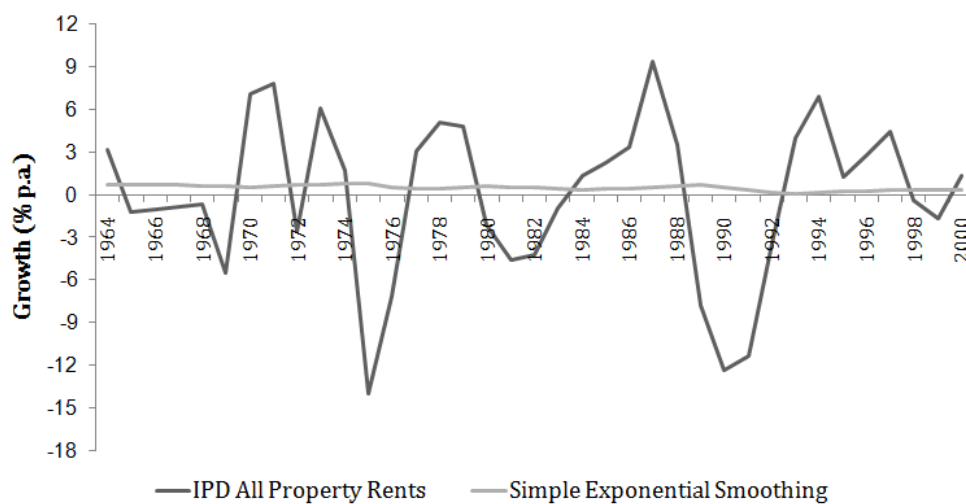


Figure 5.1 Single exponential smoothing (model fit)

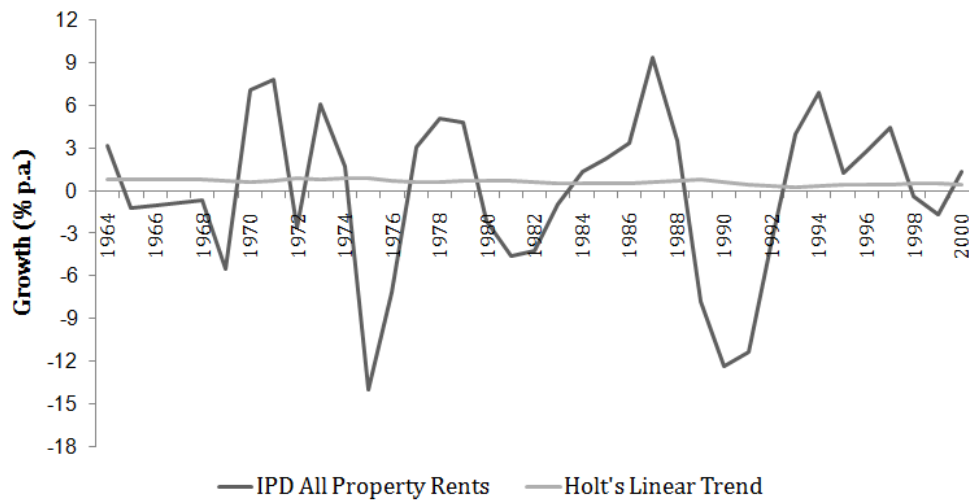


Figure 5.2 Holt's Linear Trend (model fit)

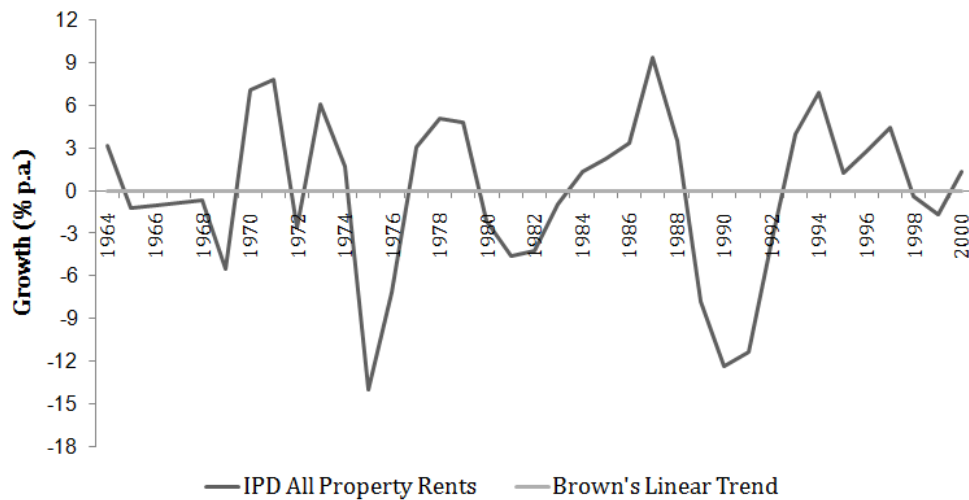


Figure 5.3 Brown's Linear Trend (model fit)

5.1.2 ARIMA/ARIMAX model estimates

To create both ARIMA and ARIMAX specifications, the same PASW 18 'Time Series Modeller' algorithm is employed. The study computes twenty ARIMA specifications ranging from ARIMA (1,0,0) to ARIMA (4,0,4) . As it was commented in Section 3.4.4, ARIMA(X) models can have any AR and MA orders. However, it was decided to select 4th as the largest ARIMA order as greater number would contain the dynamics of the previous business/property cycle.

Table 5.2 provides the ARIMA modelling estimates. As it is seen, there is no consensus between model accuracy measures which ARIMA specification fits the dependent variable best. The R-squared and MSE values indicate that ARIMA (4,0,4) is the best fitting specification. While MAE selects ARIMA (4,0,3) and MAPE selects ARIMA (1,0,2) as the most accurate models. However, AICc and BIC values suggest that ARIMA (1,0,2) is the best parameterised ARIMA specification. What is more, this specification has the lowest MAPE value. It all therefore allows to suggest that ARIMA (1,0,2) is the most accurate model amongst competing ARIMA specifications. The second most accurate is ARIMA (4,0,4) model. The least accurate is ARIMA (1,0,0) specification.

| Order of ARIMA terms | Model Fit statistics | | | | | |
|----------------------|----------------------|-------|---------|--------|--------|--------|
| | R-squared | MAE | MAPE | MSE | AICc | BIC |
| 1,0,0 | 0.174 | 3.873 | 108.985 | 25.016 | 125.84 | 129.95 |
| 1,0,1 | 0.412 | 3.137 | 87.215 | 17.791 | 115.64 | 120.83 |
| 1,0,2 | 0.517 | 2.601 | 66.035 | 14.612 | 109.85 | 115.97 |
| 1,0,3 | 0.527 | 2.605 | 68.624 | 14.308 | 112.91 | 119.77 |
| 1,0,4 | 0.529 | 2.582 | 69.369 | 14.266 | 115.62 | 123.03 |
| 2,0,0 | 0.333 | 3.280 | 94.895 | 20.188 | 120.43 | 125.63 |
| 2,0,1 | 0.425 | 3.068 | 83.969 | 17.417 | 117.65 | 123.77 |
| 2,0,2 | 0.533 | 2.615 | 71.205 | 14.128 | 112.66 | 119.52 |
| 2,0,3 | 0.560 | 2.563 | 82.892 | 13.317 | 112.30 | 119.71 |
| 2,0,4 | 0.576 | 2.549 | 79.082 | 12.842 | 115.16 | 122.91 |
| 3,0,0 | 0.333 | 3.279 | 94.891 | 20.188 | 123.12 | 129.24 |
| 3,0,1 | 0.455 | 2.965 | 88.829 | 16.505 | 118.33 | 125.19 |
| 3,0,2 | 0.549 | 2.529 | 73.182 | 13.648 | 114.28 | 121.69 |
| 3,0,3 | 0.564 | 2.510 | 75.860 | 13.202 | 116.33 | 124.07 |
| 3,0,4 | 0.559 | 2.567 | 72.258 | 13.349 | 119.00 | 126.84 |
| 4,0,0 | 0.529 | 2.794 | 100.710 | 14.266 | 113.08 | 119.95 |
| 4,0,1 | 0.529 | 2.796 | 99.968 | 14.259 | 116.13 | 123.55 |
| 4,0,2 | 0.574 | 2.542 | 81.733 | 12.893 | 115.28 | 123.02 |
| 4,0,3 | 0.578 | 2.470 | 79.555 | 12.783 | 118.51 | 126.34 |
| 4,0,4 | 0.589 | 2.521 | 80.768 | 12.451 | 121.49 | 129.14 |

Table 5.2 ARIMA model fit statistics

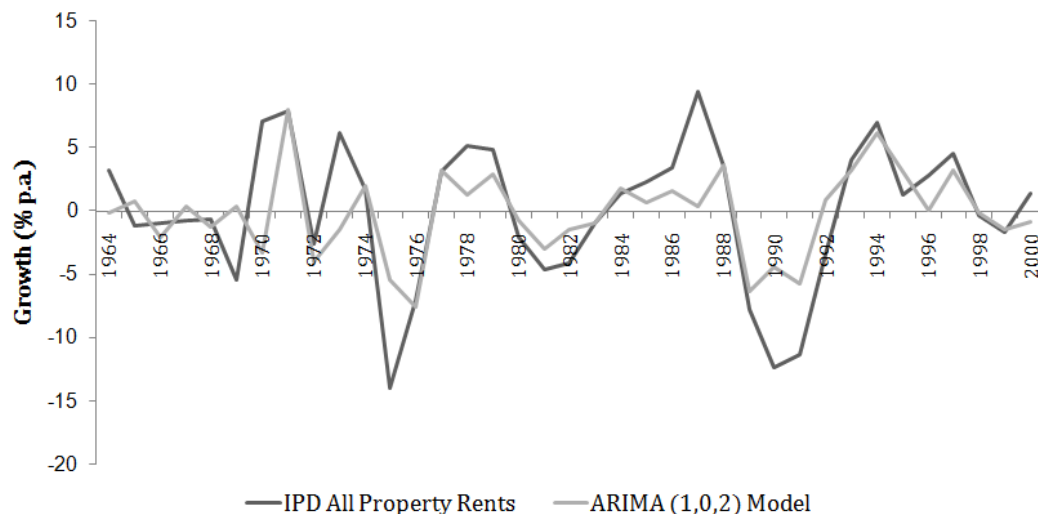


Figure 5.4 ARIMA (1,2) (model fit)

Figure 5.4 illustrates that ARIMA (1,0,2) model fits rental series. It does pick up upturn/downturn in the 1970's, property slump in the early 1990s and market correction in late 1990's. Certainly, model under-estimate decline in 1970s, 1990s and increase in late 1980's. It therefore indicates that the model is optimistic and avoids high deviations in the series. However, considering that the dependent variable is in the state of stationarity, the R-squared of 0.517 suggests that model explains more than half of the deviations in the series.

The subsequent statistics presented in Table 5.3 and Table 5.4 indicates that of all one hundred and forty ARIMAX specifications, the ARIMAX GDP (4,0,0) model has the best statistical properties. The model has the smallest AICc and BIC values. It also fits the historic series best. The second best is ARIMA (1,0,2) model with Construction Orders as an explanatory variable. The least accurate in fitting the dependent variable is ARIMA (1,0,2) specification with Employment as an explanatory variable. Although this specification performed the lest in comparison to other ARIMAX models, its in-sample fit is greater than half ARIMA specifications and of all Exponential Smoothing models.

| Explanatory Variable | ARIMAX Order | Model Fit statistics | | | | | |
|----------------------|--------------|----------------------|-------|--------|--------|--------|--------|
| | | R-squared | MAE | MAPE | MSE | AICc | BIC |
| Bank Rate | (1,0,2) | 0.521 | 2.582 | 66.398 | 14.503 | 112.32 | 119.19 |
| Construction Costs | (1,0,2) | 0.520 | 2.612 | 66.688 | 14.534 | 112.46 | 119.33 |
| Construction Orders | (1,0,2) | 0.604 | 2.608 | 80.827 | 12.208 | 103.24 | 109.85 |
| Construction Output | (1,0,2) | 0.517 | 2.597 | 65.486 | 14.610 | 112.66 | 119.52 |
| Construction Starts | (1,0,2) | 0.523 | 2.602 | 67.448 | 14.454 | 112.27 | 119.14 |
| Employment | (1,0,2) | 0.515 | 2.597 | 66.645 | 14.679 | 112.90 | 119.77 |
| GDP | (4,0,0) | 0.690 | 2.261 | 69.831 | 9.387 | 99.09 | 106.50 |

Table 5.3 ARIMAX model fit statistic

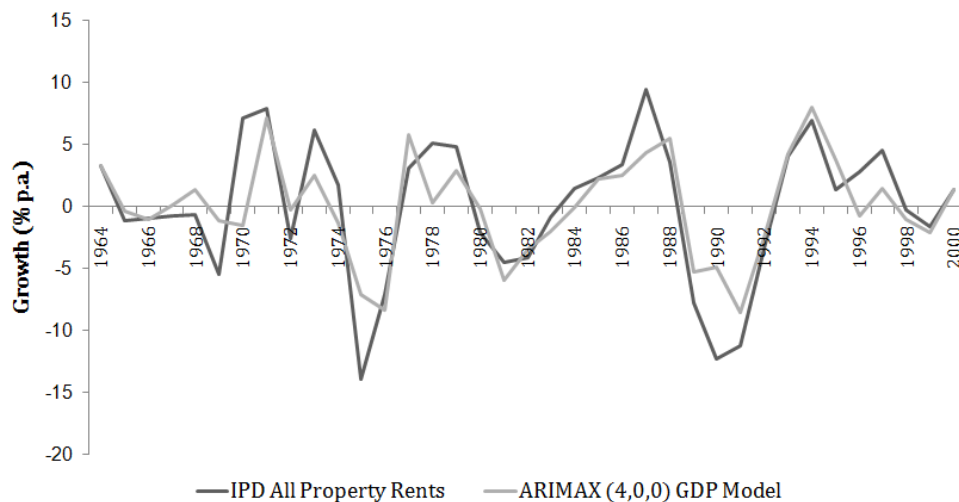


Figure 5.5 ARIMAX (4,0,0) GDP (model fit)

As both statistical and visual analysis suggest, ARIMAX (4,0,0) GDP specification fits rental series better than ARIMA (1,0,2) model. The ARIMAX (4,0,0) GDP model has greater R-squared, smaller MAPE, MSE and AIC values. As can be seen from Figure 5.5, the model tracks the dynamics of the dependent variable. It fits market correction in the 1970's, property slump in the early 1990s and that in late 1990's. It overestimates market rise in the 1978 and underestimates market decline in the 1990. However, it does perform better than the best ARIMA specification.

| ARIMAX Order | Model Fit statistics | | | | | | | | | | | | | |
|-----------------|----------------------|--------|------------------------|--------|-----------------------|--------|------------------------|--------|------------------------|--------|------------|--------|--------|--------|
| | Bank Rate | | Construction Orders | | Construction Costs | | Construction Output | | Construction Starts | | Employment | | GDP | |
| | AICc | BIC | AICc | BIC | AICc | BIC | AICc | BIC | AICc | BIC | AICc | BIC | AICc | BIC |
| 1,0,0 | 128.17 | 133.37 | 115.83 | 120.88 | 128.32 | 133.51 | 128.12 | 133.31 | 128.26 | 133.45 | 126.53 | 131.72 | 117.95 | 123.14 |
| 1,0,1 | 118.16 | 124.27 | 108.06 | 113.98 | 117.91 | 124.03 | 118.03 | 124.15 | 117.66 | 123.78 | 117.95 | 124.06 | 107.88 | 114.00 |
| 1,0,2 | 112.32 | 119.19 | 103.24 | 109.85 | 112.46 | 119.33 | 112.66 | 119.52 | 112.27 | 119.14 | 112.90 | 119.76 | 100.73 | 107.60 |
| 1,0,3 | 115.68 | 123.09 | 106.29 | 113.37 | 115.74 | 123.15 | 115.95 | 123.37 | 115.55 | 122.96 | 116.97 | 124.38 | 111.33 | 118.75 |
| 1,0,4 | 118.52 | 126.27 | 109.33 | 116.67 | 118.74 | 126.48 | 118.93 | 126.68 | 118.47 | 126.22 | 119.10 | 126.84 | 103.50 | 111.25 |
| 2,0,0 | 121.61 | 127.73 | 112.14 | 118.05 | 123.00 | 129.12 | 122.60 | 128.72 | 122.82 | 128.93 | 121.24 | 127.36 | 111.54 | 117.66 |
| 2,0,1 | 120.20 | 127.07 | 110.17 | 116.77 | 118.05 | 124.92 | 118.14 | 125.01 | 118.08 | 124.94 | 115.81 | 122.67 | 107.36 | 114.23 |
| 2,0,2 | 114.35 | 121.76 | 106.61 | 113.70 | 115.27 | 122.68 | 116.76 | 124.18 | 115.18 | 122.59 | 116.44 | 123.86 | 105.53 | 112.95 |
| 2,0,3 | 116.12 | 123.87 | 109.68 | 117.01 | 119.39 | 127.14 | 113.30 | 121.04 | 118.84 | 126.59 | 116.05 | 123.80 | 110.01 | 117.76 |
| 2,0,4 | 118.20 | 126.03 | 111.50 | 118.83 | 118.57 | 126.40 | 118.59 | 126.42 | 118.32 | 126.15 | 118.62 | 126.45 | 103.68 | 111.51 |
| 3,0,0 | 124.43 | 131.30 | 115.01 | 121.61 | 125.86 | 132.73 | 125.46 | 132.32 | 125.67 | 132.54 | 124.05 | 130.91 | 113.22 | 120.09 |
| 3,0,1 | 119.99 | 127.40 | 112.64 | 119.73 | 122.81 | 130.22 | 121.30 | 128.71 | 121.20 | 128.61 | 118.82 | 126.24 | 110.33 | 117.74 |
| 3,0,2 | 116.73 | 124.47 | 109.54 | 116.88 | 117.63 | 125.37 | 117.38 | 125.13 | 117.06 | 124.80 | 118.49 | 126.24 | 106.97 | 114.71 |
| 3,0,3 | 119.81 | 127.64 | 114.22 | 121.55 | 119.46 | 127.29 | 119.12 | 126.95 | 119.47 | 127.31 | 123.04 | 130.87 | 104.49 | 112.32 |
| 3,0,4 | 122.40 | 130.05 | 115.49 | 122.53 | 122.71 | 130.36 | 124.46 | 132.10 | 121.65 | 129.30 | 123.37 | 131.02 | 110.36 | 118.00 |
| 4,0,0 | 114.78 | 122.20 | 106.24 | 113.33 | 116.14 | 123.55 | 115.94 | 123.36 | 115.58 | 122.99 | 116.06 | 123.48 | 99.09 | 106.50 |
| 4,0,1 | 118.06 | 125.80 | 109.42 | 116.75 | 119.41 | 127.15 | 119.22 | 126.97 | 118.31 | 126.05 | 119.34 | 127.09 | 101.32 | 109.06 |
| 4,0,2 | 116.30 | 124.13 | 111.56 | 118.89 | 118.56 | 126.39 | 118.08 | 125.91 | 118.25 | 126.08 | 118.80 | 126.63 | 104.21 | 112.04 |
| 4,0,3 | 119.90 | 127.55 | 116.29 | 123.32 | 122.12 | 129.77 | 121.94 | 129.59 | 121.61 | 129.25 | 122.54 | 130.19 | 108.94 | 116.59 |
| 4,0,4 | 123.84 | 131.00 | 120.70 | 127.12 | 124.75 | 131.91 | 124.62 | 131.78 | 124.74 | 131.90 | 125.78 | 132.94 | 111.70 | 118.86 |

Table 5.4 AICc estimates for ARIMAX models

5.1.3 Simple Regression model estimates

The Simple Regression specifications are computed using PASW 'Regression' algorithm. The modelling is performed using Equation 15 as indicated in Section 3.4.6. Seven simple regression specifications are estimated using seven explanatory variables.

As the statistical analysis suggests (Table 5.5), Construction Orders is the best explanatory variable for simple regression framework. Although a GDP based model has the smallest MAE value, the Construction Orders based model has the smallest AICc and BIC values amongst competing specifications. The model also has the smallest MSE and the greatest R-squared values. What is more, Durbin-Watson statistics for the Construction Orders specification is 1.543 which indicates positive statistical outcomes. The White's test value WT is 2.005 which is less than χ^2 (5.991)⁴. Therefore, the hypothesis of Heteroskedasticity is rejected. It implies that test did not find a problem with Construction Orders based Simple Regression model.

| Explanatory Variable | Model Fit statistics | | | | | |
|----------------------|----------------------|-------|---------|--------|--------|--------|
| | R-squared | MAE | MAPE | MSE | AICc | BIC |
| Bank Rate | 0.001 | 4.333 | 98.261 | 30.246 | 130.47 | 134.47 |
| Construction Costs | 0.000 | 4.362 | 98.859 | 30.259 | 130.49 | 134.49 |
| Construction Orders | 0.339 | 3.737 | 142.379 | 20.374 | 115.26 | 119.27 |
| Construction Output | 0.015 | 4.526 | 108.083 | 33.662 | 129.94 | 133.94 |
| Construction Starts | 0.001 | 4.346 | 97.929 | 30.237 | 130.46 | 134.46 |
| Employment | 0.031 | 4.092 | 87.638 | 29.329 | 129.36 | 133.37 |
| GDP | 0.322 | 3.631 | 120.185 | 20.516 | 118.50 | 122.61 |

Table 5.5 Simple Regression model fit statistics

The principle equation for Simple Regression model with Construction Orders as an explanatory variable is as follows:

$$R_t = \alpha + \beta COr_t + e_t \quad (47)$$

⁴ χ^2 values are obtained from the University of North Carolina at Chapel Hill (2012)

Where R_t is All Property Rental Index at a time t and $CO r_t$ is the Construction Orders series at the period time t . The estimated regression equation between dependent and explanatory variables over the sample period is:

$$R_t = \hat{\alpha} + \hat{\beta}CO r_t = -0.471 + 0.001CO r_t \quad (48)$$

(0.549) (0.0002)

The coefficients α and β are OLS estimates.

The equation above indicates coefficient β to be positive. It implies that when $CO r_t$ is growing, rents are also expected to grow. However, from the visual analysis (Figure 5.6) it is seen that there are periods of inverse relationship between the two series (e.g. 1981). It thus suggests that the positive relationship between dependent and explanatory variables is expected to proceed for most of the time; however, not necessarily through all the period. The value of the coefficient β can be interpreted as following: change in $CO r_t$ by 1 will make R_t change positively by 0.001 percentage points, *ceteris paribus*. The equation also implies that when $CO r_t$ remains 0, R_t will fall by 0.471 percent, *ceteris paribus*. However, in reality when $CO r_t$ increases by 1, R_t will not always increase by 0.001 percent, and when $CO r_t$ remain flat, R_t will not necessarily decline by 0.471. This is because other factors, which are defined as e , do not remain constant over time.

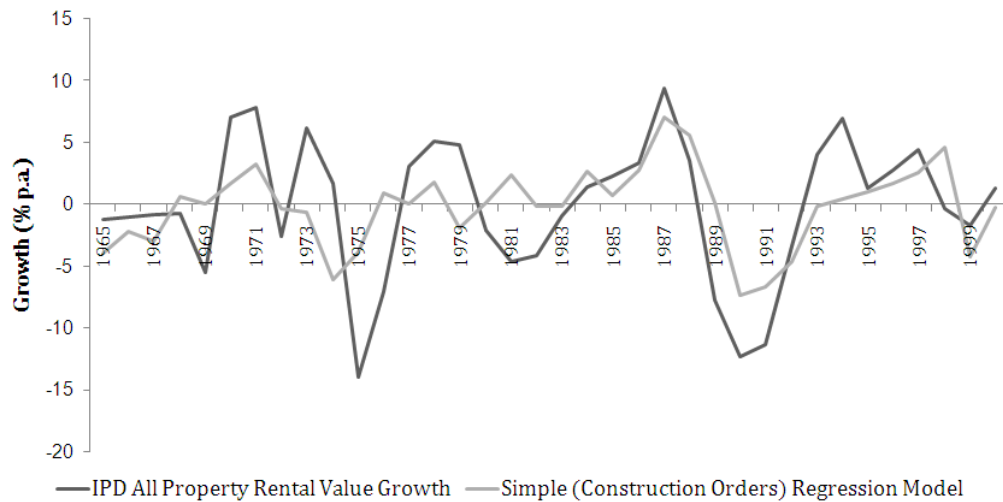


Figure 5.6 Simple Regression (Construction Orders) (model fit)

The subsequent analysis of the dynamics of the Simple Regression model with Construction Orders as an explanatory variable (Figure 5.6) suggests that the model does not track the dependent variable well. This can be explained by the low value of its R-squared (0.339). Certainly, there are periods when the model captures the deviations in the dependent variable. However, overall, its explanatory power is low. The model under-estimates the dependent variable when rents are rising and it avoids high values during when rents are declining.

5.1.4 Multiple Regression model estimates

The subsequent regression analysis (based on P-values and t-statistics) suggests Construction Output (COu_t), Construction Starts (CSt_t), Construction Orders (COr_t), and Gross Domestic Product (GDP_t) to be significant in modelling property rents (Table 5.6). Neither Employment, nor Bank Rate came up as being useful in modelling Real Estate rents within Multiple Regression Framework. It was therefore decided to drop the latter two variables out of the equation as they convey irrelevant information.

| Explanatory variables | Coefficient | t-Stat | P-value |
|-----------------------|-------------|--------|---------|
| Constant | -4.399 | -2.989 | 0.006 |
| Construction Output | -0.001 | -2.177 | 0.038 |
| Construction Costs | 0.228 | 0.161 | 0.073 |
| Construction Starts | 0.000 | 2.552 | 0.016 |
| Construction Orders | 0.001 | 3.003 | 0.006 |
| GDP | 1.560 | 2.935 | 0.007 |
| Employment | 0.003 | 0.824 | 0.417 |
| Bank Rate | 0.310 | 0.630 | 0.534 |

Table 5.6 Regression estimates for MR equation

Accordingly, Multiple Regression equation derived from the relationship between dependent and explanatory variables is as follows:

$$R_t = \alpha + \beta_1 COu_t + \beta_2 CCs_t + \beta_3 CSt_t + \beta_4 COr_t + \beta_5 GDP_t e_t \quad (49)$$

$$R_t = -4.144 - 0.001COu_t + 1.211CCs_t + 0.0010CSt_t + \quad (50)$$

$$(0.002) \quad (0.047) \quad (0.270) \quad (0.016)$$

$$+0.001COr_t + 1.8134GDP_t + e_t$$

$$(0.008) \quad (0.001)$$

As the statistical results suggest, the model tracks property rents. Given the fact that changes of the rental series are modelled, the R-squared of 0.553 indicates that the model explains more than half of the deviations in the dependent variable. The model captures market upturn and downturn in late 1980s/early 1990s, as well as tracks subsequent market movements (Figure 5.7).

The DW statistical value for Multiple Regression is 1.709. It suggests that autocorrelated disturbances are not present within the model, i.e. that values are independent. White's test for this specification is computed following the same algorithm as that for Simple Regression models. The WT value (5.04) is less than $\chi^2(18.307)$. Therefore, the hypothesis of Heteroskedasticity can be rejected.

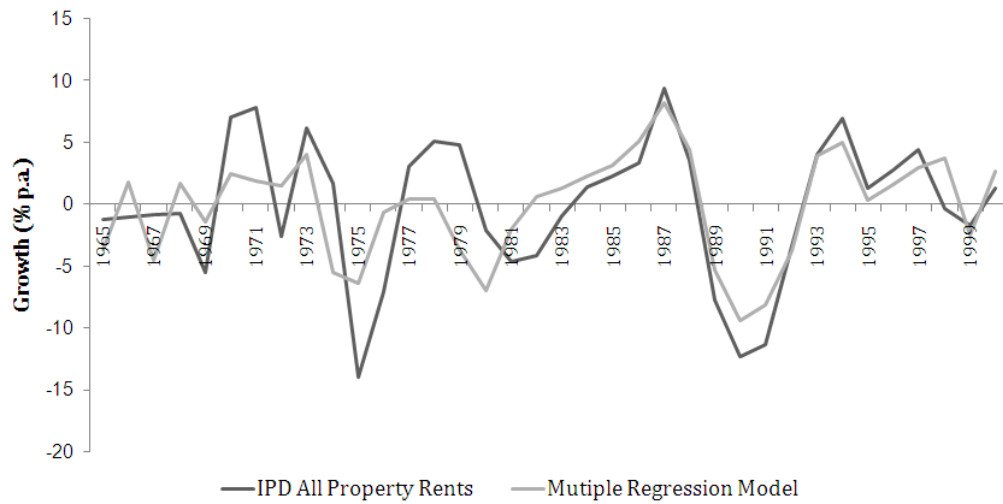


Figure 5.7 Multiple Regression (model fit)

5.1.5 Vector Autoregression model estimates

The Vector Autoregression modelling is performed following Equation 21 presented in Section 3.4.8. In this framework, the same lag length is used for every variable in every equation, i.e. $p=q$, subsequently creating VAR (p) model. Since all variables selected for the model are stationary, model estimation and testing are performed in the standard way. Estimates for each equation are obtained using OLS (Table 5.7). Acquired figures for P-values and t-statistics then indicate whether variables are significant. Lag length is selected from AICc for each system as suggested by Brooks and Tsolacos (2010). Accordingly, the best VAR specification is VAR (1)⁵:

$$\begin{aligned}
 R_t = & -2.578 + 0.055R_{t-1} - 0.001COu_{t-1} - 2.349CCs_{t-1} + & (51) \\
 & (0.154) \quad (0.807) \quad (0.097) \quad (0.085) \\
 & +0.00003CSt_{t-1} + 0.001COr_{t-1} + 1.336GDP_{t-1} + e_t \\
 & (0.436) \quad (0.249) \quad (0.078)
 \end{aligned}$$

⁵ AICc for VAR (3) is 102.60, VAR (2) is 103.58 and VAR (1) is 85.180

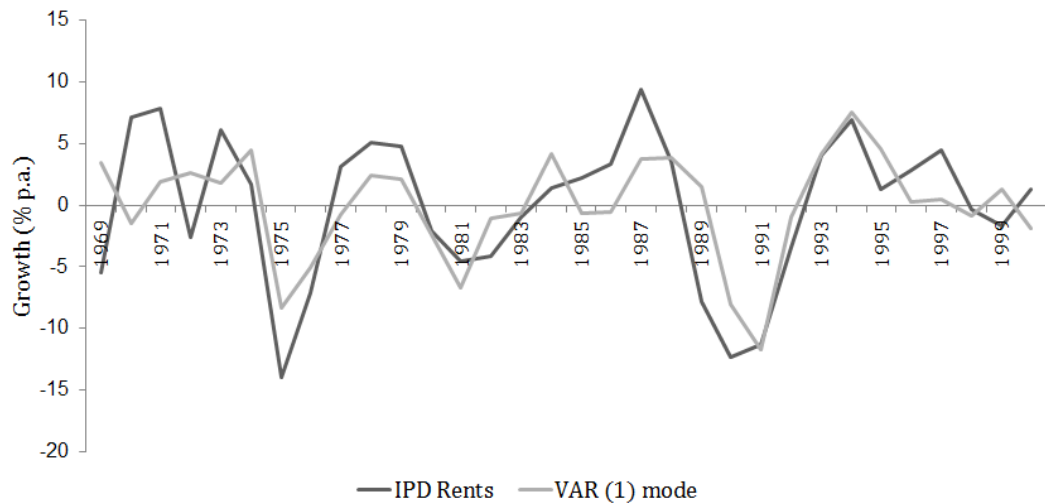


Figure 5.8 Vector Autoregression (model fit)

As it is seen from Figure 5.8 above, the model tracks historic rent series with its R-square being 0.793. The model picks up the main ups and downs in the dependent variable. However, there are periods when the model underestimates the dynamics of the dependent variable. The model does not pick up market rise in early-1970s and late-1980s. It also produces inverse estimates during a three year period from 1984 to 1886.

Regardless of these limitations, model is well parameterised. Its DW statistics is 1.545. White's test indicates that there are no difficulties associated with the specification. Its n is 32, R-squared is 1, with WT being equal to 32, which is less than χ^2 (53.384).

The following section presents out-of-sample accuracy of these models.

| Equation in VAR | | | | | | | | |
|-----------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|-------------------|
| | R_t | COu_t | CCs_t | CSt_t | COr_t | GDP_t | E_t | BR_t |
| Constant | -7.094 (0.183) | -274.5 (0.669) | -0.352 (0.616) | 28147 (0.349) | 454.7 (0.785) | 0.196 (0.888) | -72.93 (0.683) | -1.361 (0.326) |
| R_{t-1} | -0.358 (0.528) | -51.67 (0.479) | 0.094 (0.254) | 2434 (0.465) | -45.85 (0.807) | -0.282 (0.103) | 2.723 (0.891) | -0.055 (0.717) |
| R_{t-2} | -0.504 (0.457) | -28.11 (0.742) | 0.027 (0.775) | -3722 (0.353) | 135.2 (0.549) | 0.166 (0.385) | -10.16 (0.670) | 0.318 (0.108) |
| R_{t-3} | -0.772 (0.380) | 79.00 (0.478) | 0.225 (0.092) | 2541 (0.614) | -231.9 (0.428) | -0.241 (0.330) | 47.19 (0.152) | 0.075 (0.745) |
| COu_{t-1} | -0.002 (0.410) | 0.041 (0.912) | 0.000 (0.945) | 14.91 (0.386) | 0.788 (0.422) | -0.001 (0.417) | -0.048 (0.643) | 0.000 (0.709) |
| COu_{t-2} | -0.003 (0.269) | 0.066 (0.843) | 0.000 (0.336) | -14.03 (0.368) | 0.625 (0.479) | 0.000 (0.659) | -0.005 (0.960) | 0.000 (0.936) |
| COu_{t-3} | -0.001 (0.619) | -0.231 (0.327) | 0.000 (0.841) | 15.16 (0.173) | -0.781 (0.215) | 0.000 (0.795) | -0.010 (0.876) | 0.000 (0.753) |
| CCs_{t-1} | -0.688 (0.830) | -527.7 (0.225) | -0.490 (0.295) | -11542 (0.544) | -1832 (0.120) | 0.043 (0.962) | -69.29 (0.550) | -0.855 (0.338) |
| CCs_{t-2} | 3.972 (0.396) | -911.4 (0.150) | -0.964 (0.161) | 6763 (0.800) | -1553 (0.327) | 1.121 (0.392) | -202.6 (0.238) | -0.467 (0.704) |
| CCs_{t-3} | 1.580 (0.709) | -604.0 (0.285) | -0.629 (0.306) | -11545 (0.642) | -1431 (0.328) | 0.718 (0.548) | -113.9 (0.459) | 0.895 (0.441) |
| CSt_{t-1} | 0.000 (0.397) | 0.001 (0.921) | 0.000 (0.483) | -0.071 (0.862) | 0.013 (0.575) | 0.000 (0.047) | -0.002 (0.500) | 0.000 (0.264) |
| CSt_{t-2} | 0.000 (0.956) | -0.001 (0.943) | 0.000 (0.852) | 0.017 (0.968) | -0.011 (0.653) | 0.000 (0.870) | 0.004 (0.180) | 0.000 (0.158) |
| CSt_{t-3} | 0.000 (0.630) | 0.009 (0.356) | 0.000 (0.220) | -0.049 (0.910) | 0.024 (0.344) | 0.000 (0.343) | -0.001 (0.592) | 0.000 (0.318) |
| COr_{t-1} | 0.002 (0.154) | 0.345 (0.106) | 0.000 (0.469) | -0.993 (0.910) | 0.413 (0.424) | 0.001 (0.213) | -0.052 (0.351) | 0.000 (0.565) |
| COr_{t-2} | 0.001 (0.592) | 0.495 (0.058) | 0.000 (0.675) | 0.173 (0.987) | 0.233 (0.695) | 0.000 (0.761) | 0.034 (0.589) | 0.000 (0.314) |
| COr_{t-3} | 0.001 (0.465) | -0.173 (0.504) | 0.000 (0.430) | -6.172 (0.599) | -0.567 (0.407) | 0.000 (0.652) | -0.016 (0.817) | 0.000 (0.538) |
| GDP_{t-1} | 1.618 (0.350) | -72.70 (0.736) | -0.122 (0.607) | -3724 (0.705) | 340.5 (0.549) | 0.854 (0.101) | 54.095 (0.380) | 0.399 (0.390) |
| GDP_{t-2} | -0.343 (0.872) | -62.44 (0.819) | 0.228 (0.453) | 2900 (0.816) | -1389 (0.083) | -0.320 (0.594) | 128.4 (0.124) | -0.182 (0.752) |
| GDP_{t-3} | 2.846 (0.207) | 112.7 (0.681) | -0.390 (0.216) | -1743 (0.888) | 858.7 (0.251) | 0.534 (0.382) | -78.03 (0.321) | -0.163 (0.776) |
| E_{t-1} | 0.000 (0.971) | 0.570 (0.691) | 0.001 (0.519) | -27.87 (0.670) | 5.284 (0.185) | 0.001 (0.738) | 0.022 (0.955) | 0.003 (0.404) |
| E_{t-2} | -0.020 (0.137) | 0.952 (0.560) | 0.002 (0.256) | -19.33 (0.793) | -8.096 (0.087) | -0.003 (0.451) | 0.765 (0.121) | 0.003 (0.386) |
| E_{t-3} | 0.012 (0.285) | 0.736 (0.582) | 0.001 (0.475) | -52.59 (0.396) | 4.692 (0.202) | 0.001 (0.671) | -0.077 (0.836) | -0.002 (0.396) |
| BR_{t-1} | 0.735 (0.652) | -184.7 (0.386) | -0.291 (0.224) | 8847 (0.364) | 0.327 (1.000) | -0.103 (0.821) | -82.44 (0.183) | -0.491 (0.280) |
| BR_{t-2} | 0.735 (0.636) | 341.6 (0.116) | -0.160 (0.466) | 7847 (0.396) | 1800 (0.009) | -0.160 (0.711) | 0.124 (0.998) | -0.648 (0.149) |
| BR_{t-3} | -1.917 (0.300) | -55.49 (0.808) | 0.059 (0.813) | 113.7 (0.991) | -261.5 (0.663) | -0.255 (0.611) | 81.88 (0.223) | -1.361 (0.932) |
| R^2 | 0.880 | 0.976 | 0.866 | 0.869 | 0.922 | 0.922 | 0.927 | 0.926 |

Table 5.7 Estimates from VAR (p) specification
(P-values in parentheses)

5.2 Out-of-sample forecasting estimates

As the statistical results indicate (Table 5.8), the VAR (1) specification is the best fitting model. Its R-squared is the greatest of all sample models. The AICc also indicate it to be the best parameterised model. In the in-sample, VAR model outperforms all one hundred and seventy one specification computed for the current research. However, these results do not come as a surprise. The VAR model comprises a number of explanatory variables (i.e. Construction Output, Construction Costs, Construction Starts, Construction Orders and GDP), their lagged values as well as past values of dependent variable itself. It therefore justifies its goodness to fit to the historic data.

| Model Specification | Model Fit statistics | | | | | | |
|------------------------------|----------------------|-------|---------|--------|--------|--------|-------|
| | R-squared | MAE | MAPE | MSE | AICc | BIC | U |
| Exponential Smoothing | | | | | | | |
| Single exponential smoothing | -0.027 | 4.399 | 109.261 | 18.143 | 130.87 | 134.97 | 0.940 |
| Holt's Linear Trend | -0.027 | 4.390 | 110.323 | 18.351 | 131.15 | 135.26 | 0.928 |
| Brown's Linear Trend | -0.001 | 4.358 | 100.240 | 17.486 | 131.23 | 135.33 | 0.999 |
| Simple Regression | | | | | | | |
| Bank Rate | 0.001 | 4.333 | 98.261 | 16.824 | 130.47 | 134.47 | 0.953 |
| Construction Costs | 0.000 | 4.362 | 98.859 | 19.821 | 130.49 | 134.49 | 0.968 |
| Construction Orders | 0.339 | 3.737 | 142.379 | 19.280 | 115.26 | 119.27 | 0.405 |
| Construction Output | 0.015 | 4.526 | 108.083 | 31.531 | 129.94 | 133.94 | 0.879 |
| Construction Starts | 0.001 | 4.346 | 97.929 | 16.550 | 130.46 | 134.46 | 0.934 |
| Employment | 0.031 | 4.092 | 87.638 | 18.689 | 129.36 | 133.37 | 0.824 |
| GDP | 0.322 | 3.631 | 120.185 | 14.812 | 118.50 | 122.61 | 0.466 |
| Multiple Regression | 0.553 | 3.061 | 141.647 | 30.962 | 109.35 | 115.95 | 0.461 |
| Vector Autoregression | 0.793 | 2.474 | 91.845 | 12.230 | 85.180 | 122.06 | 0.481 |
| ARIMA (1,0,2) | 0.517 | 2.601 | 66.035 | 17.433 | 109.85 | 115.97 | 0.848 |
| ARIMAX | | | | | | | |
| Bank Rate (1,0,2) | 0.521 | 2.582 | 66.398 | 16.363 | 112.32 | 119.19 | 0.822 |
| Construction Costs (1,0,2) | 0.520 | 2.612 | 66.688 | 14.584 | 112.46 | 119.33 | 0.736 |
| Construction Orders (1,0,2) | 0.604 | 2.608 | 80.827 | 6.770 | 103.24 | 109.85 | 0.328 |
| Construction Output (1,0,2) | 0.517 | 2.597 | 65.486 | 17.273 | 112.66 | 119.52 | 0.839 |
| Construction Starts (1,0,2) | 0.523 | 2.602 | 67.448 | 16.229 | 112.27 | 119.14 | 0.828 |
| Employment (1,0,2) | 0.515 | 2.597 | 66.645 | 17.183 | 112.90 | 119.77 | 0.836 |
| GDP (4,0,0) | 0.690 | 2.261 | 69.831 | 10.050 | 99.09 | 106.50 | 0.433 |

Table 5.8 Summary model fit statistics

However, when it comes to out-of-sample forecasting performance, VAR's accuracy is not so impressive. Its Theil's U value is poorer than that of some less complex ARIMAX and Simple Regression models.

Regarding Exponential Smoothing specifications, their accuracy remained low in and out-of-sample. All three specifications had their U values close to one. Interestingly, similar estimates were obtained for ARIMA models. Theil's U value for the best fitting ARIMA (1,0,2) model was also close to one.

Table 5.9 reports that ARIMAXCOR (1,0,2) specification has the lowest Theil's U value of all the candidate models. This subsequently makes it the best performing specification. Interestingly, in both cases (in- and out-of-sample) simple models and ARIMAX specifications in particular generated better results than more complex Multiple Regression and VAR specifications.

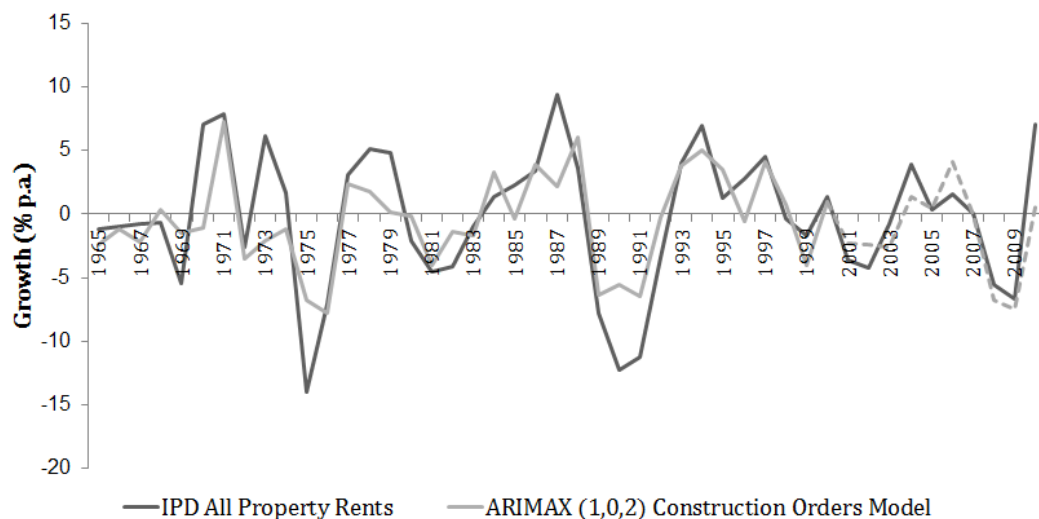


Figure 5.9 ARIMAX (1,0,2) Construction Orders (fit and accuracy)

The second most accurate of all sample models is Simple Regression specification with Construction Orders (SRCOr) as an explanatory variable, following ARIMAX GDP (4,0,0) (ARIMAXGDP) models. ARIMAXGPD model is effective within in-sample and out-of-sample forecasting. Although ARIMAXCOR, ARIMAXGDP or SRCOr models do not fit the historic series with the same degree of accuracy as it does VAR

or Multiple Regression specifications, their out-of-sample performance is better. These estimates also suggest that past values of rents itself, as well as change in Construction Orders and GDP are the most important explanatory variables to model IPD All Property Rent Index. These findings reinforce arguments presented in Section 4.4.3, where it was commented that the latter explanatory variables relate to the dynamics of the commercial property rental cycle.

Having discusses in- and out-of-sample modelling accuracy, the next section presents estimates of the Combination Forecasting.

5.3 Combination Forecasting estimates

The Combination Forecasting is produced using two principle techniques, i.e. Simple Averaging (SA) and Regression (OLS) combination. Simple Averaging is computed using Equation 22. The Regression based Combination Forecasting is estimated using Equation 23 (Section 3.4.9). The combination forecasts are produced for the 2001-2010 period with 380 combination forecasts computed in total, i.e. 190 Simple and 190 OLS. The accuracy of each combination is assessed by computing their Theil's U statistical values.

As the modelling results indicate (Table 5.9 below), the best SA Combination Forecasts are obtained from the combination of Simple Regression and ARIMAX models, which were based on construction and GDP based series. Theil's U statistic for these particular combinations is 0.35 which indicates good forecasting ability. The best OLS Combination Forecasts are obtained by combining ARIMAX and Simple Regression specifications which were computed using Construction related, Employment, and Bank Rate series. Theil's U statistic of these specifications is 0.32.

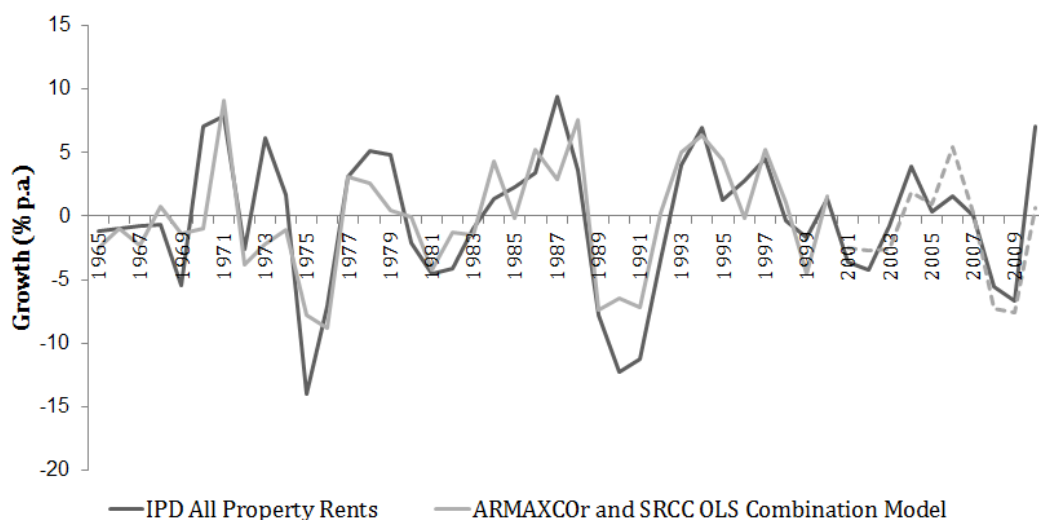


Figure 5.10 ARIMAXCOr and SRCCs OLS Combination (fit and accuracy)

Figure 5.10 above presents ARIMAXCOr and SRCCs OLS Combination model. As it is seen, this specification accurately tracks series in the out-of-sample.

Certainly, model over-estimates rental growth in 2006. Nevertheless, it pick-ups market decline in 2008 and subsequent correction in 2009 and 2010 well. Overall, model tracks dynamics of the dependent variable which subsequently makes it the best performing specification.

The following section comments on forecasting (in)accuracy in more details. It then discusses issues related to model fit, forecasting performance and increased model complexity and how it all relates to overall modelling results.

| | SES | HES | BES | ARIMA | ARIMAX (BR) | ARIMAX (CCs) | ARIMAX (COr) | ARIMAX (COu) | ARIMAX (CSt) | ARIMAX (E) | ARIMAX (GDP) | SR (BR) | SR (CCs) | SR (COr) | SR (COu) | SR (CSt) | SR (E) | SR (GDP) | MR | VAR |
|-------------|------|------|------|-------|----------------|-----------------|-----------------|-----------------|-----------------|---------------|-----------------|------------|-------------|-------------|-------------|-------------|-----------|-------------|------|-----|
| SES | - | | | | | | | | | | | | | | | | | | | |
| HES | 0.93 | - | | | | | | | | | | | | | | | | | | |
| | 0.72 | | | | | | | | | | | | | | | | | | | |
| BES | 0.97 | 0.96 | - | | | | | | | | | | | | | | | | | |
| | 0.67 | 0.89 | | | | | | | | | | | | | | | | | | |
| ARIMA | 0.93 | 0.94 | 0.91 | - | | | | | | | | | | | | | | | | |
| | 0.84 | 0.83 | 0.84 | | | | | | | | | | | | | | | | | |
| ARIMAX(BR) | 0.92 | 0.93 | 0.90 | 0.84 | - | | | | | | | | | | | | | | | |
| | 0.81 | 0.80 | 0.81 | 0.81 | | | | | | | | | | | | | | | | |
| ARIMAX(CCs) | 0.87 | 0.87 | 0.85 | 0.80 | 0.78 | - | | | | | | | | | | | | | | |
| | 0.71 | 0.70 | 0.70 | 0.65 | 0.78 | | | | | | | | | | | | | | | |
| ARIMAX(COr) | 0.49 | 0.49 | 0.49 | 0.48 | 0.47 | 0.44 | - | | | | | | | | | | | | | |
| | 0.32 | 0.33 | 0.34 | 0.32 | 0.32 | 0.32 | | | | | | | | | | | | | | |
| ARIMAX(COu) | 0.93 | 0.93 | 0.91 | 0.84 | 0.83 | 0.79 | 0.48 | - | | | | | | | | | | | | |
| | 0.83 | 0.83 | 0.83 | 0.78 | 0.82 | 0.67 | 0.32 | | | | | | | | | | | | | |
| ARIMAX(CSt) | 0.92 | 0.92 | 0.90 | 0.84 | 0.83 | 0.78 | 0.47 | 0.83 | - | | | | | | | | | | | |
| | 0.81 | 0.80 | 0.80 | 0.82 | 0.82 | 0.78 | 0.32 | 0.83 | | | | | | | | | | | | |
| ARIMAX(E) | 0.92 | 0.93 | 0.91 | 0.84 | 0.83 | 0.79 | 0.48 | 0.84 | 0.83 | - | | | | | | | | | | |
| | 0.83 | 0.83 | 0.83 | 0.85 | 0.75 | 0.70 | 0.32 | 0.84 | 0.82 | | | | | | | | | | | |
| ARIMAX(GDP) | 0.59 | 0.60 | 0.59 | 0.58 | 0.56 | 0.53 | 0.36 | 0.57 | 0.56 | 0.57 | - | | | | | | | | | |
| | 0.42 | 0.42 | 0.42 | 0.42 | 0.42 | 0.42 | 0.36 | 0.42 | 0.42 | 0.42 | | | | | | | | | | |
| SR(BR) | 0.97 | 0.96 | 0.98 | 0.90 | 0.88 | 0.83 | 0.48 | 0.90 | 0.89 | 0.89 | 0.58 | - | | | | | | | | |
| | 0.80 | 0.80 | 0.77 | 0.80 | 0.78 | 0.67 | 0.32 | 0.79 | 0.77 | 0.80 | 0.42 | | | | | | | | | |
| SR(CCs) | 0.97 | 0.97 | 0.98 | 0.93 | 0.92 | 0.89 | 0.51 | 0.93 | 0.93 | 0.93 | 0.62 | 0.98 | - | | | | | | | |
| | 0.66 | 0.71 | 0.72 | 0.90 | 0.88 | 0.89 | 0.32 | 0.89 | 0.89 | 0.90 | 0.67 | 0.93 | | | | | | | | |
| SR(COr) | 0.36 | 0.36 | 0.36 | 0.36 | 0.35 | 0.35 | 0.35 | 0.36 | 0.35 | 0.36 | 0.35 | 0.36 | 0.37 | - | | | | | | |
| | 0.39 | 0.39 | 0.39 | 0.35 | 0.34 | 0.35 | 0.36 | 0.35 | 0.35 | 0.35 | 0.38 | 0.43 | 0.39 | | | | | | | |
| SR(COu) | 0.91 | 0.91 | 0.91 | 0.90 | 0.89 | 0.89 | 0.61 | 0.90 | 0.89 | 0.90 | 0.73 | 0.91 | 0.91 | 0.41 | - | | | | | |
| | 0.64 | 0.66 | 0.67 | 0.66 | 0.62 | 0.56 | 0.33 | 0.65 | 0.62 | 0.65 | 0.42 | 0.70 | 0.86 | 0.40 | | | | | | |
| SR(CSt) | 0.95 | 0.95 | 0.97 | 0.90 | 0.88 | 0.83 | 0.47 | 0.89 | 0.88 | 0.89 | 0.57 | 0.95 | 0.98 | 0.36 | 0.91 | - | | | | |
| | 0.87 | 0.86 | 0.83 | 0.86 | 0.83 | 0.74 | 0.32 | 0.86 | 0.87 | 0.86 | 0.40 | 0.87 | 0.96 | 0.42 | 0.66 | | | | | |
| SR(E) | 0.90 | 0.90 | 0.90 | 0.87 | 0.85 | 0.80 | 0.49 | 0.87 | 0.86 | 0.86 | 0.58 | 0.88 | 0.93 | 0.39 | 0.94 | 0.88 | - | | | |
| | 0.79 | 0.79 | 0.79 | 0.81 | 0.78 | 0.69 | 0.37 | 0.81 | 0.79 | 0.80 | 0.43 | 0.85 | 0.92 | 0.44 | 0.76 | 0.77 | | | | |
| SR(GDP) | 0.56 | 0.56 | 0.56 | 0.55 | 0.54 | 0.52 | 0.38 | 0.55 | 0.54 | 0.55 | 0.45 | 0.55 | 0.58 | 0.38 | 0.69 | 0.55 | 0.56 | - | | |
| | 0.47 | 0.47 | 0.47 | 0.49 | 0.48 | 0.46 | 0.38 | 0.49 | 0.47 | 0.49 | 0.42 | 0.48 | 0.48 | 0.43 | 0.48 | 0.45 | 0.46 | | | |
| MR | 0.36 | 0.36 | 0.36 | 0.36 | 0.36 | 0.36 | 0.37 | 0.36 | 0.36 | 0.37 | 0.38 | 0.36 | 0.37 | 0.43 | 0.40 | 0.36 | 0.40 | 0.41 | - | |
| | 0.46 | 0.46 | 0.46 | 0.39 | 0.38 | 0.40 | 0.41 | 0.38 | 0.39 | 0.39 | 0.41 | 0.48 | 0.53 | 0.46 | 0.46 | 0.46 | 0.49 | 0.46 | | |
| VAR | 0.56 | 0.72 | 0.70 | 0.68 | 0.67 | 0.63 | 0.40 | 0.68 | 0.67 | 0.68 | 0.48 | 0.69 | 0.75 | 0.36 | 0.83 | 0.69 | 0.68 | 0.48 | 0.39 | - |
| | 0.58 | 0.58 | 0.59 | 0.66 | 0.64 | 0.59 | 0.34 | 0.66 | 0.64 | 0.66 | 0.42 | 0.59 | 0.88 | 0.39 | 0.57 | 0.49 | 0.54 | 0.47 | 0.44 | |

Table 5.9 Theil's U statistics for SA and OLS Combination Forecasts

NB: the top number indicates Theil's U value for SA combination; the bottom number indicates Theil's U value for OLS combination

5.4 Overall forecasting accuracy

The current research employed a number of modelling and forecasting techniques to forecast UK commercial property market. As both statistical and visual analyses suggested, none of the Exponential Smoothing models fitted the stationary rental series. The R-squared of each of the specifications was less than 0. Other statistical measures, including MSE and AIC, were also insignificant.

The analysis of ARIMA and ARIMAX model accuracy suggested that ARIMA (1,0,2) was the best fitting specification. There was no consensus between model accuracy measures which ARIMA specification fits the dependent variable best. However, ARIMA (1,0,2) model had the best properties amongst competing specifications and it tracked more than half of the deviations of the dependent variable. The least accurate was ARIMA (1,0,0) specification. Its accuracy was close to that of Exponential Smoothing models. ARIMAX GDP (4,0,0) model was the best performing specification amongst one-hundred-and-forty ARIMAX specification. The model had the highest accuracy estimates and it tracked dependent variable best. The second best specification was ARIMA (1,0,2) model with Construction Orders as an explanatory variable. The least accurate in fitting the dependent variable was ARIMAX (1,0,2) specification with Employment as an explanatory variable. These estimates corroborated earlier observations (see Section 4.4.3) that Construction Orders and GDP are significant in explaining changes in commercial property rents.

In an out-of-sample, the performance of Exponential Smoothing specifications as measured from their U value are as good as guessing or obtained using no change forecast method. Interestingly, similar estimates were obtained for ARIMA models. Theil's U valued for the best fitting ARIMA (1,0,2) model was also close to one. It all therefore adds to the observations noted in Section 2.2.3, that model fit does not guarantee forecasting performance. Regardless that ARIMA (1,0,2) model

successfully tracked around fifty percent of the dynamics of the dependent variable, its application in an out-of-sample forecasting.

In section 2.2.1 it was identified that Exponential Smoothing and ARIMA(X) models are pure time-series specifications. These models are not based upon any underlying economic or financial theory and produce forecasts only capturing empirically relevant properties of selected series. Although they come from the same class of models, their performance in tracking UK commercial property rental index was different. In case of Exponential Smoothing, neither of models performed in capturing dynamics of the dependent variable. The implications are that neither Single Exponential Smoothing, nor Holt's Linear Trend, or Brown's Linear Trend specifications, which isolate trend and seasonality from irregular variations, are applicable for stationary time-series modelling.

The ARIMA and ARIMAX models performed differently. In case of ARIMA models, the estimates advocate for this modelling technique being unsuitable for long-term forecasting purposes. These findings corroborate those noted in the literature on commercial property market modelling and forecasting (Section 2.2.2). However, ARIMAX modelling out-of-sample estimates were different. The ARIMAX specifications, which contained Construction Orders and GDP as explanatory variables, performed well by tracking around seventy percent of dynamics of the dependent variable. These two specifications also performed well in out-of-sample. As it was reported in Section 5.1.2, ARIMAXCor (1,0,2) specification had the lowest Theil's U value of all the candidate models, what made it the best performing specification.

Although it was noted in Section 2.2.2 and current estimates confirmed that ARIMA specifications are applicable only for short-term forecasting purposes only, an introduction of explanatory variable(s) into the framework significantly improved model performance both in- and out-of-sample. In the current research, ARIMA (1,0,2) specification with Construction Orders and GDP as explanatory variables improved ARIMA

(1,0,2) model performance in sample from 0.517 to 0.690 as measured by its R-squared. The out-of-sample model accuracy improved from 0.848 to 0.382 as measured by its U-coefficient. This therefore suggests that econometric specifications which incorporate past estimates of the dependent variable with a vector of key explanatory variable(s) are applicable for UK commercial property rental values forecasting.

In case of regression models, results were not uniform. Seven different Simple Regression specifications were computed using seven explanatory variables including Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment and GDP. The statistical analysis suggested that Construction Orders based specification was the best fitting model. The second best was GDP based model. There were no issues with the way models were parameterised and hypotheses of Heteroskedasticity were rejected. The subsequent analysis of the Construction Orders base Simple Regression model suggested positive interrelationship between dependent and explanatory variables. The equation derived from the regression estimates implied that a rise in Construction Orders by 1 generates 0.001 percentage point increase in Rents with everything else being equal.

However, regardless of the positive interrelationship between dependent and explanatory variables within Simple Regression framework, the general estimates suggested low explanatory power of this type of econometric specifications. The highest fitting Simple Regression specification was able to explain less than forty percent of the dynamics of the dependent variable.

In the out-of-sample, only two Simple Regression specifications were able to track the dependent variable. These models were Simple Regression specification with Construction Orders (SRCOr) and Simple Regression specification with GDP (SRGDP) as explanatory variable. Both models produced 60 percent greater accuracy than estimates obtained by chance. However, other five specifications generated out-of-sample results close to

those of no-change strategy. As afore noted, Construction Orders and GDP were both significant in explaining UK commercial property rental series. However, one variable, regardless of how significant, is not enough to explain deviations in the dependent variable.

The Multiple Regression specification was formulated using five explanatory variables including Construction Output, Construction Costs, Construction Starts, Construction Orders and GDP. The overall performance of the Multiple Regression based model was adequate both in- and out-of-sample. The model explained more than fifty percent of deviations in the dependent variable and produced twice better out-of-sample estimates than the no-change strategy. There were no issues in the way model is parameterised, i.e. autocorrelated disturbances were not present within the model and hypothesis of Heteroskedasticity was rejected.

The comparative analysis of the Multiple Regression model with Exponential Smoothing, Simple Regression and ARIMA(X) specifications suggests that the Multiple Regression model is better than any Exponential Smoothing or Simple Regression specification in explaining UK commercial property rents. The Multiple Regression model has greater in-sample accuracy. However, its statistical estimates are poorer than of some ARIMA and ARIMAX specifications. The Multiple Regression model fit, as expressed by its R-squared value (0.553), is lower than that of ARIMA (4,0,4) model (0.589) and ARIMAX (4,0,0) GDP model (0.690). Nevertheless, the Multiple Regression framework in general proves to be useful in modelling stationary time-series.

The VAR model was the most complex specification of all computed for the current research. It was also the best fitting one. The model explained around eighty percent of the deviations of the dependent variable as expressed by its R-squared. It picked-up the main turning points in the series. Model was also successful in out-of-sample by producing more than twice greater estimates than no-change strategy. However, this out-

of-sample performance was less accurate than estimates obtained from less complex specifications, such as Simple Regression model with Construction Orders as an explanatory variable, ARIMAX specification with a vector of Construction Orders and Multiple Regression equation. All this adds to the earlier suggestions that good fit does not imply good forecasting performance (Section 2.2.3), and that increased model complexity does not necessarily yield greater forecasting accuracy (Section 3.1).

The following section analyses the usefulness of Combination Forecasting. It assesses which sets of combinations generated increased modelling accuracy. It then comments the key reasons as to why certain combinations did not produce better modelling estimates.

5.5 Overall Combination Forecasting accuracy

The Chapter 3 of this thesis discussed the difficulty in using different forecasting methods. As it was indicated, as a standard procedure, property market researchers are selecting the single best model based on its accuracy or statistical complexity. However, this model selection process has been criticised as being unproductive, whereas rejected models may contain important independent information. What is more, analyst are facing dilemma in deciding which model to choose when different specifications suggest different results.

It was then commented that an alternative solution to this issue is to use improved, which mostly means more complex, modelling techniques. However, the idea of creating a more complex specification has been widely criticised. The argument that complexity does not necessarily improve modelling accuracy was presented in Section 3.1.

Accordingly, the principle of Combination Forecasting has been introduced as a useful methodology in achieving greater modelling accuracy. Various authors produced Combination Forecasting using a range of combination principles. However, it was decided to adopt a Simple and OLS based averaging for the current research. These two combination methods were established as being the key in achieving greater modelling estimates.

Following on from this, 380 combination forecasts were computed in total using Simple and OLS based combination approaches. As the modelling estimates suggested, Combination Forecasting improves overall UK commercial property forecasting accuracy. Comparing the best performing individual model (ARIMAXCO_r) out-of-sample fit with the best performing combination accuracy, it is seen that the combination forecast has better statistical properties. Theil's U value for ARIMAXCO_r+SRCCs OLS combination forecast is 0.32, while it is 0.33 for ARIMAXCO_r (the best single model).

Accuracy of combination forecasting, however, was not uniform. Neither Simple Average (SA) combinations generated better out-of-sample estimates than the best parameterised model. The most accurate SA Combination Specification (0.35) was few points less accurate than the most accurate individual model (0.33). Not all OLS based combinations generated forecasting improvement either.

There are two main reasons why SA Combination Forecasting was not more accurate than the best performing model. Firstly, this type of combination does not account for historic accuracy of each model being combined. The SA combination combines two competing forecasts together disregarding their consequential dynamics. This particular specification estimates an average (central point) of two forecasts, which, in the current setting, does not improve modelling accuracy. Secondly, SA Combination Forecasting does not relate to the possible relationship between forecasts. The combination mechanically sums two competing forecasts disregarding interconnections between different models and variables these models contain. These estimates are in line with the criticism of Combination Forecasting discussed in Section 3.2

In case of OLS combination, accuracy improvement came from ARIMAX model combinations. As it is seen from the Table 5.9, a combination of ARIMA models with Construction Orders, Bank Rate and Construction Costs as explanatory variables is more accurate than that of any single model. The OLS Combination Forecasting appreciates the historic accuracy of competing forecasts by regressing them against the dependent variable. This therefore suggests that OLS based combination of models, which incorporate autoregressive component with an effect of key explanatory variables, such as GDP and Construction Orders, improve the overall UK commercial property cycle forecasting accuracy.

The following section summarises Chapter 5.

5.6 Summary

This chapter has presented the empirical results obtained using modelling techniques specified in Chapter 3. Modelling accuracy has been evaluated within in- and out-of-sample periods.

The results obtained using Exponential Smoothing models suggested that none of the Exponential Smoothing specifications fitted the dependent variable. The poor model fit was visually observed. All three models had their R-squared values lower than zero. Exponential smoothing modelling approach therefore proved to be unsuitable for stationary time-series modelling. The out-of-sample performance of Exponential Smoothing did not improve either. All three specifications had their Theil's U values close to one.

Subsequent analysis examined modelling and forecasting accuracy of twenty ARIMA and one-hundred and forty ARIMAX specifications. The results of the study suggested that there was no consensus between modelling accuracy measures as to which ARIMA specification fitted the dependent variable best. However, following the AICc and BIC estimates, it was then commented that ARIMA (1,0,2) was the best parameterised ARIMA specification, which also had the lowest MAPE value. The model fit, as expressed by its R-squared value, suggested that this particular specification fitted the dependent variable. Certainly, there were periods when it under- or over-estimated the dynamics of the series being modelling. Nevertheless, the model was able to explain more than half of the deviations in the series. However, In the out-of-sample, ARIMA (1,0,2) model accuracy was low. Its U value approximated to one. Following on from this, the study estimated that ARIMAX GDP (4,0,0) model had the best statistical properties amongst competing ARIMAX specifications. This particular specification had the smallest AICc and BIC values, and it fitted the historic series best.

Subsequently, seven Simple Regression specifications were computed using seven explanatory variables. The statistical analysis suggested that

Construction Orders and GDP were the best explanatory variables for Simple Regression framework. However, explanatory power of these specifications was low. The R-squared value of the Construction Orders model was 0.339, and it was 0.322 of the GDP based model. In the out-of-sample, the latter two specifications performed better. The GDP based model U value was 0.466 and the Construction Orders based model U value was 0.405. Theil's U valued for other Simple Regression specifications was close to one.

The accuracy of Multiple Regression model was not impressive neither in-sample nor out-of-sample, regardless the fact that it contained five explanatory variables. Certainly, Multiple Regression specification captured the dynamics of the dependent variable and its out-of-sample performance was better than of any Simple Regression specifications. Nevertheless, its performance was lower than that of ARIMA and ARIMAX specifications.

Vector Autoregression specification provided with the best model fit. VAR specification had the largest R-squared value amongst all competing models. However, when it came to out-of-sample forecasting, VAR model performance was not so impressive. Its Theil's U value was higher than that of less complex ARIMAX and Simple Regression models.

The Combination Forecasting was produced using two principle techniques. One was Simple Averaging (SA) and second was Regression (OLS) based combination. There were 380 combination forecasts computed in total, i.e. 190 Simple and 190 OLS. The accuracy of each combination was assessed by computing their Theil's U statistical values. The modelling results suggested that Combination Forecasting improves overall forecasting accuracy. Theil's U statistics for ARIMAXCOr+SRCCs OLS combination forecasting accuracy was greater than that of the best single model.

CHAPTER 6 CONCLUSIONS

This chapter concludes the current research. A discussion of limitations and plausible explanations for unexpected results also are presented. Finally, this chapter highlights practical implications for property market participants and some avenues for further research.

6.1 Summary of the main findings

After the Global financial and property crisis of 2007-2008, it became difficult to ignore the existence of cycles in the general business sector, as well as in building and property. The issue has grown to have significant importance in the UK, as the UK property market has been characterized by boom and bust cycles with a negative impact on the overall British economy. Therefore, this research was set out to determine ways to improve forecasting accuracy of commercial property cycles in the UK.

The literature review of the thesis provided a chronological analysis of property cycle research over a one hundred year period. The particular emphasis was on research methods, data and data analysis techniques employed, and outcomes of these studies. As the review suggested, property cycles have been debated over a long period of time. Subsequently, there has been a shift in understanding on the subject. This shift was from more building/construction and population oriented explanation towards business/economic commentary. Early property cycle researchers considered property/building cycles as a local phenomenon, mostly independent from the wider economy. It was suggested that the sudden increase in population, or migration within certain areas with greater industrial opportunities, was a major driver for property/building cycles to occur. However, later studies considered property cycles as an element of the broader economy. Nowadays, analysts and investors investigate the dynamics of the property market on a global scale.

The subsequent developments in the field of property cycles research led to the construction of various mathematical models helping to explain the behaviour of the real property market. The area of property market modelling and forecasting, which was primarily developed within academia, has been quickly adopted by practitioners. Property practitioners started to employ both quantitative and qualitative research methods to arrive at the final decision. Accordingly, it has resulted in the

development of forecasting models, ranging from simple single-equation methods to more advanced multi-equation with stationary data techniques.

As the research suggested, property forecasting models fall into three major categories: judgemental, univariate and multivariate. The judgemental methods are based on subjective judgement, experience, intuition and any other relevant qualitative information. Univariate methods, also known as decomposition, extrapolative or time-series methods, produce forecasts solely based on current and past values of the series being forecasted. Multivariate methods, known as explanatory or regression methods, forecast any given variable from values of one or more variables that relate to the series of interest. The key time-series models are Moving Average, Exponential Smoothing and ARIMA. The key regression models are Simple Regression, Multiple Regression, VAR and Econometric (Simultaneous Equation). However, as the discussion suggested, despite increased complexity within commercial property market modelling and forecasting, the forecasting adequacy of these specifications can be improved.

The study discussed the difficulty in using different forecasting methods. It was established that, as a standard procedure, property market researchers are selecting the single best model based on its accuracy or statistical complexity. This model selection process has been criticised as being unproductive. First of all, rejected models may contain useful independent information. It was commented that when the aim of the research is to obtain the most accurate forecast, discarding alternative models is unproductive. What is more, researchers are facing difficulty in deciding on the outcomes of research when competing specifications produce different results. The suggestion came to use improved, which mostly means more complex, modelling techniques. However, this proposition has been strongly criticised, i.e. it would require more resources, greater skills and/or additional training to those already at work. The empirical evidences from various fields of research were also not in favour of complex models.

Accordingly, the research presented the principle of Combination Forecasting as a medium helping to achieve greater predictive outcomes. This modelling approach was originally developed by economists and business researchers who were motivated that a combination of forecasts from different methods and sources generates greater predictive results. It was even recommended that Combination Forecasting should become a standard practice within forecasting. Certainly, some researchers argued that Combination Forecasting does not necessarily lead to a better forecasting performance. Nevertheless, theoretical and empirical findings, which date back more than forty years, suggested that Combination Forecasting often outperforms individual forecasts. The Combination Forecasting has been successfully applied within various fields of research, including business, economics and management, psychology, and real estate. Although application of this methodology for commercial property modelling and forecasting has been limited to residential property only.

The study established that Combination Forecasting can be produced simply by averaging different forecasts or employing more complex methods, including weighting or regression estimates. The major principle of forecast averaging is simply by computing the average of two forecasts for the forecasting period. Weighting techniques have two basic principle alternatives. One is historical weighting, which gives weights to the forecasts based on their historic fit. In many cases, each forecast is weighted according to its Mean Squared Error (MSE). Second approach is subjective weighting, which is also known as Bayesian approach. Using this approach, weights to the forecasts are assigned by forecasters themselves based upon their personal experience and judgements as to which model fits and represents the historic data best. The regression, also known as the Ordinary Least Squares (OLS), based combination approach is considered to be a more advanced combination technique.

The research adopted the principle of Combination Forecasting as a means of improving forecasting accuracy of commercial property cycles in

the UK. Two combination techniques, Simple and Regression averaging, were then selected to combine univariate and regression forecasting models. The Univariate (Time-series) methods employed for the research were Exponential Smoothing (Single, Holt's Linear Trend and Brown's Linear Trend), ARIMA and ARIMAX. The Regression based models estimated for the study were Simple Regression, Multiple Regression, and Vector Autoregression.

Following on from this, the study assessed dependent and explanatory variables. The IPD All Property Rents index was chosen as a dependent variable. This index was selected since it is well regarded within UK property investment community and is regularly used by property researchers. The use of rental series as a dependent variable was governed by the suggestions that it is the most important variable for property economics.

The analysis of the data-sets of seventeen organisations and thirteen publications made it possible to collect statistical data on twenty-seven explanatory variables for the 1963-2010 period. The study employed annual chain-linking principle in situations when time-series were of limited length. All time-series were then tested for stationarity. Subsequently, a combination of variable reduction techniques enabled to select seven key explanatory variables which were then used for modelling. These variables were Bank Rate, Construction Costs, Construction Orders, Construction Output, Construction Starts, Employment, and GDP.

All time-series were divided into initialisation and hold-out periods accordingly. Initialisation period was for 1963-2000. The hold-out periods was for 2001-2010. Modelling accuracy was assessed by computing Mean Absolute Error (MAE), Mean Absolute Percentage Error (MAPE) and Mean Squared Error (MSE), as well as Akaike Information Criterion (AIC) and Bayesian Information Criterion (BIC). The out-of-sample modelling accuracy was examined by estimating Theil's second inequality coefficient ' U_2 '. These accuracy measures were established as being the

most commonly used within commercial real estate research and applicable for the current study.

Following on from this, the study assessed whether combination forecasts from different forecasting techniques are more accurate than single model outputs. It investigated which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts more accurately.

The study compared the forecasting ability of eight alternative modelling techniques and a Combination Forecasting to forecast the UK commercial property market rents. The best fitting individual model proved to be VAR specification. Its R-squared was the greatest of all sample models. The AICc also indicate it to be the best parameterised model. However, these results did not come as a surprise. The VAR model comprised key explanatory variables, including Construction Starts, Construction Output, Construction Orders, Construction Costs and GDP, their lagged values as well as past values of the dependent variable itself.

However, despite its goodness of fit, this specification did not produce accurate forecasts. It therefore suggested that goodness of fit does not imply good forecasting performance. The best individual model forecast was obtained from the ARIMAX (1,0,2) specification with Construction Orders as an explanatory variable (ARIMAXCOR). Subsequently, Combination Forecasts were produced using two principle techniques, i.e. Simple Averaging (SA) and Regression (OLS) combination. As results of the study suggested, the ARIMAXCOR+SRCCs OLS combination forecast had better statistical properties than the best single model. It therefore suggested that combination approach and OLS combination in particular is used for commercial property cycle forecasting accuracy improvement.

These findings extend to a practical application of the Combination Forecasting in UK commercial property market modelling field. Often analysts/researchers have access to few competing modelling estimates. It is likely, that these estimates diverge. Therefore, a standard procedure

in econometrics, when a single best model is selected based on its accuracy or its statistical complexity/sophistication, is ineffective. As it was commented throughout the current study, rejected methods may contain useful independent information. What is more, model complexity does not necessarily yield greater modelling results. In that case, when a few alternative models are available, the best approach is to combine them.

The following section present limitations which were unavoidable while conducting this research project.

6.2 Limitations of the research

Although this research was carefully executed, there were some unavoidable limitations. First of all, the modelling was conducted using PASW 18 (SPSS) statistical package. As the discussion in Section 3.3.1 suggested, PASW 18 is a comprehensive software package allowing for time-series modelling. However, it is considered to be a generalised statistical package and that research would benefit if all modelling was done with more specialised software. Hence, it would allow computing Structural econometric specification. This would therefore allow for the employment of all real estate forecasting methods indicated in Figure 2.3 (Section 2.2.1).

The research employed twenty-seven explanatory variables which were obtained from statistical tables of seventeen organisations and thirteen publications. However, there was a small number of key variables for which data was not available. These particular variables were Business Orders, Consumer Confidence, Floor-space, Index of Services, Retail Sales, Take-up, Business Turnover, Risk Premium and Vacancy Rate. The introduction of these variables would certainly enable obtaining additional insights into the dynamics of the UK commercial property market.

Additionally, the study used annual time series over the 1963-2010 period. This gave thirty-seven data points. Although it was established that this length is enough to build a reliable and well parameterised model, the study would benefit from a longer series. This would allow for the estimation of a greater interdependence between dependent and explanatory variables as well as obtaining more accurate autoregressive component.

The next section discusses the practical implications of this research for property market participants.

6.3 Implications for property market participants

After the global financial and property crisis of 2007-2013, neither the general business sector nor building and property sectors ignore the existence of cycles. The cycle issue has grown to have significant importance in the UK, as the UK property market has been characterized by boom and bust cycles with a negative impact on the overall UK economy. Property participants realised that a sound grasp of property cycles is a key determinant of financial success or failure.

The current research examined the UK commercial property market cycle forecasting accuracy and its improvement through Combination Forecasting. Firstly, a chronological analysis of property cycle research over a one hundred year period was presented. The particular emphasis was on research methods, data and data analysis techniques employed, and outcomes of these studies. As the review suggested, property cycles have been debated over a long period of time. Subsequently, there has been a shift in understanding on the subject. This shift was from a more building/construction and population oriented explanation towards business/economic commentary. Secondly, the study discussed developments in the field of property cycles research and various cycle theories. Following on from this, the research commented on the application of econometrics in assessing cycle duration. Finally, it assessed whether Combination Forecasts from different forecasting techniques are better than single model outputs. It examined which of them - combination or single forecast - fits the UK commercial property market better, and which of these options forecasts best. As the results of the study suggested, Combination Forecasting is useful in improving UK commercial property cycle forecasting accuracy.

The results of the current research inform real estate market participants. A greater awareness of cycles and the ability to forecast them more accurately could be useful for both the private and public sectors in examining economic issues. The existence of business cycles implies that

the economy has its rhythm and dynamic behaviour. Analysts, who can recognise short and long property cycles, determine their repetitive nature, and subsequently estimate future direction, are well positioned to anticipate changes in the economy and property market better.

For investors and portfolio managers, this updated knowledge of forecasting accuracy improvement through Combination Forecasting allows making better investment decisions. A greater understanding of the length of the cycles and improved forecasting accuracy can enrich their strategies. A better appreciation of market timing allows them to allocate funds more effectively. For property developers, an increased market timing knowledge is even more crucial. Considering, that property market lags the general economy by around 2 years (as mentioned above, construction lag depends on the nature of the project as well as its complexity and location), having a greater appreciation of the property market cycle and the existing situation, allows developers to plan projects with a greater accuracy. Knowing where they are in the cycle and having obtained more accurate forecasting estimates, developers can subsequently either build new projects in the anticipation that once projects are completed, the general economy will be in the upturn and therefore there will be a demand for property, or they can acquire new sites when economy and property market is in correction, so that when the economy recovers, they can start building. Additionally, policy makers, wary of future crashes, could bring real estate cycle insights to bear on future policy design to guide the general economy towards stability.

This research has thrown up many questions in need of further investigation. The following section presents some possible future research avenues.

6.4 Further related work

The study was not able to explore all the issues that have come up during the course of the research and the author is aware that more exists to be researched in this field. The further related work could assess alternative combination techniques, examine whether combination of more than two forecasting models further improves the accuracy of commercial property forecasting, assess effectiveness of Combination Forecasting within shorter/longer out-of-sample period, as well as establish whether Combination Forecasting is applicable in forecasting alternative real estate indicators.

As it was discussed in section 3.2.2, there is a number of forecasting combination techniques available to researches. One of them is the weighting approach. It was suggested that weighting is computed using model historic fit which is mostly derived from Mean Squared Error (MSE) estimates of each competing forecast, or it can be assigned by modellers themselves based on their experience and judgement. Certainly, weighting combination was an object of some heavy criticism. Nevertheless, further research in this direction can yield additional insights into the accuracy improvement through Weighting Combination.

The research employed a combination of two competing forecasts within its framework. The combination of two models came up from the literature review where it was established that in case of OLS Combination Forecasting, a combination of more than two models can yield negative results. However, a further research could assess whether combination of three and more models does improve the accuracy of commercial property forecasting.

A future study investigating effectiveness of Combination Forecasting within shorter/longer out-of-sample periods could also be very interesting. The current study adopted 10-year out-of-sample period. However, considering different properties of univariate and multivariate modelling techniques, which were discussed in Section 2.2.1, it would be useful to

assess the forecasting accuracy of each model and their combination within different time scale.

Further, research could assess whether the principle of Combination Forecasting is applicable in modelling real estate indicators. The current research employed rental index as the dependent variable. The use of this particular variable came from the suggestions that rent dynamics is of particular importance for investors and analysts. It was commented that rent acts as an agent which brings four inter-related property markets, i.e. user, financial, development and land market into simultaneous equilibrium. However, further studies could examine the applicability of Combination Forecasting to model real estate returns, yields and other property market indicators.

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APPENDIX A. Time-series used for the research

| Year | IPD Rents | Bank Rate | Business Output | Car Registrations | Construction Orders |
|------|--------------|--------------|--------------------|----------------------|------------------------|
| | % p.a. | % p.a. | index | 000's | £ mill |
| 1963 | 8.33 | 4.00 | 11 | 1,466 | |
| 1964 | 11.54 | 6.00 | 11.6 | 1,711.2 | 14,612.59 |
| 1965 | 10.34 | 6.00 | 12.2 | 1,600.7 | 12,088.61 |
| 1966 | 9.38 | 7.00 | 12.5 | 1,493.6 | 10,819.20 |
| 1967 | 8.57 | 6.42 | 13.7 | 1,575.2 | 8,982.52 |
| 1968 | 7.89 | 7.25 | 13.8 | 1,561.9 | 9,781.19 |
| 1969 | 2.44 | 8.00 | 14.3 | 1,401.8 | 10,187.07 |
| 1970 | 9.52 | 7.25 | 15.2 | 1,524.9 | 11,778.61 |
| 1971 | 17.39 | 5.50 | 15.9 | 1,741.6 | 14,505.69 |
| 1972 | 14.81 | 6.00 | 16.6 | 2,183.7 | 14,603.43 |
| 1973 | 20.97 | 9.23 | 17.6 | 2,230.3 | 14,479.09 |
| 1974 | 22.67 | 12.13 | 18.2 | 1,750.40 | 10,341.50 |
| 1975 | 8.70 | 10.85 | 18.8 | 1,749.90 | 7,869.93 |
| 1976 | 1.60 | 11.68 | 19.6 | 1,838.00 | 8,934.07 |
| 1977 | 4.70 | 8.96 | 20.3 | 1,862.00 | 9,352.23 |
| 1978 | 9.80 | 9.04 | 21.5 | 2,151.40 | 11,067.05 |
| 1979 | 14.60 | 14.00 | 22.9 | 2,369.90 | 10,040.59 |
| 1980 | 12.50 | 15.00 | 23.7 | 2,155.80 | 10,481.20 |
| 1981 | 7.92 | 12.00 | 24.7 | 2,030.30 | 12,592.29 |
| 1982 | 3.77 | 11.89 | 26.3 | 2,103.90 | 12,823.37 |
| 1983 | 2.84 | 9.93 | 28.4 | 2,307.50 | 13,086.93 |
| 1984 | 4.23 | 10.02 | 30.6 | 2,238.90 | 15,447.97 |
| 1985 | 6.49 | 12.52 | 32.4 | 2,309.30 | 16,366.69 |
| 1986 | 9.86 | 10.94 | 36 | 2,333.70 | 18,735.94 |
| 1987 | 19.27 | 9.38 | 38 | 2,473.90 | 24,284.44 |
| 1988 | 22.84 | 9.46 | 41.5 | 2,723.50 | 28,786.56 |
| 1989 | 15.07 | 10.00 | 42.2 | 2,828.90 | 29,260.90 |
| 1990 | 2.77 | 13.88 | 43.8 | 2,438.70 | 24,219.92 |
| 1991 | -8.53 | 11.88 | 43.1 | 1,921.50 | 19,684.24 |
| 1992 | -11.93 | 8.38 | 41.9 | 1,901.80 | 16,620.22 |
| 1993 | -7.87 | 5.63 | 43.1 | 2,073.90 | 16,867.12 |
| 1994 | -0.94 | 5.63 | 46.7 | 2,249.00 | 17,545.45 |
| 1995 | 0.38 | 6.50 | 49.1 | 2,306.54 | 18,676.86 |
| 1996 | 3.19 | 5.92 | 52.7 | 2,410.12 | 20,310.51 |
| 1997 | 7.68 | 6.75 | 57.1 | 2,597.71 | 22,537.09 |
| 1998 | 7.33 | 6.94 | 63.2 | 2,740.00 | 26,267.90 |
| 1999 | 5.68 | 5.42 | 67.8 | 2,766.00 | 23,552.22 |
| 2000 | 7.01 | 5.88 | 73.5 | 2,871.00 | 23,745.69 |
| 2001 | 3.40 | 4.96 | 77.8 | 3,138.00 | 23,214.21 |
| 2002 | -0.85 | 4.00 | 78.9 | 3,229.00 | 22,076.48 |
| 2003 | -1.58 | 3.67 | 83.1 | 3,231.90 | 19,836.03 |
| 2004 | 2.29 | 4.38 | 87.9 | 3,185.44 | 22,790.70 |
| 2005 | 2.69 | 4.50 | 93.6 | 3,021.37 | 24,319.16 |
| 2006 | 4.24 | 4.88 | 100 | 2,913.58 | 30,886.63 |
| 2007 | 4.30 | 5.50 | 106.9 | 2,996.91 | 31,587.63 |
| 2008 | -1.20 | 3.95 | 109.3 | 2,672.19 | 22,922.01 |
| 2009 | -7.90 | 1.00 | 102.6 | 2,371.21 | 13,289.57 |
| 2010 | -0.80 | 0.50 | 103.5 | 2,400.00 | 14,755.00 |

| Year | Construction Completions | | Construction Starts | Consumer Confidence | Consumer Expenditure |
|------|--------------------------|----------------------------|---------------------|---------------------|----------------------|
| | Construction Output | House building Completions | | | |
| | £ mill | numbers | numbers | index | £ |
| | | | | 444,647 | |
| 1963 | 8147.69 | 307,710 | | 409,593 | 19,547 |
| 1964 | 8685.53 | 383,190 | | 395,717 | 20,865 |
| 1965 | 9301.38 | 391,230 | | 466,973 | 22,149 |
| 1966 | 9311.81 | 396,010 | | 411,366 | 23,386 |
| 1967 | 9738.58 | 415,460 | | 358,263 | 24,566 |
| 1968 | 9247.58 | 425,830 | | 332,703 | 26,455 |
| 1969 | 9446.82 | 378,330 | | 359,202 | 28,054 |
| 1970 | 9751.99 | 362,230 | | 366,297 | 30,541 |
| 1971 | 10549.92 | 364,480 | | 342,823 | 34,226 |
| 1972 | 10250.20 | 330,940 | | 262,907 | 38,787 |
| 1973 | 10467.79 | 304,640 | 97.71 | 336,876 | 44,511 |
| 1974 | 9615.23 | 279,630 | 95.70 | 339,484 | 51,356 |
| 1975 | 8765.71 | 322,000 | 98.44 | 278,556 | 63,038 |
| 1976 | 7745.16 | 324,840 | 101.05 | 276,157 | 73,243 |
| 1977 | 7704.11 | 314,160 | 104.81 | 234,843 | 83,823 |
| 1978 | 8499.01 | 288,690 | 101.60 | 161,813 | 96,656 |
| 1979 | 8088.24 | 251,820 | 96.83 | 160,874 | 114,693 |
| 1980 | 8098.97 | 242,000 | 96.60 | 202,084 | 133,174 |
| 1981 | 8208.42 | 206,630 | 99.76 | 230,252 | 148,052 |
| 1982 | 9255.73 | 182,850 | 102.47 | 207,718 | 162,228 |
| 1983 | 9454.04 | 209,030 | 101.32 | 208,552 | 178,027 |
| 1984 | 10205.03 | 220,410 | 98.05 | 222,950 | 191,390 |
| 1985 | 11072.08 | 207,470 | 98.68 | 240,581 | 209,382 |
| 1986 | 12226.87 | 216,540 | 102.35 | 262,699 | 232,095 |
| 1987 | 14599.25 | 226,230 | 102.32 | 209,387 | 255,361 |
| 1988 | 16690.29 | 242,360 | 99.61 | 171,203 | 288,346 |
| 1989 | 21252.29 | 221,460 | 96.82 | 171,620 | 315,822 |
| 1990 | 23821.30 | 203,230 | 97.93 | 170,690 | 343,041 |
| 1991 | 20874.32 | 191,450 | 98.05 | 164,150 | 364,586 |
| 1992 | 17168.49 | 179,690 | 97.70 | 193,380 | 384,131 |
| 1993 | 14411.28 | 186,070 | 98.26 | 211,420 | 406,813 |
| 1994 | 14364.03 | 193,970 | 99.85 | 178,390 | 426,710 |
| 1995 | 14774.00 | 199,930 | 101.20 | 185,850 | 448,720 |
| 1996 | 16329.08 | 189,270 | 103.58 | 200,820 | 482,041 |
| 1997 | 18285.60 | 191,110 | 102.24 | 187,930 | 512,482 |
| 1998 | 19867.94 | 181,020 | 101.72 | 191,120 | 546,887 |
| 1999 | 22386.69 | 181,990 | 101.69 | 186,190 | 582,371 |
| 2000 | 22461.23 | 176,850 | 101.43 | 192,070 | 616,558 |
| 2001 | 22320.95 | 174,080 | 101.66 | 194,370 | 647,777 |
| 2002 | 22887.13 | 181,960 | 101.05 | 208,570 | 680,964 |
| 2003 | 22253.74 | 190,490 | 101.97 | 227,990 | 714,605 |
| 2004 | 23560.97 | 203,490 | 102.19 | 223,900 | 749,867 |
| 2005 | 23672.56 | 209,580 | 101.34 | 223,970 | 784,140 |
| 2006 | 26462.61 | 212,800 | 101.55 | 228,650 | 819,610 |
| 2007 | 29429.60 | 225,330 | 97.21 | 134,500 | 861,695 |
| 2008 | 30006.73 | 182,960 | 97.64 | 106,820 | 892,194 |
| 2009 | 22947.12 | 152,630 | 99.41 | 130840 | 874,380 |
| 2010 | 23025.56 | 134080 | | | 919,310 |

| Year | Depreciation | Real household disposable income | Employment | Foreign Direct Investment | GDP Growth |
|------|--------------|----------------------------------|------------|---------------------------|------------|
| | £ mill | index | 000's | \$ mill | % p.a. |
| 1963 | 59 | 143.8 | 11406.08 | | 4.30 |
| 1964 | 67 | 148.9 | 11682.38 | -24.90 | 5.48 |
| 1965 | 68 | 150.8 | 12199.55 | 29.02 | 2.23 |
| 1966 | 75 | 153.4 | 12579.75 | 24.10 | 1.93 |
| 1967 | 77 | 154.8 | 12933.98 | 14.56 | 2.47 |
| 1968 | 83 | 156.9 | 13059.14 | 41.53 | 4.20 |
| 1969 | 86 | 157.7 | 13266.95 | -10.98 | 2.07 |
| 1970 | 96 | 163.0 | 13545.61 | 39.24 | 2.24 |
| 1971 | 109 | 164.1 | 13701.47 | 17.55 | 2.09 |
| 1972 | 130 | 177.2 | 13956.51 | -33.97 | 3.66 |
| 1973 | 165 | 188.0 | 14509.11 | 130.91 | 7.20 |
| 1974 | 226 | 186.1 | 15257.70 | 69.45 | -1.31 |
| 1975 | 293 | 187.5 | 15619.02 | -19.35 | -0.62 |
| 1976 | 362 | 186.5 | 16202.31 | 8.94 | 2.64 |
| 1977 | 458 | 182.5 | 16665.16 | 53.95 | 2.38 |
| 1978 | 568 | 195.9 | 16847.00 | -22.89 | 3.23 |
| 1979 | 732 | 207.2 | 17259.00 | 54.40 | 2.69 |
| 1980 | 946 | 210.2 | 17465.00 | 43.73 | -2.03 |
| 1981 | 1145 | 209.2 | 17210.00 | -32.67 | -1.22 |
| 1982 | 1319 | 209.2 | 17165.00 | 3.23 | 2.20 |
| 1983 | 1438 | 213.6 | 17211.00 | 11.83 | 3.69 |
| 1984 | 1620 | 221.3 | 17859.00 | -105.33 | 2.69 |
| 1985 | 1866 | 228.4 | 18217.00 | -2593.92 | 3.62 |
| 1986 | 2191 | 237.6 | 18424.00 | 29.60 | 4.01 |
| 1987 | 2655 | 241.0 | 18909.00 | 64.02 | 4.56 |
| 1988 | 3075 | 254.0 | 19666.00 | 31.89 | 5.03 |
| 1989 | 3817 | 265.5 | 20283.00 | 51.94 | 2.28 |
| 1990 | 4813 | 276.8 | 20733.00 | -0.50 | 0.78 |
| 1991 | 5643 | 281.2 | 20459.00 | -51.93 | -1.39 |
| 1992 | 5928 | 288.1 | 20408.00 | 2.38 | 0.15 |
| 1993 | 6104 | 296.1 | 20313.00 | 16.22 | 2.22 |
| 1994 | 6234 | 299.5 | 20532.00 | -35.13 | 4.28 |
| 1995 | 6574 | 306.5 | 20908.00 | 94.83 | 3.05 |
| 1996 | 7129 | 315.1 | 21170.00 | 26.99 | 2.89 |
| 1997 | 7098 | 327.5 | 21679.00 | 30.38 | 3.31 |
| 1998 | 7843 | 333.4 | 21824.00 | 96.74 | 3.61 |
| 1999 | 8787 | 341.7 | 22403.00 | 22.22 | 3.47 |
| 2000 | 9391 | 354.9 | 22959.00 | 46.31 | 3.92 |
| 2001 | 9817 | 369.2 | 23497.00 | -53.64 | 2.46 |
| 2002 | 10558 | 375.4 | 23886.00 | -55.07 | 2.10 |
| 2003 | 11325 | 385.1 | 24361.00 | -0.04 | 2.81 |
| 2004 | 12022 | 387.3 | 24762.00 | 86.03 | 2.95 |
| 2005 | 12809 | 392.5 | 25205.00 | 213.53 | 2.17 |
| 2006 | 13138 | 393.1 | 25602.00 | -13.24 | 2.79 |
| 2007 | 13377 | 392.3 | 25822.00 | 18.21 | 2.68 |
| 2008 | 14390 | 397.9 | 26152.00 | -50.40 | -0.07 |
| 2009 | 15522 | 399.0 | 25843.00 | -22.01 | -4.87 |
| 2010 | | 395.9 | 25662.00 | -41.58 | 1.40 |

| Year | FTSE All-Share Index | Lagged Dependent Variable | Gilts-Treasury Bills-Yields | |
|------|----------------------|---------------------------|---------------------------------------|----------------------|
| | | | 2.5% Consolidated Stock Average Yield | Par yield (20 years) |
| | index | % p.a. | % | % |
| 1963 | 107.86 | | 5.59 | 5.44 |
| 1964 | 97.07 | 8.33 | 6.03 | 5.96 |
| 1965 | 103.6 | 11.54 | 6.42 | 6.60 |
| 1966 | 93.95 | 10.34 | 6.81 | 7.10 |
| 1967 | 121.18 | 9.38 | 6.70 | 6.98 |
| 1968 | 173.72 | 8.57 | 7.40 | 7.75 |
| 1969 | 147.34 | 7.89 | 8.89 | 9.29 |
| 1970 | 136.26 | 2.44 | 9.17 | 9.47 |
| 1971 | 193.39 | 9.52 | 9.07 | 9.09 |
| 1972 | 218.18 | 17.39 | 9.13 | 9.14 |
| 1973 | 149.76 | 14.81 | 10.85 | 11.00 |
| 1974 | 66.89 | 20.97 | 14.95 | 15.17 |
| 1975 | 158.08 | 22.67 | 14.68 | 14.78 |
| 1976 | 151.96 | 8.70 | 14.25 | 14.82 |
| 1977 | 214.53 | 1.60 | 12.31 | 13.07 |
| 1978 | 220.22 | 4.70 | 11.92 | 12.81 |
| 1979 | 229.79 | 9.80 | 11.38 | 13.34 |
| 1980 | 291.99 | 14.60 | 11.86 | 14.15 |
| 1981 | 313.12 | 12.50 | 12.99 | 15.14 |
| 1982 | 382.22 | 7.92 | 11.90 | 13.23 |
| 1983 | 470.50 | 3.77 | 10.24 | 11.09 |
| 1984 | 592.94 | 2.84 | 10.15 | 10.71 |
| 1985 | 682.94 | 4.23 | 10.11 | 10.78 |
| 1986 | 835.48 | 6.49 | 9.47 | 10.13 |
| 1987 | 870.22 | 9.86 | 9.31 | 9.73 |
| 1988 | 926.59 | 19.27 | 9.12 | 9.61 |
| 1989 | 1204.70 | 22.84 | 9.26 | 9.84 |
| 1990 | 1032.25 | 15.07 | 10.88 | 11.38 |
| 1991 | 1187.70 | 2.77 | 9.99 | 10.19 |
| 1992 | 1363.79 | -8.53 | 9.16 | 9.37 |
| 1993 | 1682.15 | -11.93 | 7.69 | 8.07 |
| 1994 | 1521.44 | -7.87 | 8.18 | 7.81 |
| 1995 | 1803.09 | -0.94 | 8.24 | 8.09 |
| 1996 | 2013.66 | 0.38 | 8.03 | 8.16 |
| 1997 | 2411.00 | 3.19 | 7.15 | 6.99 |
| 1998 | 2673.92 | 7.68 | 5.59 | 5.34 |
| 1999 | 3242.06 | 7.33 | 4.87 | 4.51 |
| 2000 | 2983.81 | 5.68 | 4.93 | 4.42 |
| 2001 | 2523.88 | 7.01 | 4.99 | 4.67 |
| 2002 | 1893.73 | 3.40 | 5.04 | 4.75 |
| 2003 | 2207.38 | -0.85 | 4.87 | 4.64 |
| 2004 | 2410.75 | -1.58 | 4.79 | 4.69 |
| 2005 | 2847.02 | 2.29 | 4.45 | 4.34 |
| 2006 | 3221.42 | 2.69 | 4.24 | 4.17 |
| 2007 | 3286.67 | 4.24 | 4.62 | 4.56 |
| 2008 | 2209.29 | 4.30 | 4.60 | 4.66 |
| 2009 | 2761.00 | -1.20 | 4.54 | 4.45 |
| 2010 | 3063.00 | -7.90 | 4.66 | 4.47 |

| Year | Money Supply | | Profitability | UK House Price Index | Inflation |
|------|--------------|-------------|---------------|----------------------|-----------|
| | Broad (M4) | Narrow (M0) | | | |
| | £ bn | £ bn | £ bn | index | % p.a. |
| 1963 | 14.80 | 2.40 | 936 | 150.20 | 2 |
| 1964 | 15.90 | 2.56 | 1036 | 164.20 | 3.3 |
| 1965 | 17.40 | 2.73 | 959 | 177.30 | 4.8 |
| 1966 | 18.50 | 2.89 | 915 | 187.30 | 3.9 |
| 1967 | 20.90 | 2.87 | 977 | 197.50 | 2.5 |
| 1968 | 22.70 | 3.12 | 1050 | 212.10 | 4.7 |
| 1969 | 23.80 | 3.90 | 1009 | 223.30 | 5.4 |
| 1970 | 26.60 | 3.80 | 1095 | 236.90 | 6.4 |
| 1971 | 31.00 | 4.10 | 1201 | 270.10 | 9.4 |
| 1972 | 38.20 | 4.40 | 1343 | 368.10 | 7.1 |
| 1973 | 46.60 | 4.90 | 1244 | 478.40 | 9.2 |
| 1974 | 51.70 | 5.40 | 968 | 533.00 | 16 |
| 1975 | 57.80 | 6.20 | 1174 | 573.60 | 24.2 |
| 1976 | 64.40 | 7.00 | 1190 | 627.60 | 16.5 |
| 1977 | 74.00 | 7.80 | 1239 | 677.20 | 15.8 |
| 1978 | 85.20 | 8.90 | 1365 | 807.20 | 8.3 |
| 1979 | 97.50 | 10.10 | 1306 | 1048.80 | 13.4 |
| 1980 | 114.30 | 10.90 | 1267 | 1231.70 | 18 |
| 1981 | 137.80 | 11.50 | 1351 | 1266.90 | 11.9 |
| 1982 | 153.90 | 11.90 | 1542 | 1314.40 | 8.6 |
| 1983 | 174.20 | 12.60 | 1669 | 1461.00 | 4.6 |
| 1984 | 198.20 | 13.30 | 1760 | 1643.60 | 5 |
| 1985 | 224.10 | 13.90 | 1743 | 1818.20 | 6.1 |
| 1986 | 258.00 | 14.50 | 1801 | 1990.00 | 3.4 |
| 1987 | 304.50 | 15.20 | 1937 | 2282.90 | 4.2 |
| 1988 | 357.30 | 16.20 | 2148 | 2718.80 | 4.9 |
| 1989 | 425.70 | 17.20 | 1580 | 3253.40 | 7.8 |
| 1990 | 477.40 | 18.10 | 1398 | 3050.80 | 9.5 |
| 1991 | 504.60 | 18.50 | 1306 | 2889.10 | 5.9 |
| 1992 | 518.20 | 19.00 | 1136 | 2740.50 | 3.7 |
| 1993 | 543.40 | 19.90 | 1196 | 2708.50 | 1.6 |
| 1994 | 566.30 | 21.20 | 1274 | 2730.90 | 2.4 |
| 1995 | 622.40 | 22.40 | 1135 | 2710.30 | 3.5 |
| 1996 | 681.60 | 24.00 | 1242 | 2824.00 | 2.4 |
| 1997 | 719.90 | 25.50 | 1440 | 3131.00 | 3.1 |
| 1998 | 782.00 | 27.00 | 1347 | 3448.40 | 3.4 |
| 1999 | 813.70 | 28.90 | 1469 | 3761.60 | 1.5 |
| 2000 | 881.60 | 31.20 | 1433 | 4250.50 | 3 |
| 2001 | 940.00 | 33.50 | 1457 | 4696.50 | 1.8 |
| 2002 | 1006.10 | 36.20 | 1586 | 5627.80 | 1.7 |
| 2003 | 1077.90 | 38.80 | 1345 | 6730.00 | 2.9 |
| 2004 | 1174.50 | 41.20 | 1792 | 7862.40 | 3 |
| 2005 | 1322.90 | 43.00 | 1529 | 8267.90 | 2.8 |
| 2006 | 1493.30 | 45.20 | 1594 | 8804.50 | 3.2 |
| 2007 | 1671.00 | 47.30 | 1548 | 9592.20 | 4.3 |
| 2008 | 1933.90 | 50.20 | 889 | 8936.90 | 4 |
| 2009 | 2038.50 | 54.30 | 847 | 8277.80 | -0.5 |
| 2010 | 2152.70 | 57.00 | 883 | 8752.30 | 4.6 |

| Year | ONS leading indicators | | Unemployment | Vacancy Rate | Job Vacancies |
|------|------------------------|---------------------|--------------|--------------|---------------|
| | Index of Services | Index of Production | | | |
| | index | index | % p.a. | % | 000's |
| 1963 | | 52.6 | 2.2 | | 23,914 |
| 1964 | | 57.00 | 1.6 | | 24,241 |
| 1965 | | 58.60 | 1.4 | | 24,531 |
| 1966 | | 59.50 | 1.4 | | 24,720 |
| 1967 | | 59.90 | 2.2 | | 24,254 |
| 1968 | | 64.50 | 2.3 | | 24,084 |
| 1969 | | 66.70 | 2.3 | | 24,051 |
| 1970 | | 67.00 | 2.4 | | 23,897 |
| 1971 | | 66.70 | 4.2 | | 23,543 |
| 1972 | | 67.90 | 4.4 | | 23,547 |
| 1973 | | 74.00 | 3.7 | | 24,132 |
| 1974 | | 72.50 | 3.7 | | 24,271 |
| 1975 | | 68.60 | 4.5 | | 24,186 |
| 1976 | | 70.80 | 5.4 | | 23,990 |
| 1977 | | 74.50 | 5.6 | | 24,079 |
| 1978 | | 76.60 | 5.6 | | 24,244 |
| 1979 | | 79.50 | 5.4 | | 24,663 |
| 1980 | | 74.30 | 6.9 | | 24,470 |
| 1981 | | 72.00 | 9.8 | | 23,308 |
| 1982 | | 73.40 | 10.9 | | 22,799 |
| 1983 | | 76.00 | 11.6 | | 22,421 |
| 1984 | | 76.10 | 11.9 | | 22,613 |
| 1985 | | 80.30 | 11.4 | | 22,812 |
| 1986 | | 82.20 | 11.4 | | 22,776 |
| 1987 | | 85.50 | 10.5 | | 22,989 |
| 1988 | | 89.70 | 8.6 | | 23,708 |
| 1989 | | 91.50 | 7.2 | | 24,149 |
| 1990 | | 91.30 | 7.2 | | 24,450 |
| 1991 | | 88.20 | 8.9 | | 23,774 |
| 1992 | | 88.50 | 10.1 | | 23,392 |
| 1993 | | 90.40 | 10.5 | | 23,014 |
| 1994 | | 95.30 | 9.6 | | 23,095 |
| 1995 | | 97.00 | 8.7 | | 23,475 |
| 1996 | 3.60 | 98.30 | 8.2 | | 23,789 |
| 1997 | 4.20 | 99.70 | 7.0 | | 24,401 |
| 1998 | 5.20 | 100.70 | 6.3 | | 24,775 |
| 1999 | 4.60 | 102.20 | 6.0 | | 25,168 |
| 2000 | 4.80 | 104.10 | 5.6 | | 25,744 |
| 2001 | 3.60 | 102.50 | 5.1 | 6.80 | 26,100 |
| 2002 | 2.40 | 100.80 | 5.2 | 9.50 | 26,244 |
| 2003 | 3.50 | 100.20 | 5.1 | 14.50 | 26,324 |
| 2004 | 3.50 | 101.20 | 4.9 | 15.30 | 26,566 |
| 2005 | 3.10 | 100.00 | 4.9 | 12.00 | 26,970 |
| 2006 | 4.00 | 100.00 | 5.5 | 8.70 | 27,287 |
| 2007 | 3.50 | 100.10 | 5.4 | 5.10 | 27,426 |
| 2008 | 0.50 | 97.00 | 5.8 | 5.70 | 27,645 |
| 2009 | -3.20 | 87.20 | 7.8 | 9.70 | 27,048 |
| 2010 | 1.10 | 89.10 | 8.0 | 8.10 | 26,615 |

| Year | Gross Capital Formation | Total Returns | Index of Land Prices | Risk Premium | Construction Costs |
|------|----------------------------|------------------|-------------------------|--------------|-----------------------|
| | £ mill | % p.a. | index | % | index |
| 1963 | 3,484,779,541 | 10.30 | 40 | | 5.42 |
| 1964 | 3,655,323,394 | 8.30 | 56 | | 5.61 |
| 1965 | 4,351,000,000 | 4.70 | 63 | | 5.87 |
| 1966 | 4,608,000,000 | 3.20 | 67 | | 6.10 |
| 1967 | 4,921,000,000 | 7.90 | 68 | | 6.25 |
| 1968 | 5,296,000,000 | 21.30 | 79 | -0.32 | 6.55 |
| 1969 | 5,571,000,000 | 5.20 | 98 | -0.96 | 6.88 |
| 1970 | 6,367,000,000 | 24.60 | 100 | -1.01 | 7.33 |
| 1971 | 6,963,000,000 | 16.10 | 114 | 0.23 | 8.01 |
| 1972 | 7,394,000,000 | 29.50 | 192 | 1.92 | 8.60 |
| 1973 | 9,087,000,000 | 28.50 | 298 | 2.00 | 9.39 |
| 1974 | 11,504,000,000 | -16.20 | 296 | -1.29 | 10.89 |
| 1975 | 13,965,000,000 | 11.50 | 204 | -2.37 | 13.50 |
| 1976 | 16,535,000,000 | 9.40 | 204 | 0.20 | 15.75 |
| 1977 | 19,092,000,000 | 26.50 | 216 | 0.11 | 18.26 |
| 1978 | 22,012,000,000 | 25.70 | 263 | 0.97 | 19.75 |
| 1979 | 25,912,000,000 | 23.00 | 373 | 0.74 | 22.41 |
| 1980 | 29,003,000,000 | 17.50 | 492 | 0.92 | 26.45 |
| 1981 | 29,300,000,000 | 15.00 | 512 | 1.05 | 29.59 |
| 1982 | 31,712,000,000 | 7.50 | 576 | 0.26 | 32.13 |
| 1983 | 33,469,000,000 | 7.60 | 649 | 0.42 | 33.59 |
| 1984 | 38,202,000,000 | 8.60 | 733 | 0.20 | 35.28 |
| 1985 | 42,899,000,000 | 8.30 | 952 | 0.38 | 37.41 |
| 1986 | 43,137,000,000 | 11.10 | 1,101 | 0.73 | 38.68 |
| 1987 | 50,257,000,000 | 25.80 | 1,600 | 0.50 | 40.29 |
| 1988 | 60,555,000,000 | 29.70 | 2,091 | 0.39 | 42.27 |
| 1989 | 74,981,000,000 | 15.40 | 2,063 | 0.49 | 45.56 |
| 1990 | 78,284,000,000 | -8.40 | 1,869 | 0.64 | 49.87 |
| 1991 | 72,073,000,000 | -3.20 | 1,776 | 0.66 | 52.78 |
| 1992 | 68,560,000,000 | -1.70 | 1,591 | 0.72 | 54.65 |
| 1993 | 66,807,000,000 | 20.00 | 1,554 | 0.48 | 55.51 |
| 1994 | 72,069,000,000 | 12.00 | 1,785 | 0.70 | 56.86 |
| 1995 | 80,447,000,000 | 3.50 | 1,878 | 0.32 | 58.84 |
| 1996 | 90,414,000,000 | 10.00 | 2,026 | 0.36 | 60.27 |
| 1997 | 97,487,000,000 | 16.80 | 2,035 | 0.18 | 62.14 |
| 1998 | 112,796,000,000 | 11.80 | 2,192 | 0.10 | 65.31 |
| 1999 | 115,795,000,000 | 14.50 | 2,590 | 0.38 | 69.01 |
| 2000 | 118,917,000,000 | 10.40 | 3,053 | 0.30 | 72.80 |
| 2001 | 118,334,000,000 | 6.79 | 3,793 | 0.18 | 77.66 |
| 2002 | 118,172,000,000 | 9.64 | 4,505 | 0.32 | 84.38 |
| 2003 | 117,167,000,000 | 10.85 | 5,322 | 0.14 | 89.48 |
| 2004 | 117,736,000,000 | 18.33 | 12,247 | 0.13 | 95.10 |
| 2005 | 137,984,000,000 | 19.10 | 13,378 | -0.03 | 100.00 |
| 2006 | 127,938,000,000 | 18.10 | 14,382 | 0.09 | 103.82 |
| 2007 | 143,848,000,000 | -3.40 | 15,704 | 0.00 | 108.25 |
| 2008 | 144,518,000,000 | -22.10 | 14,748 | 0.00 | 109.14 |
| 2009 | 121,282,000,000 | 3.50 | 10,356 | 0.32 | 103.02 |
| 2010 | 127,184,000,000 | 14.50 | 9,667 | 0.10 | 99.13 |

| Year | Floor-space mill., sq.m. | Number of property transactions 000's | Turnover £ mill | Retail Sales % p.a. | Net Investment £ mill |
|------|-----------------------------|---|--------------------|------------------------|-----------------------------|
| 1963 | | | | | 920 |
| 1964 | | | | | 1016 |
| 1965 | | 11.40 | | | 1151 |
| 1966 | | 10.30 | | | 1658 |
| 1967 | | 10.40 | | | 1873 |
| 1968 | | 10.50 | | | 2152 |
| 1969 | | 10.50 | | | 2518 |
| 1970 | | 9.60 | | | 2917 |
| 1971 | | 9.90 | | | 3429 |
| 1972 | | 10.20 | | | 3839 |
| 1973 | | 10.00 | | | 5353 |
| 1974 | | 7.30 | | | 6196 |
| 1975 | | 6.50 | | | 7499 |
| 1976 | | 6.90 | | | 9042 |
| 1977 | | 8.70 | | | 12097 |
| 1978 | | 9.20 | | | 15013 |
| 1979 | | 8.90 | | | 18467 |
| 1980 | | 8.50 | | | 22977 |
| 1981 | | 8.30 | | | 26878 |
| 1982 | | 9.40 | | | 29419 |
| 1983 | | 10.60 | | | 31306 |
| 1984 | | 11.30 | | | 34432 |
| 1985 | | 11.60 | | | 36523 |
| 1986 | 6.61 | 10.70 | | | 40093 |
| 1987 | 6.63 | 11.10 | | | 47792 |
| 1988 | 6.54 | 11.70 | | | 61216 |
| 1989 | 6.71 | 11.30 | | 2.70 | 70727 |
| 1990 | 6.96 | 10.40 | | 1.30 | 66068 |
| 1991 | 7.41 | 9.80 | | -2.10 | 61038 |
| 1992 | 7.76 | 9.70 | | 0.20 | 53836 |
| 1993 | 7.82 | 10.50 | | 2.50 | 59779 |
| 1994 | 7.8 | 11.40 | | 3.20 | 64675 |
| 1995 | 7.66 | 11.50 | | 0.50 | 60957 |
| 1996 | 7.65 | 12.10 | | 2.90 | 62740 |
| 1997 | 7.67 | 12.30 | | 4.20 | 73126 |
| 1998 | 7.42 | 12.30 | | 2.20 | 74202 |
| 1999 | 7.46 | 12.00 | | 2.60 | 85376 |
| 2000 | 7.71 | 11.90 | 9881.20 | 4.00 | 87523 |
| 2001 | 7.82 | 11.50 | 18026.10 | 5.50 | 87656 |
| 2002 | 7.95 | 11.70 | 18717.00 | 6.40 | 89679 |
| 2003 | 8.24 | 12.10 | 19067.10 | 3.20 | 94275 |
| 2004 | 8.23 | 12.50 | 18867.30 | 6.20 | 97895 |
| 2005 | 7.91 | 12.60 | 18941.10 | 2.50 | 103860 |
| 2006 | 7.64 | 13.20 | 20537.30 | 3.00 | 107914 |
| 2007 | 7.54 | 13.60 | 21463.00 | 3.50 | 110977 |
| 2008 | 7.91 | 13.30 | 21359.40 | 2.20 | 79910 |
| 2009 | 8.23 | 11.30 | 17624.50 | 1.60 | 75109 |
| 2010 | 8.22 | 11.50 | 20643.40 | 1.50 | |

APPENDIX B. Model estimates

B.1 In-sample

| Year | IPD Rents (1st.dif) | ARIMA Order | | | | |
|------|------------------------|-------------|--------|--------|--------|--------|
| | | 100 | 101 | 102 | 103 | 104 |
| 1964 | 3.21 | 0.048 | 0.123 | -0.167 | -0.175 | -0.169 |
| 1965 | -1.19 | 1.342 | 1.483 | 0.792 | 0.855 | 0.994 |
| 1966 | -0.97 | -0.461 | -1.575 | -2.130 | -2.350 | -2.324 |
| 1967 | -0.80 | -0.370 | 0.709 | 0.333 | 0.364 | 0.163 |
| 1968 | -0.68 | -0.302 | -0.988 | -1.242 | -1.335 | -1.240 |
| 1969 | -5.46 | -0.249 | 0.474 | 0.301 | 0.318 | 0.228 |
| 1970 | 7.08 | -2.209 | -4.303 | -3.357 | -3.694 | -3.676 |
| 1971 | 7.87 | 2.933 | 9.229 | 8.012 | 8.988 | 8.503 |
| 1972 | -2.58 | 3.253 | -1.965 | -4.072 | -4.713 | -3.532 |
| 1973 | 6.15 | -1.028 | -0.112 | -1.455 | -1.601 | -2.050 |
| 1974 | 1.70 | 2.551 | 5.058 | 2.012 | 2.295 | 2.276 |
| 1975 | -13.97 | 0.725 | -3.095 | -5.512 | -6.300 | -5.484 |
| 1976 | -7.10 | -5.700 | -8.149 | -7.618 | -8.295 | -8.764 |
| 1977 | 3.10 | -2.881 | 1.911 | 3.197 | 3.694 | 2.956 |
| 1978 | 5.10 | 1.299 | 0.871 | 1.233 | 1.349 | 1.830 |
| 1979 | 4.80 | 2.119 | 3.440 | 2.872 | 3.144 | 3.151 |
| 1980 | -2.10 | 1.996 | 0.840 | -0.815 | -0.933 | -0.668 |
| 1981 | -4.58 | -0.833 | -2.339 | -2.977 | -3.339 | -3.243 |
| 1982 | -4.16 | -1.849 | -1.411 | -1.502 | -1.564 | -1.831 |
| 1983 | -0.93 | -1.676 | -1.932 | -0.970 | -1.085 | -1.060 |
| 1984 | 1.39 | -0.352 | 1.176 | 1.821 | 2.094 | 1.883 |
| 1985 | 2.26 | 0.599 | 0.178 | 0.683 | 0.688 | 0.900 |
| 1986 | 3.37 | 0.954 | 1.815 | 1.598 | 1.804 | 1.712 |
| 1987 | 9.41 | 1.411 | 1.201 | 0.388 | 0.355 | 0.576 |
| 1988 | 3.56 | 3.886 | 6.712 | 3.596 | 3.995 | 3.985 |
| 1989 | -7.77 | 1.490 | -3.207 | -6.390 | -7.250 | -6.393 |
| 1990 | -12.30 | -3.157 | -3.231 | -4.456 | -4.792 | -5.291 |
| 1991 | -11.30 | -5.013 | -6.921 | -5.753 | -6.349 | -6.362 |
| 1992 | -3.40 | -4.604 | -2.659 | 0.851 | 1.109 | 0.482 |
| 1993 | 4.05 | -1.365 | -0.165 | 3.193 | 3.513 | 3.466 |
| 1994 | 6.94 | 1.690 | 3.616 | 6.217 | 6.890 | 6.751 |
| 1995 | 1.31 | 2.873 | 2.450 | 3.065 | 3.261 | 3.601 |
| 1996 | 2.81 | 0.566 | -1.077 | 0.000 | -0.021 | 0.014 |
| 1997 | 4.49 | 1.180 | 3.452 | 3.168 | 3.493 | 3.302 |
| 1998 | -0.34 | 1.868 | 0.593 | -0.177 | -0.263 | 0.116 |
| 1999 | -1.65 | -0.113 | -0.701 | -1.515 | -1.708 | -1.668 |
| 2000 | 1.33 | -0.649 | -0.563 | -0.853 | -0.915 | -1.019 |

| Year | ARIMA Order | | | | | |
|------|-------------|--------|--------|---------|--------|--------|
| | 200 | 201 | 202 | 203 | 204 | 300 |
| 1964 | 0.029 | 0.118 | -0.184 | -0.295 | -0.215 | 0.029 |
| 1965 | 1.357 | 1.415 | 0.944 | 1.050 | 1.150 | 1.357 |
| 1966 | -2.051 | -1.736 | -2.555 | -2.536 | -2.203 | -2.051 |
| 1967 | -0.046 | 0.875 | 0.302 | -0.005 | -0.478 | -0.046 |
| 1968 | -0.042 | -1.049 | -1.398 | -1.705 | -1.834 | -0.042 |
| 1969 | -0.037 | 0.564 | 0.294 | -0.073 | -0.025 | -0.037 |
| 1970 | -2.940 | -4.546 | -3.925 | -4.199 | -2.961 | -2.939 |
| 1971 | 6.570 | 10.247 | 9.625 | 8.672 | 7.200 | 6.569 |
| 1972 | 1.698 | -3.158 | -4.936 | -4.595 | -2.850 | 1.699 |
| 1973 | -4.859 | 0.149 | -1.982 | -2.439 | -1.672 | -4.860 |
| 1974 | 4.788 | 5.370 | 2.402 | 0.919 | -0.054 | 4.787 |
| 1975 | -1.582 | -3.885 | -6.892 | -7.726 | -6.726 | -1.581 |
| 1976 | -9.026 | -8.308 | -9.033 | -10.232 | -8.934 | -9.026 |
| 1977 | 1.741 | 2.999 | 3.896 | 1.794 | 0.994 | 1.741 |
| 1978 | 4.892 | 0.636 | 1.660 | 0.372 | 1.337 | 4.894 |
| 1979 | 1.745 | 3.677 | 3.357 | 2.287 | 4.319 | 1.746 |
| 1980 | 0.715 | 0.399 | -0.945 | -1.885 | 0.627 | 0.715 |
| 1981 | -3.270 | -2.494 | -3.689 | -4.344 | -2.816 | -3.271 |
| 1982 | -1.811 | -1.323 | -1.697 | -2.827 | -2.951 | -1.811 |
| 1983 | -0.504 | -1.850 | -1.163 | -1.816 | -2.146 | -0.504 |
| 1984 | 1.241 | 1.447 | 2.311 | 1.440 | 1.464 | 1.241 |
| 1985 | 1.249 | 0.067 | 0.803 | 0.628 | 1.745 | 1.249 |
| 1986 | 0.778 | 1.946 | 1.964 | 1.527 | 2.586 | 0.779 |
| 1987 | 1.073 | 1.061 | 0.374 | 0.051 | 0.914 | 1.073 |
| 1988 | 4.198 | 7.170 | 4.157 | 2.104 | 2.544 | 4.198 |
| 1989 | -1.856 | -4.408 | -7.829 | -9.290 | -6.965 | -1.856 |
| 1990 | -6.124 | -2.854 | -5.413 | -8.020 | -6.597 | -6.124 |
| 1991 | -3.999 | -7.390 | -6.787 | -8.651 | -7.747 | -3.999 |
| 1992 | -1.477 | -1.740 | 1.171 | -0.494 | -0.496 | -1.476 |
| 1993 | 2.808 | -0.224 | 4.041 | 3.674 | 4.326 | 2.809 |
| 1994 | 3.886 | 4.279 | 7.510 | 7.801 | 8.949 | 3.888 |
| 1995 | 2.435 | 1.857 | 3.732 | 5.056 | 6.485 | 2.436 |
| 1996 | -2.146 | -1.095 | -0.012 | 2.137 | 2.197 | -2.146 |
| 1997 | 1.140 | 3.603 | 3.758 | 5.158 | 2.969 | 1.139 |
| 1998 | 1.505 | 0.428 | -0.300 | 1.151 | -0.850 | 1.504 |
| 1999 | -2.091 | -0.984 | -1.879 | -0.693 | -2.175 | -2.091 |
| 2000 | -0.813 | -0.363 | -1.090 | -0.447 | -1.701 | -0.814 |

| Year | ARIMA Order | | | | | |
|------|-------------|--------|--------|--------|--------|--------|
| | 301 | 302 | 304 | 304 | 400 | 401 |
| 1964 | -0.224 | -0.213 | -0.223 | -0.187 | -0.048 | -0.044 |
| 1965 | 1.217 | 1.164 | 1.162 | 0.970 | 1.263 | 1.270 |
| 1966 | -2.441 | -2.535 | -2.475 | -2.059 | -2.088 | -2.090 |
| 1967 | -1.026 | -0.325 | -0.315 | -0.280 | -0.018 | -0.018 |
| 1968 | -0.694 | -1.361 | -1.566 | -1.384 | -1.913 | -1.913 |
| 1969 | -0.464 | 0.040 | 0.000 | 0.642 | 0.370 | 0.450 |
| 1970 | -2.399 | -3.529 | -3.576 | -3.251 | -2.612 | -2.710 |
| 1971 | 5.117 | 7.925 | 7.943 | 6.812 | 7.940 | 8.074 |
| 1972 | 1.019 | -2.642 | -3.207 | -2.712 | -1.456 | -1.504 |
| 1973 | -5.558 | -3.046 | -2.608 | -0.691 | -1.739 | -1.651 |
| 1974 | 0.522 | 1.062 | 0.587 | 0.413 | 4.178 | 4.187 |
| 1975 | -4.408 | -5.965 | -6.690 | -5.345 | -7.947 | -7.958 |
| 1976 | -9.828 | -9.878 | -9.863 | -6.894 | -6.200 | -6.078 |
| 1977 | -0.105 | 1.869 | 1.594 | 1.510 | 2.346 | 2.238 |
| 1978 | 4.647 | 2.486 | 1.797 | 0.977 | 1.149 | 1.150 |
| 1979 | 2.488 | 3.535 | 3.614 | 4.594 | 5.797 | 5.975 |
| 1980 | 0.252 | -0.456 | -0.440 | 0.289 | 4.033 | 3.879 |
| 1981 | -3.752 | -3.559 | -3.397 | -4.343 | -4.433 | -4.619 |
| 1982 | -2.789 | -2.496 | -2.449 | -3.211 | -2.468 | -2.421 |
| 1983 | -0.738 | -1.125 | -1.291 | -0.111 | -2.625 | -2.626 |
| 1984 | 1.611 | 1.889 | 1.884 | 3.152 | 1.748 | 1.843 |
| 1985 | 2.063 | 1.483 | 1.445 | 0.380 | 2.393 | 2.368 |
| 1986 | 1.378 | 1.837 | 2.060 | 0.331 | 2.189 | 2.153 |
| 1987 | 0.740 | 0.708 | 0.738 | 0.891 | 1.367 | 1.342 |
| 1988 | 1.383 | 3.109 | 3.001 | 4.767 | 3.309 | 3.417 |
| 1989 | -4.770 | -6.732 | -7.286 | -5.394 | -4.233 | -4.203 |
| 1990 | -8.780 | -7.118 | -7.113 | -6.474 | -5.750 | -5.724 |
| 1991 | -5.735 | -7.111 | -7.659 | -7.492 | -5.902 | -6.006 |
| 1992 | -0.462 | 0.073 | -0.034 | 1.071 | -2.945 | -2.951 |
| 1993 | 5.754 | 4.677 | 4.544 | 4.650 | 5.432 | 5.475 |
| 1994 | 7.899 | 8.125 | 8.572 | 6.183 | 7.271 | 7.164 |
| 1995 | 6.012 | 5.266 | 5.791 | 2.708 | 6.072 | 5.962 |
| 1996 | 1.095 | 0.903 | 1.777 | 0.525 | -0.834 | -1.015 |
| 1997 | 1.879 | 3.335 | 3.934 | 3.284 | 0.880 | 0.900 |
| 1998 | 1.104 | 0.272 | 0.341 | -0.016 | -2.374 | -2.311 |
| 1999 | -2.383 | -1.976 | -1.814 | -1.547 | -3.002 | -2.848 |
| 2000 | -1.973 | -1.646 | -1.659 | -1.356 | -0.819 | -0.775 |

| Year | ARIMA Order | | | ARIMAX Order | | |
|------|-------------|--------|--------|--------------|--------|--------|
| | 402 | 403 | 404 | Bank Rate | 101 | 102 |
| | | | | 100 | | |
| 1964 | -0.249 | -0.249 | -0.234 | 0.376 | 0.129 | 0.010 |
| 1965 | 1.113 | 1.124 | 1.066 | 1.207 | 1.480 | 0.709 |
| 1966 | -2.304 | -2.304 | -2.307 | -0.305 | -1.580 | -1.959 |
| 1967 | -0.138 | -0.162 | -0.176 | -0.554 | 0.698 | 0.204 |
| 1968 | -2.094 | -2.186 | -2.210 | -0.131 | -0.989 | -1.023 |
| 1969 | -0.018 | 0.044 | 0.376 | -0.192 | 0.471 | 0.251 |
| 1970 | -3.687 | -3.580 | -3.173 | -2.427 | -4.353 | -3.245 |
| 1971 | 8.111 | 7.845 | 7.876 | 2.712 | 9.323 | 7.758 |
| 1972 | -4.080 | -3.429 | -3.612 | 3.494 | -2.040 | -3.952 |
| 1973 | -1.926 | -2.467 | -1.177 | -0.531 | -0.043 | -1.353 |
| 1974 | 1.094 | 1.885 | 1.517 | 2.840 | 5.067 | 2.136 |
| 1975 | -8.969 | -9.840 | -9.246 | 0.298 | -3.137 | -5.722 |
| 1976 | -8.231 | -7.378 | -7.085 | -5.545 | -8.238 | -7.196 |
| 1977 | 0.572 | 0.314 | 1.716 | -3.452 | 1.955 | 2.803 |
| 1978 | 0.727 | 0.464 | 0.030 | 1.513 | 0.840 | 1.702 |
| 1979 | 3.269 | 3.884 | 4.557 | 2.981 | 3.548 | 2.921 |
| 1980 | 0.732 | 0.969 | 2.703 | 1.829 | 0.769 | -0.629 |
| 1981 | -3.927 | -4.390 | -5.742 | -1.439 | -2.336 | -3.247 |
| 1982 | -1.635 | -1.507 | -3.673 | -1.686 | -1.463 | -1.137 |
| 1983 | -2.375 | -2.493 | -0.959 | -2.032 | -1.948 | -1.342 |
| 1984 | 2.001 | 1.889 | 3.514 | -0.211 | 1.191 | 2.266 |
| 1985 | 1.090 | 1.494 | 0.646 | 1.018 | 0.179 | 0.551 |
| 1986 | 2.261 | 1.909 | 1.279 | 0.510 | 1.829 | 1.691 |
| 1987 | 0.780 | 1.095 | 1.264 | 1.261 | 1.197 | 0.150 |
| 1988 | 2.295 | 1.936 | 3.108 | 4.049 | 6.841 | 3.637 |
| 1989 | -7.274 | -6.790 | -6.765 | 1.585 | -3.367 | -6.615 |
| 1990 | -7.334 | -7.634 | -7.181 | -2.579 | -3.148 | -3.987 |
| 1991 | -7.262 | -6.952 | -7.175 | -5.703 | -7.182 | -6.194 |
| 1992 | -1.705 | -2.271 | -1.782 | -5.128 | -2.540 | 1.204 |
| 1993 | 5.154 | 5.719 | 6.016 | -1.614 | -0.328 | 2.745 |
| 1994 | 7.561 | 7.391 | 8.188 | 1.897 | 3.835 | 6.630 |
| 1995 | 7.322 | 7.435 | 6.150 | 3.050 | 2.309 | 2.631 |
| 1996 | 1.946 | 1.850 | 0.061 | 0.402 | -0.969 | 0.263 |
| 1997 | 4.897 | 4.394 | 3.450 | 1.368 | 3.414 | 2.823 |
| 1998 | -0.498 | -0.393 | -0.557 | 1.855 | 0.652 | -0.022 |
| 1999 | -1.610 | -1.968 | -1.303 | -0.398 | -0.792 | -1.997 |
| 2000 | -1.700 | -1.285 | -1.502 | -0.479 | -0.504 | -0.569 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | Bank Rate | | | | | |
| | 103 | 104 | 200 | 201 | 202 | 203 |
| 1964 | -0.040 | 0.003 | 0.886 | 0.682 | 0.576 | 0.449 |
| 1965 | 0.808 | 0.928 | 0.976 | 1.135 | 0.776 | 0.835 |
| 1966 | -2.187 | -2.172 | -1.365 | -1.454 | -1.934 | -2.032 |
| 1967 | 0.255 | 0.025 | -0.596 | 0.331 | -0.416 | -0.494 |
| 1968 | -1.153 | -1.020 | 0.679 | -0.288 | -0.298 | -0.602 |
| 1969 | 0.260 | 0.166 | -0.071 | 0.060 | -0.143 | -0.109 |
| 1970 | -3.621 | -3.640 | -3.452 | -4.564 | -3.608 | -3.607 |
| 1971 | 8.732 | 8.359 | 6.481 | 10.004 | 8.715 | 8.630 |
| 1972 | -4.437 | -3.336 | 2.162 | -2.236 | -2.773 | -3.260 |
| 1973 | -1.506 | -2.000 | -4.285 | -0.965 | -3.223 | -2.762 |
| 1974 | 2.474 | 2.484 | 5.500 | 7.367 | 4.086 | 2.705 |
| 1975 | -6.286 | -5.655 | -2.501 | -5.668 | -7.902 | -8.147 |
| 1976 | -7.950 | -8.478 | -8.131 | -7.224 | -7.727 | -8.303 |
| 1977 | 3.241 | 2.546 | 0.318 | 1.357 | 1.566 | 1.272 |
| 1978 | 1.724 | 2.348 | 6.148 | 3.102 | 4.844 | 4.269 |
| 1979 | 3.125 | 3.223 | 3.364 | 2.779 | 3.294 | 3.603 |
| 1980 | -0.699 | -0.500 | -0.293 | 1.213 | 0.381 | 0.372 |
| 1981 | -3.501 | -3.516 | -4.119 | -4.246 | -4.783 | -4.695 |
| 1982 | -1.270 | -1.480 | -0.890 | -0.029 | -0.238 | -0.487 |
| 1983 | -1.425 | -1.457 | -1.936 | -3.369 | -2.386 | -2.446 |
| 1984 | 2.399 | 2.308 | 1.892 | 2.747 | 3.687 | 3.795 |
| 1985 | 0.536 | 0.771 | 1.970 | -0.061 | 1.363 | 1.187 |
| 1986 | 1.872 | 1.781 | -0.623 | 1.216 | 1.305 | 1.976 |
| 1987 | 0.206 | 0.388 | 1.290 | 1.232 | 0.888 | 0.499 |
| 1988 | 4.100 | 4.146 | 4.423 | 6.409 | 3.197 | 3.287 |
| 1989 | -7.201 | -6.578 | -2.237 | -3.615 | -6.717 | -7.668 |
| 1990 | -4.396 | -4.891 | -4.871 | -3.175 | -5.993 | -6.238 |
| 1991 | -6.682 | -6.905 | -5.912 | -7.112 | -7.016 | -8.061 |
| 1992 | 1.213 | 0.744 | -1.562 | -2.489 | 0.318 | 0.507 |
| 1993 | 3.018 | 2.989 | 2.420 | 0.341 | 4.552 | 4.429 |
| 1994 | 7.038 | 7.136 | 4.114 | 3.723 | 7.374 | 8.475 |
| 1995 | 2.894 | 3.168 | 2.255 | 2.390 | 4.421 | 4.905 |
| 1996 | 0.138 | 0.207 | -2.895 | -2.203 | -0.871 | 0.263 |
| 1997 | 3.195 | 2.979 | 1.844 | 4.236 | 3.781 | 3.829 |
| 1998 | -0.107 | 0.288 | 1.217 | 0.041 | -0.662 | -0.582 |
| 1999 | -2.028 | -2.163 | -2.852 | -1.546 | -2.984 | -2.946 |
| 2000 | -0.694 | -0.752 | -0.206 | 0.117 | -1.135 | -1.592 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | Bank Rate | | | | | |
| | 204 | 300 | 301 | 302 | 303 | 304 |
| 1964 | 0.010 | 0.904 | 0.671 | 0.085 | 0.126 | -0.001 |
| 1965 | 1.079 | 0.970 | 0.857 | 1.046 | 1.003 | 0.887 |
| 1966 | -2.055 | -1.353 | -1.734 | -2.299 | -2.221 | -1.876 |
| 1967 | -0.615 | -0.534 | -1.328 | -0.547 | -0.545 | -0.409 |
| 1968 | -1.550 | 0.679 | 0.184 | -0.998 | -1.000 | -1.167 |
| 1969 | -0.068 | -0.119 | -0.223 | -0.012 | -0.002 | 0.596 |
| 1970 | -3.007 | -3.543 | -2.784 | -3.470 | -3.430 | -3.178 |
| 1971 | 7.153 | 6.675 | 5.326 | 7.787 | 7.774 | 6.518 |
| 1972 | -2.727 | 1.982 | 1.598 | -2.384 | -2.641 | -2.443 |
| 1973 | -1.574 | -4.260 | -4.912 | -2.964 | -2.703 | -0.521 |
| 1974 | 0.277 | 5.902 | 1.628 | 1.290 | 1.174 | 0.453 |
| 1975 | -7.092 | -2.687 | -5.011 | -6.411 | -6.695 | -5.524 |
| 1976 | -8.741 | -8.178 | -8.714 | -9.423 | -9.185 | -6.371 |
| 1977 | 0.590 | 0.453 | -0.689 | 1.317 | 1.251 | 1.036 |
| 1978 | 1.955 | 5.981 | 6.275 | 3.367 | 3.257 | 1.342 |
| 1979 | 4.516 | 3.161 | 4.648 | 3.892 | 3.970 | 4.786 |
| 1980 | 0.834 | -0.242 | -0.080 | -0.217 | -0.169 | 0.564 |
| 1981 | -3.160 | -4.068 | -4.241 | -3.981 | -3.987 | -4.727 |
| 1982 | -2.381 | -0.791 | -1.302 | -1.874 | -1.721 | -2.899 |
| 1983 | -2.458 | -2.039 | -1.367 | -1.654 | -1.777 | -0.337 |
| 1984 | 2.017 | 1.889 | 2.544 | 2.623 | 2.782 | 3.573 |
| 1985 | 1.549 | 1.882 | 3.171 | 1.441 | 1.362 | 0.166 |
| 1986 | 2.630 | -0.660 | 0.348 | 1.930 | 2.056 | 0.342 |
| 1987 | 0.683 | 1.377 | 1.018 | 0.469 | 0.377 | 0.801 |
| 1988 | 2.893 | 4.535 | 1.965 | 3.330 | 3.355 | 4.895 |
| 1989 | -7.260 | -2.265 | -4.977 | -7.167 | -7.452 | -5.566 |
| 1990 | -6.184 | -4.729 | -7.514 | -6.614 | -6.356 | -6.123 |
| 1991 | -8.570 | -5.896 | -7.261 | -8.072 | -8.339 | -7.887 |
| 1992 | -0.284 | -1.683 | -0.595 | 0.492 | 0.675 | 1.301 |
| 1993 | 3.747 | 2.166 | 5.521 | 4.173 | 3.981 | 4.214 |
| 1994 | 9.495 | 3.921 | 7.986 | 8.867 | 9.124 | 6.440 |
| 1995 | 6.040 | 2.199 | 5.465 | 4.739 | 4.645 | 2.388 |
| 1996 | 2.471 | -2.869 | -0.302 | 1.115 | 1.395 | 0.719 |
| 1997 | 2.737 | 2.097 | 1.941 | 2.872 | 2.868 | 2.931 |
| 1998 | -0.618 | 1.242 | 0.431 | 0.376 | 0.368 | 0.065 |
| 1999 | -2.887 | -2.858 | -3.696 | -2.828 | -2.945 | -1.916 |
| 2000 | -1.574 | -0.074 | -1.942 | -1.386 | -1.296 | -1.125 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|---------|---------|---------|---------------------|
| | Bank Rate | | | | | Construction Orders |
| | 400 | 401 | 402 | 403 | 404 | 100 |
| 1964 | 0.651 | 0.649 | 0.567 | 0.604 | 0.596 | -3.526 |
| 1965 | 0.983 | 0.986 | 0.799 | 0.790 | 0.799 | -1.428 |
| 1966 | -1.555 | -1.557 | -1.657 | -1.628 | -1.657 | -2.441 |
| 1967 | -0.402 | -0.400 | -0.623 | -0.684 | -0.698 | 1.020 |
| 1968 | -0.883 | -0.886 | -0.942 | -0.932 | -0.968 | -0.200 |
| 1969 | 0.123 | 0.150 | -0.314 | -0.196 | -0.097 | 0.258 |
| 1970 | -2.859 | -2.903 | -3.311 | -3.263 | -3.154 | 4.260 |
| 1971 | 8.137 | 8.199 | 7.796 | 7.717 | 7.757 | 0.865 |
| 1972 | -1.363 | -1.392 | -3.289 | -2.767 | -2.562 | -1.098 |
| 1973 | -1.366 | -1.318 | -1.855 | -2.062 | -1.705 | -3.945 |
| 1974 | 5.487 | 5.485 | 2.852 | 3.451 | 3.424 | -1.767 |
| 1975 | -9.043 | -9.059 | -10.409 | -11.040 | -10.730 | -1.557 |
| 1976 | -5.764 | -5.686 | -6.981 | -6.135 | -6.145 | -1.768 |
| 1977 | 1.752 | 1.698 | -0.194 | -0.205 | 0.579 | 2.414 |
| 1978 | 2.797 | 2.785 | 2.743 | 2.465 | 2.235 | -0.880 |
| 1979 | 6.174 | 6.238 | 4.173 | 5.300 | 5.423 | 1.657 |
| 1980 | 3.711 | 3.642 | 1.795 | 1.660 | 2.642 | 1.677 |
| 1981 | -5.193 | -5.294 | -4.281 | -4.836 | -5.865 | -1.712 |
| 1982 | -2.065 | -2.035 | -0.436 | -0.468 | -1.239 | -1.028 |
| 1983 | -3.280 | -3.274 | -2.772 | -2.719 | -2.038 | 2.313 |
| 1984 | 2.798 | 2.838 | 3.465 | 3.381 | 3.524 | 0.466 |
| 1985 | 2.149 | 2.120 | 1.776 | 2.143 | 1.780 | 2.880 |
| 1986 | 1.237 | 1.235 | 1.883 | 1.464 | 1.565 | 6.650 |
| 1987 | 1.484 | 1.472 | 1.243 | 1.551 | 1.384 | 5.852 |
| 1988 | 3.278 | 3.334 | 1.955 | 1.740 | 2.060 | -0.194 |
| 1989 | -4.177 | -4.153 | -7.065 | -6.498 | -6.242 | -8.501 |
| 1990 | -4.814 | -4.807 | -6.530 | -6.622 | -6.253 | -7.340 |
| 1991 | -7.567 | -7.615 | -8.458 | -8.472 | -8.718 | -5.434 |
| 1992 | -2.787 | -2.776 | -1.685 | -1.886 | -1.926 | 0.085 |
| 1993 | 4.408 | 4.424 | 4.207 | 4.766 | 5.150 | 1.406 |
| 1994 | 7.858 | 7.813 | 8.416 | 8.365 | 8.716 | 2.518 |
| 1995 | 5.598 | 5.524 | 6.860 | 6.795 | 6.133 | 1.688 |
| 1996 | -1.829 | -1.913 | 1.505 | 0.878 | 0.119 | 2.626 |
| 1997 | 1.353 | 1.373 | 4.674 | 4.232 | 3.681 | 4.707 |
| 1998 | -2.678 | -2.643 | -1.280 | -1.400 | -1.440 | -4.830 |
| 1999 | -3.377 | -3.289 | -3.074 | -3.163 | -2.924 | 0.328 |
| 2000 | -0.357 | -0.335 | -1.841 | -1.479 | -1.276 | -3.526 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Orders | | | | | |
| | 101 | 102 | 103 | 104 | 200 | 201 |
| 1964 | -2.827 | -2.355 | -2.449 | -2.394 | -3.250 | -2.858 |
| 1965 | -1.050 | -1.163 | -1.191 | -1.138 | -1.331 | -1.170 |
| 1966 | -2.302 | -2.228 | -2.317 | -2.213 | -2.957 | -2.461 |
| 1967 | 1.157 | 0.334 | 0.360 | 0.335 | 0.704 | 1.113 |
| 1968 | -1.190 | -1.500 | -1.557 | -1.473 | -1.021 | -1.282 |
| 1969 | -0.811 | -1.074 | -1.031 | -1.170 | -0.154 | -0.492 |
| 1970 | 7.311 | 7.326 | 7.282 | 7.041 | 6.694 | 7.500 |
| 1971 | -1.534 | -3.512 | -3.439 | -2.796 | -0.671 | -2.476 |
| 1972 | -0.740 | -2.128 | -2.154 | -2.287 | -3.368 | -0.558 |
| 1973 | -0.182 | -1.122 | -1.241 | -1.361 | -1.834 | -0.264 |
| 1974 | -2.931 | -6.721 | -6.671 | -6.168 | -3.388 | -3.766 |
| 1975 | -6.087 | -7.745 | -7.714 | -7.857 | -5.596 | -5.847 |
| 1976 | 1.468 | 2.355 | 2.219 | 1.533 | 1.379 | 2.631 |
| 1977 | 1.840 | 1.783 | 1.823 | 2.004 | 5.531 | 1.624 |
| 1978 | 0.493 | 0.196 | 0.020 | 0.348 | -1.479 | 0.230 |
| 1979 | 2.183 | -0.179 | -0.097 | -0.056 | 0.908 | 1.847 |
| 1980 | -1.731 | -3.993 | -3.986 | -3.778 | -1.269 | -2.089 |
| 1981 | -0.938 | -1.407 | -1.421 | -1.809 | -1.637 | -0.278 |
| 1982 | -1.957 | -1.653 | -1.665 | -1.716 | 0.931 | -1.784 |
| 1983 | 3.120 | 3.337 | 3.318 | 3.211 | 3.429 | 3.413 |
| 1984 | -0.994 | -0.391 | -0.378 | -0.255 | 0.602 | -1.162 |
| 1985 | 4.469 | 3.953 | 3.930 | 3.877 | 3.090 | 4.620 |
| 1986 | 3.469 | 2.154 | 2.372 | 2.406 | 5.514 | 3.134 |
| 1987 | 8.295 | 6.085 | 6.023 | 6.060 | 5.415 | 8.326 |
| 1988 | -4.354 | -6.383 | -6.047 | -5.958 | -1.660 | -4.841 |
| 1989 | -6.127 | -5.592 | -5.863 | -5.954 | -8.422 | -5.544 |
| 1990 | -8.546 | -6.456 | -6.210 | -6.735 | -4.689 | -8.071 |
| 1991 | -3.991 | -0.210 | -0.584 | -0.479 | -3.511 | -3.560 |
| 1992 | 0.439 | 3.843 | 4.033 | 3.649 | 2.204 | 0.761 |
| 1993 | 2.467 | 5.078 | 4.712 | 5.264 | 1.622 | 2.046 |
| 1994 | 2.977 | 3.513 | 3.715 | 3.622 | 1.538 | 2.727 |
| 1995 | -0.610 | -0.539 | -0.712 | -0.239 | -0.966 | -1.148 |
| 1996 | 4.582 | 4.142 | 4.257 | 3.843 | 2.354 | 4.938 |
| 1997 | 2.286 | 0.729 | 0.742 | 1.103 | 4.031 | 1.735 |
| 1998 | -4.469 | -4.040 | -4.051 | -4.185 | -5.817 | -4.216 |
| 1999 | 2.120 | 0.989 | 0.957 | 0.909 | 1.956 | 2.207 |
| 2000 | -2.827 | -2.355 | -2.449 | -2.394 | -3.250 | -2.858 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Orders | | | | | |
| | 202 | 203 | 204 | 300 | 301 | 302 |
| 1964 | -2.323 | -2.375 | -1.914 | | | |
| 1965 | -1.149 | -1.171 | -0.958 | -3.244 | -3.014 | -2.080 |
| 1966 | -2.208 | -2.247 | -1.708 | -1.327 | -1.240 | -1.017 |
| 1967 | 0.320 | 0.336 | 0.179 | -2.951 | -2.739 | -1.919 |
| 1968 | -1.525 | -1.509 | -1.215 | 0.768 | 1.004 | 0.230 |
| 1969 | -1.159 | -1.051 | -1.600 | -1.024 | -1.364 | -1.358 |
| 1970 | 7.532 | 7.286 | 6.774 | -0.161 | -0.310 | -1.594 |
| 1971 | -3.664 | -3.492 | -2.322 | 6.779 | 7.534 | 7.384 |
| 1972 | -2.205 | -2.130 | -2.022 | -0.808 | -2.152 | -2.680 |
| 1973 | -1.019 | -1.179 | -1.528 | -3.294 | -1.782 | -2.831 |
| 1974 | -6.933 | -6.707 | -6.836 | -1.592 | -0.657 | -1.038 |
| 1975 | -8.022 | -7.725 | -8.324 | -3.432 | -3.900 | -6.646 |
| 1976 | 2.478 | 2.329 | 0.454 | -5.605 | -6.257 | -8.852 |
| 1977 | 1.814 | 1.776 | 1.584 | 1.574 | 2.815 | 1.306 |
| 1978 | 0.275 | 0.172 | 1.756 | 5.359 | 3.251 | 2.317 |
| 1979 | -0.233 | -0.187 | 0.610 | -1.668 | -0.432 | 0.774 |
| 1980 | -4.186 | -3.973 | -3.825 | 1.023 | 1.401 | -0.160 |
| 1981 | -1.449 | -1.418 | -2.816 | -1.261 | -2.204 | -4.208 |
| 1982 | -1.695 | -1.651 | -2.522 | -1.520 | -0.643 | -2.283 |
| 1983 | 3.393 | 3.337 | 2.876 | 0.893 | -0.658 | -1.760 |
| 1984 | -0.410 | -0.398 | 0.638 | 3.287 | 3.622 | 3.074 |
| 1985 | 4.004 | 3.967 | 3.939 | 0.499 | -0.604 | 0.098 |
| 1986 | 2.022 | 2.171 | 2.049 | 3.093 | 4.223 | 3.660 |
| 1987 | 6.124 | 6.113 | 5.028 | 5.484 | 3.763 | 2.124 |
| 1988 | -6.698 | -6.376 | -6.425 | 5.484 | 7.416 | 5.426 |
| 1989 | -5.607 | -5.573 | -6.450 | -1.676 | -4.153 | -6.471 |
| 1990 | -6.580 | -6.492 | -7.486 | -8.397 | -6.521 | -6.587 |
| 1991 | -0.027 | -0.196 | -0.418 | -4.703 | -6.703 | -6.815 |
| 1992 | 3.954 | 3.792 | 4.423 | -3.713 | -3.266 | -0.098 |
| 1993 | 5.326 | 5.093 | 7.163 | 2.105 | 1.598 | 4.440 |
| 1994 | 3.547 | 3.469 | 5.046 | 1.516 | 1.915 | 6.376 |
| 1995 | -0.562 | -0.502 | 0.656 | 1.583 | 2.253 | 4.290 |
| 1996 | 4.163 | 4.113 | 3.223 | -0.915 | -1.505 | 0.066 |
| 1997 | 0.627 | 0.770 | 0.304 | 2.536 | 4.184 | 3.702 |
| 1998 | -4.111 | -4.077 | -3.873 | 4.053 | 2.334 | 0.880 |
| 1999 | 0.975 | 1.022 | 0.036 | -5.841 | -4.914 | -4.220 |
| 2000 | -2.323 | -2.375 | -1.914 | 2.076 | 2.369 | 0.364 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Orders | | | | | |
| | 303 | 304 | 400 | 401 | 402 | 403 |
| 1964 | | | | | | |
| 1965 | -2.638 | -2.141 | -2.329 | -2.312 | -1.428 | -2.436 |
| 1966 | -0.935 | -1.062 | -1.024 | -1.018 | -0.866 | -0.967 |
| 1967 | -2.280 | -1.944 | -2.096 | -2.077 | -1.277 | -2.166 |
| 1968 | 0.830 | 0.238 | 0.563 | 0.556 | 0.055 | 0.792 |
| 1969 | -1.382 | -1.301 | -1.578 | -1.573 | -0.968 | -1.496 |
| 1970 | -0.848 | -1.213 | -0.970 | -1.080 | -2.232 | -0.730 |
| 1971 | 7.277 | 6.942 | 7.287 | 7.612 | 8.084 | 7.676 |
| 1972 | -0.709 | -2.553 | -2.428 | -2.517 | -3.707 | -2.420 |
| 1973 | -0.880 | -1.721 | -1.084 | -0.875 | -1.425 | 0.043 |
| 1974 | -1.490 | -1.781 | -0.551 | -0.522 | -0.116 | -1.040 |
| 1975 | -3.922 | -6.188 | -7.737 | -7.539 | -8.708 | -5.559 |
| 1976 | -6.254 | -6.787 | -5.385 | -5.169 | -8.172 | -5.992 |
| 1977 | 1.509 | 1.185 | 2.025 | 1.782 | 0.594 | 3.079 |
| 1978 | 3.518 | 1.018 | 1.464 | 1.486 | 0.512 | 2.289 |
| 1979 | 2.490 | 1.705 | 2.529 | 3.067 | 1.815 | 2.415 |
| 1980 | 2.710 | 0.690 | 4.652 | 4.301 | 0.699 | 2.958 |
| 1981 | -1.908 | -4.546 | -3.956 | -4.576 | -4.495 | -1.894 |
| 1982 | -2.660 | -2.729 | -2.040 | -1.787 | -1.760 | -1.437 |
| 1983 | -2.850 | -1.095 | -1.798 | -1.908 | -2.912 | -3.486 |
| 1984 | 2.952 | 4.097 | 3.093 | 3.346 | 2.497 | 2.486 |
| 1985 | 0.830 | -0.461 | 2.632 | 2.451 | 0.379 | 0.406 |
| 1986 | 5.799 | 2.716 | 4.141 | 3.898 | 3.260 | 6.486 |
| 1987 | 4.895 | 2.388 | 3.927 | 3.698 | 1.737 | 4.840 |
| 1988 | 7.126 | 6.575 | 4.949 | 5.177 | 3.972 | 7.383 |
| 1989 | -5.013 | -6.076 | -3.744 | -3.868 | -6.918 | -6.050 |
| 1990 | -7.504 | -6.557 | -7.623 | -7.582 | -7.258 | -6.852 |
| 1991 | -8.034 | -7.047 | -5.243 | -5.461 | -7.013 | -7.803 |
| 1992 | -2.281 | 0.389 | -3.343 | -3.457 | -1.771 | -1.947 |
| 1993 | 2.997 | 4.020 | 5.953 | 5.993 | 5.531 | 3.884 |
| 1994 | 4.169 | 4.957 | 4.523 | 4.079 | 6.465 | 4.332 |
| 1995 | 2.714 | 3.363 | 4.432 | 4.347 | 6.871 | 3.472 |
| 1996 | -2.197 | 0.270 | -1.610 | -2.007 | 0.827 | -2.593 |
| 1997 | 1.223 | 3.739 | 1.409 | 1.654 | 5.061 | 1.615 |
| 1998 | 0.243 | 0.444 | -0.431 | -0.301 | -0.519 | -1.824 |
| 1999 | -4.256 | -3.658 | -5.682 | -5.314 | -3.096 | -4.170 |
| 2000 | 3.450 | 0.837 | 1.847 | 2.002 | -0.868 | 3.262 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------------------|--------|--------|--------|--------|
| | Construction Orders | Construction Costs | | | | |
| | 404 | 100 | 101 | 102 | 103 | 104 |
| 1964 | | 0.053 | 0.124 | -0.165 | -0.171 | -0.165 |
| 1965 | -2.290 | 1.350 | 1.548 | 0.778 | 0.878 | 0.998 |
| 1966 | -0.937 | -0.439 | -1.675 | -2.152 | -2.413 | -2.384 |
| 1967 | -2.016 | -0.348 | 0.709 | 0.311 | 0.355 | 0.155 |
| 1968 | 0.793 | -0.326 | -1.012 | -1.216 | -1.331 | -1.215 |
| 1969 | -1.436 | -0.234 | 0.459 | 0.273 | 0.280 | 0.183 |
| 1970 | -0.916 | -2.225 | -4.535 | -3.282 | -3.755 | -3.668 |
| 1971 | 7.626 | 2.922 | 9.826 | 7.964 | 9.226 | 8.644 |
| 1972 | -2.022 | 3.310 | -2.236 | -4.135 | -4.856 | -3.685 |
| 1973 | -0.484 | -1.063 | 0.043 | -1.427 | -1.503 | -1.984 |
| 1974 | 0.705 | 2.449 | 5.368 | 2.041 | 2.554 | 2.503 |
| 1975 | -7.271 | 0.578 | -3.128 | -5.342 | -6.156 | -5.306 |
| 1976 | -4.019 | -5.549 | -8.907 | -7.708 | -8.617 | -9.045 |
| 1977 | 2.033 | -2.962 | 2.386 | 3.507 | 4.156 | 3.499 |
| 1978 | 1.840 | 1.533 | 0.338 | 0.852 | 0.806 | 1.256 |
| 1979 | 2.598 | 1.833 | 4.428 | 3.489 | 4.079 | 4.107 |
| 1980 | 3.856 | 1.840 | 0.417 | -1.030 | -1.263 | -0.974 |
| 1981 | -2.801 | -0.540 | -2.272 | -2.806 | -3.093 | -3.057 |
| 1982 | -0.913 | -1.800 | -1.865 | -1.685 | -1.842 | -2.050 |
| 1983 | -3.554 | -1.508 | -1.987 | -0.962 | -1.125 | -1.088 |
| 1984 | 1.101 | -0.472 | 1.227 | 1.848 | 2.130 | 1.951 |
| 1985 | 2.196 | 0.543 | 0.268 | 0.745 | 0.713 | 0.947 |
| 1986 | 4.054 | 1.172 | 1.674 | 1.337 | 1.529 | 1.352 |
| 1987 | 6.598 | 1.294 | 1.547 | 0.594 | 0.668 | 0.923 |
| 1988 | 5.390 | 3.867 | 7.039 | 3.306 | 3.864 | 3.731 |
| 1989 | -3.741 | 1.283 | -3.208 | -5.988 | -6.756 | -5.853 |
| 1990 | -8.292 | -3.250 | -3.451 | -4.598 | -5.024 | -5.509 |
| 1991 | -5.816 | -4.673 | -7.761 | -5.729 | -6.493 | -6.456 |
| 1992 | -4.361 | -4.519 | -2.690 | 0.751 | 0.857 | 0.309 |
| 1993 | 5.110 | -1.247 | -0.543 | 3.141 | 3.317 | 3.318 |
| 1994 | 3.135 | 1.533 | 4.345 | 6.324 | 7.031 | 6.907 |
| 1995 | 3.810 | 2.811 | 2.248 | 3.030 | 3.164 | 3.502 |
| 1996 | -1.505 | 0.740 | -0.999 | -0.133 | -0.243 | -0.251 |
| 1997 | 0.228 | 1.064 | 3.686 | 3.279 | 3.720 | 3.546 |
| 1998 | -0.175 | 1.670 | 0.843 | -0.107 | -0.192 | 0.209 |
| 1999 | -6.148 | -0.098 | -0.880 | -1.467 | -1.657 | -1.639 |
| 2000 | 4.577 | -0.618 | -0.479 | -0.824 | -0.871 | -0.960 |

| Year | ARIMAX Order | | | | | |
|------|--------------------|--------|--------|--------|--------|--------|
| | Construction Costs | | | | | |
| | 200 | 201 | 202 | 203 | 204 | 300 |
| 1964 | 0.022 | -0.236 | -0.186 | -0.161 | -0.213 | 0.022 |
| 1965 | 1.349 | 1.160 | 0.969 | 0.776 | 1.117 | 1.347 |
| 1966 | -2.122 | -2.136 | -2.644 | -2.248 | -2.175 | -2.121 |
| 1967 | -0.071 | -1.344 | 0.265 | 0.354 | -0.501 | -0.068 |
| 1968 | -0.003 | -0.792 | -1.388 | -1.269 | -1.831 | -0.002 |
| 1969 | -0.087 | -0.578 | 0.224 | 0.314 | -0.074 | -0.088 |
| 1970 | -2.918 | -1.915 | -3.969 | -3.461 | -2.770 | -2.914 |
| 1971 | 6.656 | 3.910 | 9.839 | 8.643 | 6.991 | 6.654 |
| 1972 | 1.575 | 1.056 | -5.083 | -4.890 | -2.888 | 1.559 |
| 1973 | -4.843 | -4.720 | -1.900 | -0.985 | -1.557 | -4.835 |
| 1974 | 4.981 | -0.915 | 2.646 | 2.104 | -0.131 | 4.991 |
| 1975 | -1.394 | -4.246 | -6.668 | -5.503 | -6.597 | -1.394 |
| 1976 | -9.335 | -9.193 | -9.494 | -8.133 | -8.856 | -9.328 |
| 1977 | 2.137 | -1.017 | 4.537 | 4.248 | 1.241 | 2.160 |
| 1978 | 4.484 | 3.577 | 0.914 | 0.219 | 0.971 | 4.457 |
| 1979 | 2.329 | 3.490 | 4.684 | 4.601 | 4.934 | 2.335 |
| 1980 | 0.740 | 0.827 | -1.491 | -1.620 | 0.679 | 0.740 |
| 1981 | -3.746 | -3.582 | -3.297 | -2.507 | -2.573 | -3.754 |
| 1982 | -1.649 | -2.715 | -2.112 | -2.059 | -3.133 | -1.635 |
| 1983 | -0.874 | -1.123 | -1.159 | -0.951 | -2.243 | -0.884 |
| 1984 | 1.450 | 1.675 | 2.324 | 1.991 | 1.459 | 1.453 |
| 1985 | 1.180 | 2.178 | 0.850 | 0.693 | 1.884 | 1.173 |
| 1986 | 0.400 | 1.090 | 1.532 | 1.318 | 2.408 | 0.387 |
| 1987 | 1.383 | 0.879 | 0.812 | 0.716 | 1.096 | 1.390 |
| 1988 | 4.094 | 0.421 | 3.842 | 3.626 | 2.100 | 4.085 |
| 1989 | -1.540 | -4.476 | -7.163 | -6.281 | -6.640 | -1.531 |
| 1990 | -6.061 | -8.479 | -5.825 | -4.450 | -6.657 | -6.045 |
| 1991 | -4.458 | -6.694 | -6.980 | -6.456 | -7.675 | -4.457 |
| 1992 | -1.352 | -0.717 | 0.886 | 1.066 | -0.584 | -1.345 |
| 1993 | 2.537 | 5.366 | 3.769 | 2.714 | 4.319 | 2.521 |
| 1994 | 4.106 | 8.475 | 7.759 | 7.020 | 9.103 | 4.099 |
| 1995 | 2.358 | 6.746 | 3.524 | 2.633 | 6.562 | 2.346 |
| 1996 | -2.469 | 1.902 | -0.272 | -0.090 | 2.088 | -2.477 |
| 1997 | 1.461 | 2.073 | 3.980 | 3.479 | 2.875 | 1.475 |
| 1998 | 1.729 | 1.209 | -0.209 | -0.090 | -0.995 | 1.733 |
| 1999 | -2.178 | -2.152 | -1.892 | -1.493 | -2.223 | -2.177 |
| 2000 | -0.721 | -2.209 | -1.029 | -0.778 | -1.665 | -0.712 |

| Year | ARIMAX Order | | | | | |
|------|--------------------|--------|--------|--------|--------|--------|
| | Construction Costs | | | | | |
| | 301 | 302 | 303 | 304 | 400 | 401 |
| 1964 | 0.088 | -0.206 | -0.228 | -0.183 | -0.047 | -0.044 |
| 1965 | 1.394 | 1.172 | 1.049 | 0.966 | 1.263 | 1.270 |
| 1966 | -2.107 | -2.495 | -2.450 | -2.061 | -2.079 | -2.082 |
| 1967 | 0.713 | -0.405 | -0.207 | -0.286 | -0.016 | -0.016 |
| 1968 | -0.789 | -1.294 | -1.509 | -1.367 | -1.918 | -1.918 |
| 1969 | 0.471 | -0.028 | -0.040 | 0.623 | 0.376 | 0.453 |
| 1970 | -4.362 | -3.388 | -3.483 | -3.222 | -2.610 | -2.707 |
| 1971 | 10.250 | 7.571 | 7.923 | 6.798 | 7.925 | 8.058 |
| 1972 | -2.664 | -2.308 | -3.713 | -2.729 | -1.442 | -1.489 |
| 1973 | -1.272 | -2.992 | -2.317 | -0.630 | -1.732 | -1.650 |
| 1974 | 5.639 | 1.071 | 0.859 | 0.480 | 4.145 | 4.159 |
| 1975 | -3.567 | -5.394 | -6.388 | -5.188 | -7.973 | -7.983 |
| 1976 | -9.355 | -9.935 | -9.723 | -6.950 | -6.156 | -6.044 |
| 1977 | 4.019 | 1.944 | 2.511 | 1.694 | 2.288 | 2.187 |
| 1978 | 1.354 | 2.123 | 0.837 | 0.703 | 1.193 | 1.195 |
| 1979 | 4.158 | 4.286 | 4.639 | 5.036 | 5.715 | 5.889 |
| 1980 | -0.262 | -0.450 | -0.898 | 0.208 | 4.053 | 3.906 |
| 1981 | -2.854 | -3.340 | -3.025 | -4.281 | -4.404 | -4.587 |
| 1982 | -1.725 | -2.606 | -2.488 | -3.319 | -2.466 | -2.421 |
| 1983 | -1.404 | -1.108 | -1.194 | -0.046 | -2.584 | -2.588 |
| 1984 | 1.651 | 1.884 | 1.977 | 3.175 | 1.694 | 1.788 |
| 1985 | 0.471 | 1.591 | 1.361 | 0.333 | 2.422 | 2.400 |
| 1986 | 1.331 | 1.447 | 1.426 | 0.129 | 2.230 | 2.193 |
| 1987 | 1.421 | 1.039 | 0.997 | 1.139 | 1.353 | 1.329 |
| 1988 | 6.372 | 2.775 | 2.473 | 4.685 | 3.323 | 3.429 |
| 1989 | -3.945 | -5.885 | -6.657 | -5.178 | -4.285 | -4.255 |
| 1990 | -4.215 | -7.206 | -7.003 | -6.567 | -5.736 | -5.711 |
| 1991 | -6.679 | -7.123 | -7.487 | -7.436 | -5.868 | -5.970 |
| 1992 | -1.335 | -0.198 | -0.085 | 1.035 | -2.958 | -2.966 |
| 1993 | 0.904 | 4.456 | 4.125 | 4.488 | 5.463 | 5.504 |
| 1994 | 4.720 | 8.099 | 8.336 | 6.139 | 7.226 | 7.126 |
| 1995 | 1.832 | 5.226 | 5.178 | 2.723 | 6.109 | 6.004 |
| 1996 | -1.924 | 0.705 | 1.182 | 0.502 | -0.789 | -0.966 |
| 1997 | 3.459 | 3.357 | 4.069 | 3.328 | 0.859 | 0.879 |
| 1998 | 0.615 | 0.466 | 0.296 | -0.009 | -2.400 | -2.337 |
| 1999 | -1.462 | -1.913 | -1.782 | -1.483 | -3.012 | -2.863 |
| 2000 | -0.460 | -1.616 | -1.558 | -1.263 | -0.825 | -0.782 |

| Year | ARIMAX Order | | | | | |
|------|--------------------|--------|--------|---------------------|--------|--------|
| | Construction Costs | | | Construction Output | | |
| | 402 | 403 | 404 | 100 | 101 | 102 |
| 1964 | -0.245 | -0.248 | -0.222 | 0.092 | 0.079 | -0.179 |
| 1965 | 1.106 | 1.111 | 0.980 | 1.374 | 1.474 | 0.771 |
| 1966 | -2.386 | -2.357 | -2.317 | -0.600 | -1.547 | -2.145 |
| 1967 | -0.184 | -0.178 | -0.150 | -0.305 | 0.650 | 0.322 |
| 1968 | -2.036 | -2.145 | -2.032 | -0.574 | -0.835 | -1.261 |
| 1969 | -0.036 | -0.015 | 0.533 | -0.195 | 0.360 | 0.292 |
| 1970 | -3.672 | -3.520 | -3.292 | -2.180 | -4.333 | -3.344 |
| 1971 | 8.305 | 7.894 | 8.332 | 3.028 | 9.363 | 7.955 |
| 1972 | -4.394 | -3.652 | -4.771 | 2.943 | -1.891 | -4.131 |
| 1973 | -1.717 | -2.382 | -0.044 | -0.980 | -0.207 | -1.489 |
| 1974 | 1.079 | 1.890 | 0.900 | 2.152 | 5.499 | 1.905 |
| 1975 | -8.511 | -9.543 | -8.036 | 0.486 | -3.311 | -5.565 |
| 1976 | -8.643 | -7.683 | -7.927 | -5.900 | -8.081 | -7.623 |
| 1977 | 1.344 | 0.860 | 3.039 | -2.797 | 1.828 | 3.198 |
| 1978 | 0.193 | 0.095 | -0.417 | 1.460 | 0.933 | 1.203 |
| 1979 | 4.738 | 4.691 | 5.824 | 1.791 | 3.637 | 2.823 |
| 1980 | 0.387 | 0.906 | 0.974 | 1.950 | 0.807 | -0.884 |
| 1981 | -3.660 | -4.258 | -4.592 | -0.860 | -2.366 | -3.014 |
| 1982 | -1.785 | -1.489 | -4.609 | -1.584 | -1.629 | -1.532 |
| 1983 | -2.505 | -2.697 | -0.674 | -1.793 | -1.849 | -0.984 |
| 1984 | 2.579 | 2.397 | 4.340 | -0.211 | 1.025 | 1.797 |
| 1985 | 0.898 | 1.260 | 0.561 | 0.693 | 0.240 | 0.654 |
| 1986 | 2.086 | 1.792 | 0.029 | 1.118 | 1.681 | 1.556 |
| 1987 | 0.805 | 1.127 | 1.083 | 1.908 | 1.053 | 0.340 |
| 1988 | 2.173 | 1.698 | 5.155 | 4.109 | 6.864 | 3.486 |
| 1989 | -6.915 | -6.468 | -6.907 | 2.546 | -4.125 | -6.449 |
| 1990 | -7.396 | -7.749 | -7.451 | -2.960 | -3.045 | -4.510 |
| 1991 | -7.739 | -7.202 | -8.805 | -6.246 | -7.038 | -5.756 |
| 1992 | -1.495 | -2.140 | 0.946 | -5.388 | -2.127 | 0.864 |
| 1993 | 4.793 | 5.405 | 4.891 | -1.807 | -0.181 | 3.205 |
| 1994 | 8.185 | 7.856 | 8.040 | 1.924 | 3.919 | 6.205 |
| 1995 | 6.883 | 7.171 | 3.960 | 2.893 | 2.344 | 3.020 |
| 1996 | 1.569 | 1.634 | 0.853 | 0.916 | -1.206 | -0.021 |
| 1997 | 4.838 | 4.463 | 3.328 | 1.502 | 3.436 | 3.106 |
| 1998 | -0.443 | -0.370 | -0.745 | 2.015 | 0.463 | -0.237 |
| 1999 | -1.616 | -1.949 | -1.204 | 0.398 | -1.007 | -1.570 |
| 2000 | -1.769 | -1.358 | -1.140 | -1.003 | -0.329 | -0.914 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|---------|
| | Construction Output | | | | | |
| | 103 | 104 | 200 | 201 | 202 | 203 |
| 1964 | -0.202 | -0.188 | 0.108 | -0.242 | -0.165 | -0.424 |
| 1965 | 0.850 | 0.991 | 1.406 | 1.130 | 1.092 | 1.064 |
| 1966 | -2.301 | -2.340 | -2.257 | -2.040 | -2.661 | -2.378 |
| 1967 | 0.310 | 0.147 | 0.146 | -1.283 | 0.177 | -0.352 |
| 1968 | -1.158 | -1.192 | -0.484 | -0.842 | -1.462 | -1.106 |
| 1969 | 0.221 | 0.183 | 0.141 | -0.532 | 0.120 | -0.574 |
| 1970 | -3.637 | -3.707 | -3.021 | -1.917 | -3.734 | -3.939 |
| 1971 | 9.000 | 8.611 | 6.727 | 3.774 | 8.518 | 8.459 |
| 1972 | -4.440 | -3.524 | 1.129 | 1.110 | -3.038 | -3.554 |
| 1973 | -1.728 | -2.136 | -4.718 | -4.701 | -3.695 | -3.133 |
| 1974 | 2.860 | 2.524 | 4.123 | -1.133 | 2.891 | 2.483 |
| 1975 | -6.355 | -5.595 | -1.909 | -4.516 | -6.822 | -8.197 |
| 1976 | -7.926 | -8.733 | -9.427 | -8.884 | -9.206 | -8.930 |
| 1977 | 3.581 | 2.994 | 1.903 | -1.438 | 2.548 | 1.406 |
| 1978 | 1.665 | 1.925 | 4.962 | 3.708 | 2.645 | 1.827 |
| 1979 | 3.281 | 3.196 | 1.130 | 2.645 | 1.914 | 3.206 |
| 1980 | -0.628 | -0.595 | 0.743 | 0.354 | 0.032 | -0.302 |
| 1981 | -3.256 | -3.269 | -3.465 | -3.243 | -4.526 | -3.319 |
| 1982 | -1.475 | -1.822 | -1.439 | -2.916 | -1.449 | -1.684 |
| 1983 | -0.947 | -1.035 | -0.712 | -0.990 | -1.614 | -0.202 |
| 1984 | 2.092 | 1.882 | 1.640 | 1.330 | 2.126 | 2.602 |
| 1985 | 0.806 | 0.910 | 1.336 | 2.043 | 0.934 | 2.340 |
| 1986 | 1.749 | 1.682 | 1.037 | 1.482 | 1.589 | 2.570 |
| 1987 | 0.259 | 0.506 | 1.797 | 0.659 | 0.858 | 0.739 |
| 1988 | 4.005 | 4.006 | 4.463 | 0.464 | 3.127 | 2.456 |
| 1989 | -7.880 | -6.742 | -0.189 | -4.697 | -5.292 | -11.507 |
| 1990 | -4.874 | -5.384 | -5.855 | -8.514 | -6.851 | -8.963 |
| 1991 | -6.394 | -6.425 | -5.016 | -6.136 | -5.254 | -9.435 |
| 1992 | 1.198 | 0.501 | -1.750 | -0.769 | -0.521 | -1.047 |
| 1993 | 3.634 | 3.502 | 1.995 | 5.441 | 5.019 | 3.411 |
| 1994 | 6.862 | 6.751 | 3.722 | 8.114 | 6.352 | 7.118 |
| 1995 | 3.463 | 3.638 | 1.849 | 6.657 | 4.672 | 5.470 |
| 1996 | -0.256 | -0.123 | -1.792 | 2.321 | -0.301 | 1.344 |
| 1997 | 3.604 | 3.334 | 1.504 | 1.908 | 3.492 | 5.392 |
| 1998 | -0.481 | -0.001 | 1.787 | 0.921 | 0.243 | 0.295 |
| 1999 | -1.886 | -1.808 | -1.186 | -2.049 | -1.797 | -1.730 |
| 2000 | -0.883 | -1.037 | -1.242 | -2.246 | -1.196 | -0.954 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Output | | | | | |
| | 204 | 300 | 301 | 302 | 303 | 304 |
| 1964 | -0.247 | 0.108 | -0.197 | -0.245 | -0.302 | -0.215 |
| 1965 | 1.073 | 1.405 | 1.218 | 1.160 | 1.145 | 1.070 |
| 1966 | -2.065 | -2.257 | -2.471 | -2.526 | -2.381 | -2.164 |
| 1967 | -0.482 | 0.110 | -0.950 | -0.374 | -0.513 | -0.479 |
| 1968 | -1.614 | -0.476 | -0.848 | -1.227 | -1.344 | -1.330 |
| 1969 | -0.071 | 0.146 | -0.423 | -0.039 | -0.236 | 0.416 |
| 1970 | -2.852 | -2.990 | -2.410 | -3.548 | -3.427 | -3.154 |
| 1971 | 7.000 | 6.660 | 5.050 | 8.100 | 7.631 | 7.181 |
| 1972 | -2.544 | 1.190 | 0.783 | -2.537 | -2.734 | -2.353 |
| 1973 | -1.682 | -4.730 | -5.476 | -3.142 | -2.866 | -1.591 |
| 1974 | 0.433 | 3.992 | 0.213 | 1.573 | 1.025 | 0.676 |
| 1975 | -6.458 | -1.858 | -4.564 | -6.073 | -6.887 | -5.394 |
| 1976 | -8.263 | -9.415 | -9.968 | -9.660 | -9.296 | -7.755 |
| 1977 | 1.008 | 1.822 | -0.268 | 1.955 | 1.255 | 1.302 |
| 1978 | 1.602 | 5.042 | 4.402 | 2.757 | 2.222 | 2.012 |
| 1979 | 4.445 | 1.190 | 2.024 | 3.804 | 3.977 | 4.750 |
| 1980 | 0.889 | 0.716 | 0.011 | -0.205 | 0.171 | 0.081 |
| 1981 | -2.654 | -3.474 | -3.990 | -3.464 | -3.015 | -3.937 |
| 1982 | -2.782 | -1.482 | -2.870 | -2.388 | -2.198 | -2.972 |
| 1983 | -1.832 | -0.702 | -1.038 | -0.947 | -0.868 | -0.807 |
| 1984 | 1.574 | 1.663 | 1.486 | 1.970 | 1.989 | 2.565 |
| 1985 | 1.866 | 1.371 | 1.888 | 1.593 | 1.784 | 1.526 |
| 1986 | 2.448 | 1.046 | 1.292 | 1.853 | 2.083 | 1.398 |
| 1987 | 0.690 | 1.789 | 0.879 | 0.592 | 0.559 | 0.149 |
| 1988 | 2.410 | 4.423 | 1.422 | 3.189 | 2.612 | 3.335 |
| 1989 | -7.411 | -0.164 | -4.062 | -7.490 | -8.646 | -6.117 |
| 1990 | -6.552 | -5.876 | -8.356 | -7.291 | -7.831 | -6.002 |
| 1991 | -7.504 | -5.054 | -5.836 | -7.260 | -8.031 | -7.497 |
| 1992 | -0.434 | -1.694 | -0.383 | 0.060 | -0.400 | 0.050 |
| 1993 | 4.165 | 2.068 | 5.587 | 4.667 | 4.419 | 4.610 |
| 1994 | 8.481 | 3.785 | 7.817 | 8.117 | 8.363 | 7.937 |
| 1995 | 6.326 | 1.862 | 5.708 | 5.395 | 6.273 | 4.433 |
| 1996 | 1.870 | -1.805 | 1.088 | 0.714 | 1.797 | -0.165 |
| 1997 | 2.937 | 1.430 | 1.877 | 3.433 | 4.181 | 2.339 |
| 1998 | -0.966 | 1.772 | 1.117 | 0.091 | 0.075 | 0.045 |
| 1999 | -2.274 | -1.174 | -2.029 | -2.253 | -2.268 | -1.181 |
| 2000 | -1.611 | -1.278 | -2.018 | -1.640 | -1.855 | -1.454 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------------|
| | Construction | | | | | Construction |
| | Output | 400 | 401 | 402 | 403 | Starts |
| | | 400 | 401 | 402 | 403 | 100 |
| 1964 | -0.002 | -0.001 | -0.320 | -0.299 | -0.261 | -0.152 |
| 1965 | 1.289 | 1.292 | 1.084 | 1.099 | 0.970 | 1.386 |
| 1966 | -2.174 | -2.175 | -2.147 | -2.198 | -2.224 | 0.126 |
| 1967 | 0.065 | 0.065 | -0.332 | -0.312 | -0.209 | -0.956 |
| 1968 | -2.105 | -2.107 | -1.797 | -1.939 | -1.879 | -0.49 |
| 1969 | 0.521 | 0.556 | -0.211 | -0.044 | 0.433 | -0.246 |
| 1970 | -2.696 | -2.737 | -3.509 | -3.554 | -3.203 | -1.921 |
| 1971 | 8.026 | 8.085 | 8.049 | 8.024 | 8.270 | 2.954 |
| 1972 | -1.756 | -1.781 | -3.784 | -3.466 | -4.384 | 3.113 |
| 1973 | -1.702 | -1.661 | -1.715 | -2.097 | -0.246 | -1.511 |
| 1974 | 3.715 | 3.720 | 1.647 | 2.014 | 1.363 | 3.373 |
| 1975 | -7.938 | -7.950 | -8.986 | -9.626 | -8.331 | 0.559 |
| 1976 | -6.497 | -6.444 | -7.351 | -6.796 | -7.302 | -6.15 |
| 1977 | 2.420 | 2.384 | 0.471 | 0.120 | 2.519 | -2.701 |
| 1978 | 1.175 | 1.169 | 1.238 | 1.097 | 0.381 | 1.046 |
| 1979 | 5.460 | 5.542 | 4.244 | 4.548 | 5.204 | 1.757 |
| 1980 | 3.896 | 3.841 | 1.360 | 1.215 | 1.726 | 2.251 |
| 1981 | -4.632 | -4.711 | -3.130 | -3.725 | -4.674 | -0.504 |
| 1982 | -2.217 | -2.199 | -1.453 | -1.465 | -4.336 | -1.747 |
| 1983 | -2.746 | -2.750 | -1.647 | -1.982 | -0.649 | -1.901 |
| 1984 | 1.982 | 2.024 | 2.206 | 2.157 | 4.408 | -0.249 |
| 1985 | 2.377 | 2.369 | 1.651 | 1.738 | 0.832 | 0.736 |
| 1986 | 2.412 | 2.399 | 2.373 | 2.086 | 0.243 | 1.077 |
| 1987 | 1.678 | 1.664 | 0.641 | 0.871 | 0.582 | 1.558 |
| 1988 | 3.443 | 3.484 | 2.224 | 1.988 | 5.384 | 3.488 |
| 1989 | -3.336 | -3.332 | -8.977 | -8.097 | -7.945 | 1.413 |
| 1990 | -5.604 | -5.600 | -7.712 | -7.864 | -7.394 | -3.026 |
| 1991 | -6.048 | -6.092 | -7.868 | -7.402 | -9.035 | -5.019 |
| 1992 | -2.958 | -2.964 | -1.746 | -2.161 | 1.103 | -4.644 |
| 1993 | 5.262 | 5.287 | 4.952 | 5.662 | 5.033 | -1.109 |
| 1994 | 7.489 | 7.450 | 7.178 | 7.030 | 7.835 | 1.775 |
| 1995 | 5.540 | 5.495 | 7.809 | 7.913 | 4.350 | 2.628 |
| 1996 | -0.937 | -1.006 | 1.689 | 1.471 | 0.981 | 0.754 |
| 1997 | 0.698 | 0.708 | 5.342 | 4.797 | 3.325 | 1.305 |
| 1998 | -2.216 | -2.191 | -1.013 | -0.837 | -1.200 | 1.773 |
| 1999 | -2.562 | -2.502 | -1.931 | -2.145 | -1.443 | -0.02 |
| 2000 | -0.958 | -0.940 | -1.850 | -1.436 | -0.981 | -0.666 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Starts | | | | | |
| | 101 | 102 | 103 | 104 | 200 | 201 |
| 1964 | -0.064 | -0.366 | -0.35 | -0.373 | -0.273 | -0.391 |
| 1965 | 1.576 | 0.792 | 0.866 | 1.021 | 1.422 | 1.173 |
| 1966 | -1.242 | -1.649 | -1.954 | -1.876 | -1.313 | -1.658 |
| 1967 | 0.133 | -0.269 | -0.184 | -0.489 | -1.116 | -1.795 |
| 1968 | -0.88 | -1.086 | -1.15 | -1.052 | 0.145 | -0.903 |
| 1969 | 0.199 | -0.054 | -0.024 | -0.113 | -0.162 | -0.56 |
| 1970 | -4.171 | -2.926 | -3.339 | -3.327 | -2.701 | -1.818 |
| 1971 | 9.564 | 7.694 | 8.752 | 8.306 | 6.5 | 3.725 |
| 1972 | -2.064 | -3.931 | -4.591 | -3.449 | 1.597 | 1.027 |
| 1973 | -0.601 | -2.151 | -2.214 | -2.751 | -5.54 | -5.075 |
| 1974 | 6.252 | 2.956 | 3.209 | 3.365 | 6.128 | -0.556 |
| 1975 | -4.1 | -6.342 | -7.154 | -6.435 | -2.373 | -4.719 |
| 1976 | -8.307 | -7.184 | -7.873 | -8.453 | -9.399 | -9.226 |
| 1977 | 1.751 | 2.755 | 3.263 | 2.609 | 2.227 | -1.329 |
| 1978 | 0.944 | 1.336 | 1.474 | 1.906 | 4.302 | 3.463 |
| 1979 | 3.233 | 2.136 | 2.497 | 2.44 | 1.292 | 2.326 |
| 1980 | 1.242 | -0.441 | -0.57 | -0.267 | 1.057 | 0.39 |
| 1981 | -2.61 | -3.309 | -3.722 | -3.646 | -3.137 | -3.237 |
| 1982 | -1.197 | -1.096 | -1.195 | -1.478 | -1.732 | -3.029 |
| 1983 | -2.476 | -1.503 | -1.619 | -1.645 | -0.676 | -1.231 |
| 1984 | 1.689 | 2.306 | 2.571 | 2.38 | 1.613 | 1.368 |
| 1985 | -0.147 | 0.313 | 0.292 | 0.496 | 1.374 | 2.107 |
| 1986 | 2.398 | 2.12 | 2.314 | 2.225 | 0.952 | 1.57 |
| 1987 | 0.978 | 0.145 | 0.091 | 0.324 | 1.34 | 0.812 |
| 1988 | 7.255 | 3.598 | 4.105 | 4.075 | 3.666 | 0.299 |
| 1989 | -3.897 | -6.661 | -7.533 | -6.699 | -1.785 | -4.687 |
| 1990 | -3.023 | -4.251 | -4.603 | -5.111 | -6.128 | -8.46 |
| 1991 | -7.895 | -5.946 | -6.614 | -6.668 | -4.163 | -6.199 |
| 1992 | -2.351 | 1.059 | 1.29 | 0.637 | -1.478 | -0.857 |
| 1993 | -0.444 | 3.278 | 3.529 | 3.502 | 3.274 | 5.609 |
| 1994 | 4.323 | 6.427 | 7.09 | 6.947 | 3.974 | 8.214 |
| 1995 | 1.994 | 2.835 | 3.043 | 3.34 | 2.184 | 6.614 |
| 1996 | -0.573 | 0.397 | 0.335 | 0.379 | -1.732 | 2.577 |
| 1997 | 3.317 | 3.037 | 3.361 | 3.188 | 1.175 | 2.104 |
| 1998 | 0.894 | 0.052 | -0.037 | 0.323 | 1.38 | 1.002 |
| 1999 | -1.012 | -1.543 | -1.762 | -1.723 | -1.866 | -1.842 |
| 2000 | -0.377 | -0.657 | -0.731 | -0.839 | -0.892 | -2.101 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|--------|
| | Construction Starts | | | | | |
| | 202 | 203 | 204 | 300 | 301 | 302 |
| 1964 | -0.507 | -0.331 | -0.387 | -0.279 | -0.425 | -0.417 |
| 1965 | 1.07 | 0.779 | 1.136 | 1.421 | 1.257 | 1.225 |
| 1966 | -1.941 | -1.764 | -1.734 | -1.303 | -1.941 | -2.038 |
| 1967 | -0.854 | -0.14 | -1.007 | -1.185 | -1.727 | -1.034 |
| 1968 | -0.946 | -1.133 | -1.737 | 0.15 | -0.677 | -1.195 |
| 1969 | -0.413 | 0.027 | -0.231 | -0.138 | -0.525 | -0.236 |
| 1970 | -3.368 | -3.043 | -2.605 | -2.66 | -2.268 | -3.268 |
| 1971 | 9.175 | 7.909 | 6.9 | 6.41 | 4.981 | 7.793 |
| 1972 | -4.165 | -4.186 | -2.805 | 1.68 | 0.878 | -2.566 |
| 1973 | -3.751 | -1.928 | -2.229 | -5.571 | -6.019 | -3.611 |
| 1974 | 4.563 | 2.725 | 0.794 | 5.966 | 1.271 | 2.299 |
| 1975 | -8.711 | -6.337 | -7.151 | -2.297 | -4.821 | -6.748 |
| 1976 | -8.518 | -7.296 | -8.572 | -9.409 | -10.16 | -9.69 |
| 1977 | 2.877 | 2.946 | 0.696 | 2.145 | 0.087 | 1.571 |
| 1978 | 2.236 | 1.293 | 1.363 | 4.428 | 4.217 | 2.42 |
| 1979 | 1.977 | 2.344 | 3.651 | 1.371 | 2.025 | 2.876 |
| 1980 | 0.038 | -0.584 | 0.79 | 1.026 | 0.278 | -0.066 |
| 1981 | -4.682 | -3.295 | -3.144 | -3.156 | -3.797 | -3.902 |
| 1982 | -1.148 | -1.16 | -2.752 | -1.799 | -2.929 | -2.254 |
| 1983 | -2.107 | -1.444 | -2.611 | -0.66 | -1.04 | -1.773 |
| 1984 | 2.968 | 2.313 | 1.807 | 1.662 | 1.682 | 2.292 |
| 1985 | 0.453 | 0.309 | 1.472 | 1.429 | 2.084 | 1.095 |
| 1986 | 2.451 | 2.127 | 2.897 | 0.963 | 1.444 | 2.312 |
| 1987 | 0.382 | 0.096 | 0.666 | 1.32 | 0.907 | 0.558 |
| 1988 | 3.585 | 3.757 | 2.511 | 3.591 | 1.081 | 3.368 |
| 1989 | -7.302 | -6.917 | -7.02 | -1.78 | -4.704 | -6.824 |
| 1990 | -6.421 | -4.163 | -6.217 | -6.181 | -8.694 | -6.751 |
| 1991 | -6.201 | -6.152 | -7.76 | -4.208 | -5.833 | -7.471 |
| 1992 | 0.193 | 1.251 | -0.377 | -1.396 | -0.55 | 0.089 |
| 1993 | 5.353 | 3.167 | 4.241 | 3.393 | 5.952 | 4.511 |
| 1994 | 6.857 | 6.619 | 8.872 | 4.092 | 7.937 | 8.213 |
| 1995 | 4.625 | 2.757 | 6.023 | 2.217 | 5.853 | 4.913 |
| 1996 | -0.19 | 0.399 | 2.313 | -1.734 | 1.397 | 1.269 |
| 1997 | 4.131 | 3.047 | 2.818 | 1.071 | 2.021 | 3.294 |
| 1998 | -0.303 | -0.008 | -0.617 | 1.348 | 1.117 | 0.537 |
| 1999 | -1.573 | -1.6 | -2.05 | -1.865 | -2.131 | -1.909 |
| 2000 | -0.377 | -0.657 | -0.731 | -0.949 | -1.869 | -1.368 |

| Year | ARIMAX Order | | | | | |
|------|---------------------|--------|--------|--------|--------|---------|
| | Construction Starts | | | | | |
| | 303 | 304 | 400 | 401 | 402 | 403 |
| 1964 | -0.424 | -0.634 | -0.401 | -0.525 | -0.506 | -0.585 |
| 1965 | 1.205 | 1.114 | 1.32 | 1.402 | 1.181 | 1.209 |
| 1966 | -2.003 | -1.034 | -1.227 | -0.861 | -1.693 | -1.483 |
| 1967 | -1.034 | -1.939 | -1.288 | -1.863 | -1.071 | -1.414 |
| 1968 | -1.394 | -1.245 | -1.653 | -1.459 | -1.792 | -1.816 |
| 1969 | -0.282 | 0.25 | -0.242 | 0.028 | -0.404 | -0.388 |
| 1970 | -3.202 | -2.418 | -1.663 | -1.923 | -3.253 | -3.045 |
| 1971 | 7.629 | 5.709 | 7.453 | 8.122 | 8.236 | 7.993 |
| 1972 | -3.025 | -1.976 | -1.681 | -2.124 | -4.351 | -3.795 |
| 1973 | -3.322 | -1.977 | -2.659 | -2.278 | -2.358 | -3.066 |
| 1974 | 1.592 | 2.105 | 5.465 | 6.138 | 2.172 | 3.29 |
| 1975 | -7.403 | -6.716 | -8.835 | -9.359 | -9.486 | -10.762 |
| 1976 | -9.621 | -6.594 | -6.003 | -4.954 | -8.291 | -6.868 |
| 1977 | 1.208 | -0.046 | 2.02 | 0.565 | 0.366 | -0.666 |
| 1978 | 1.904 | 1.633 | 0.856 | 1.607 | 0.892 | 1.006 |
| 1979 | 2.914 | 3.839 | 5.668 | 6.487 | 2.873 | 3.518 |
| 1980 | -0.122 | 0.836 | 3.898 | 2.293 | 0.507 | 0.197 |
| 1981 | -3.815 | -5.582 | -4.295 | -4.931 | -4.172 | -4.341 |
| 1982 | -2.276 | -2.685 | -2.367 | -1.798 | -1.689 | -1.696 |
| 1983 | -1.928 | -0.763 | -3.103 | -3.469 | -3.03 | -3.318 |
| 1984 | 2.243 | 4.022 | 2.166 | 3.312 | 2.482 | 2.506 |
| 1985 | 1.078 | -0.494 | 2.719 | 2.31 | 0.605 | 1.065 |
| 1986 | 2.471 | 1.2 | 2.704 | 2.712 | 2.901 | 2.381 |
| 1987 | 0.521 | 0.975 | 1.545 | 1.328 | 0.519 | 1.152 |
| 1988 | 3.04 | 4.669 | 2.535 | 3.207 | 2.857 | 1.93 |
| 1989 | -7.401 | -5.641 | -4.055 | -3.849 | -7.642 | -6.548 |
| 1990 | -6.903 | -6.551 | -5.806 | -5.75 | -6.816 | -7.624 |
| 1991 | -7.884 | -8.098 | -5.779 | -6.498 | -7.856 | -7.028 |
| 1992 | 0.051 | 0.899 | -2.937 | -2.874 | -1.213 | -2.219 |
| 1993 | 4.563 | 5.159 | 5.906 | 6.386 | 5.025 | 6.247 |
| 1994 | 8.692 | 6.635 | 7.52 | 6.664 | 7.857 | 7.167 |
| 1995 | 5.496 | 2.525 | 5.948 | 5.242 | 6.783 | 7.237 |
| 1996 | 2.07 | 1.104 | -0.413 | -1.451 | 1.935 | 1.548 |
| 1997 | 3.76 | 3.086 | 0.805 | 1.291 | 5.05 | 4.66 |
| 1998 | 0.55 | 0.471 | -2.334 | -1.882 | -0.442 | -0.281 |
| 1999 | -1.813 | -1.242 | -2.895 | -1.866 | -1.101 | -1.419 |
| 2000 | -1.446 | -1.377 | -0.979 | -0.957 | -1.752 | -1.180 |

| Year | ARIMAX Order | | | | | |
|------|--------------|------------|--------|--------|--------|--------|
| | Construction | Employment | | | | |
| | Starts | | | | | |
| | 404 | 100 | 101 | 102 | 103 | 104 |
| 1964 | -0.646 | -0.134 | 0.197 | -0.207 | -0.233 | -0.209 |
| 1965 | 1.181 | 2.412 | 1.465 | 0.862 | 1.298 | 1.135 |
| 1966 | -1.251 | -0.577 | -1.599 | -2.165 | -2.546 | -2.386 |
| 1967 | -1.721 | -0.331 | 0.694 | 0.375 | 0.543 | 0.186 |
| 1968 | -1.877 | -1.28 | -0.861 | -1.376 | -1.625 | -1.373 |
| 1969 | -0.323 | -0.384 | 0.45 | 0.322 | 0.265 | 0.257 |
| 1970 | -2.318 | -2.248 | -4.534 | -3.367 | -3.657 | -3.702 |
| 1971 | 7.273 | 2.365 | 10.037 | 7.818 | 8.139 | 8.234 |
| 1972 | -3.573 | 3.405 | -2.188 | -4.22 | -3.424 | -3.469 |
| 1973 | -2.405 | 0.164 | -0.148 | -1.431 | -3.129 | -2.114 |
| 1974 | 3.009 | 4.198 | 5.274 | 1.934 | 3.955 | 2.233 |
| 1975 | -10.374 | 0.104 | -3.244 | -5.636 | -7.115 | -5.466 |
| 1976 | -6.684 | -4.745 | -9.032 | -7.312 | -6.932 | -8.501 |
| 1977 | 0.17 | -2.829 | 2.32 | 3.211 | 3.038 | 2.871 |
| 1978 | 0.318 | 0.427 | 0.797 | 1.316 | 2.749 | 2.095 |
| 1979 | 4.17 | 2.913 | 3.855 | 2.874 | 2.435 | 3.202 |
| 1980 | 1.628 | 1.364 | 0.841 | -0.928 | 0.018 | -0.754 |
| 1981 | -5.85 | -3.315 | -2.122 | -3.226 | -4.597 | -3.526 |
| 1982 | -2.396 | -2.469 | -1.627 | -1.558 | -1.109 | -1.902 |
| 1983 | -2.405 | -2.281 | -1.791 | -1.169 | -1.779 | -1.286 |
| 1984 | 2.885 | 1.726 | 0.875 | 2.035 | 2.767 | 2.156 |
| 1985 | 0.994 | 0.158 | 0.555 | 0.389 | 0.268 | 0.558 |
| 1986 | 2.632 | 0.396 | 1.739 | 1.669 | 1.641 | 1.809 |
| 1987 | 0.737 | 2.47 | 1.445 | 0.169 | 0.624 | 0.389 |
| 1988 | 2.161 | 5.755 | 6.985 | 3.665 | 3.448 | 4.151 |
| 1989 | -6.343 | 2.076 | -3.52 | -6.64 | -5.832 | -6.533 |
| 1990 | -6.869 | -3.242 | -3.524 | -4.276 | -5.827 | -5.145 |
| 1991 | -7.582 | -8.221 | -7.177 | -6.128 | -5.247 | -6.838 |
| 1992 | -1.945 | -5.315 | -2.864 | 1.195 | 0.17 | 0.86 |
| 1993 | 6.549 | -2.607 | 0.135 | 2.783 | 4.224 | 2.961 |
| 1994 | 8.131 | 2.115 | 3.801 | 6.524 | 5.999 | 7.142 |
| 1995 | 6.239 | 3.452 | 2.767 | 2.601 | 3.932 | 3.097 |
| 1996 | 0.996 | 0.216 | -1.277 | 0.204 | -0.801 | 0.252 |
| 1997 | 3.94 | 2.234 | 3.864 | 2.79 | 3.601 | 2.841 |
| 1998 | -0.54 | 0.753 | 0.611 | -0.231 | -0.818 | 0.142 |
| 1999 | -0.941 | 1.454 | -0.875 | -1.685 | -1.334 | -1.829 |
| 2000 | -1.330 | -0.071 | -0.624 | -0.833 | -1.142 | -1.001 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | Employment | | | | | |
| | 200 | 201 | 202 | 203 | 204 | 300 |
| 1964 | -0.096 | -0.384 | -0.247 | -0.345 | -0.253 | -0.106 |
| 1965 | 2.365 | 2.457 | 1.464 | 1.492 | 1.269 | 2.406 |
| 1966 | -2.407 | -2.48 | -2.792 | -2.66 | -2.05 | -2.415 |
| 1967 | 0.343 | -1.053 | 0.325 | 0.06 | -0.298 | 0.18 |
| 1968 | -0.817 | -1.665 | -1.64 | -2.048 | -2.1 | -0.779 |
| 1969 | 0.104 | -0.383 | 0.2 | -0.047 | -0.024 | 0.133 |
| 1970 | -3.262 | -2.074 | -3.776 | -4.111 | -2.735 | -3.126 |
| 1971 | 6.043 | 3.053 | 8.324 | 7.7 | 6.533 | 5.716 |
| 1972 | 1.966 | 1.117 | -3.021 | -3.73 | -3.016 | 2.223 |
| 1973 | -4.078 | -3.876 | -3.791 | -3.128 | -1.182 | -4.059 |
| 1974 | 6.111 | 0.519 | 3.603 | 1.335 | -0.07 | 5.626 |
| 1975 | -2.073 | -4.857 | -7.248 | -8.187 | -6.794 | -1.846 |
| 1976 | -7.527 | -6.936 | -8.04 | -9.072 | -7.923 | -7.391 |
| 1977 | 1.721 | -0.165 | 2.872 | 0.983 | 0.995 | 1.491 |
| 1978 | 4.599 | 4.493 | 3.427 | 1.527 | 1.203 | 4.904 |
| 1979 | 2.923 | 5.395 | 2.833 | 2.138 | 4.375 | 3.286 |
| 1980 | -0.148 | 1.245 | 0.091 | -0.869 | 0.981 | -0.22 |
| 1981 | -5.302 | -4.615 | -4.841 | -4.928 | -2.619 | -5.48 |
| 1982 | -2.103 | -2.873 | -1.46 | -2.173 | -2.839 | -2.307 |
| 1983 | -1.791 | -2.005 | -1.786 | -2.246 | -2.723 | -1.786 |
| 1984 | 2.758 | 2.778 | 2.891 | 2.423 | 1.474 | 2.834 |
| 1985 | 0.122 | 0.631 | 0.474 | 0.199 | 1.137 | 0.188 |
| 1986 | 0.898 | 0.49 | 1.776 | 1.795 | 2.807 | 0.845 |
| 1987 | 2.266 | 1.533 | 0.697 | 0.049 | 0.827 | 2.303 |
| 1988 | 5.678 | 2.412 | 3.475 | 1.884 | 2.715 | 5.585 |
| 1989 | -1.381 | -3.667 | -6.24 | -8.484 | -7.013 | -1.311 |
| 1990 | -5.72 | -7.487 | -6.78 | -8.372 | -5.82 | -5.84 |
| 1991 | -6.528 | -8.204 | -5.941 | -8.406 | -8.077 | -6.707 |
| 1992 | -1.372 | -0.356 | 0.279 | -0.729 | -0.043 | -1.165 |
| 1993 | 0.975 | 4.21 | 4.767 | 3.907 | 3.329 | 1.233 |
| 1994 | 4.049 | 8.03 | 7.004 | 7.745 | 9.216 | 4.256 |
| 1995 | 2.361 | 6.204 | 4.579 | 5.667 | 5.856 | 2.45 |
| 1996 | -2.708 | 0.698 | -0.545 | 2.18 | 2.835 | -2.797 |
| 1997 | 2.317 | 2.017 | 3.609 | 5.208 | 2.29 | 2.019 |
| 1998 | 0.283 | -1.276 | -0.669 | 0.652 | -1.293 | 0.194 |
| 1999 | -0.163 | -1.092 | -1.577 | -0.349 | -2.534 | -0.11 |
| 2000 | -0.806 | -2.316 | -1.497 | -1.051 | -1.492 | -0.893 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | Employment | | | | | |
| | 301 | 302 | 303 | 304 | 400 | 401 |
| 1964 | -0.358 | -0.323 | 0.204 | -0.185 | -0.069 | -0.073 |
| 1965 | 2.337 | 1.941 | 1.731 | 1.025 | 1.499 | 1.511 |
| 1966 | -2.634 | -2.703 | -2.067 | -2.173 | -2.161 | -2.165 |
| 1967 | -0.824 | -0.349 | -0.164 | -0.262 | 0.056 | 0.059 |
| 1968 | -1.496 | -1.884 | -1.26 | -1.332 | -2.095 | -2.105 |
| 1969 | -0.322 | 0.154 | 0.836 | 0.652 | 0.493 | 0.438 |
| 1970 | -2.325 | -3.323 | -3.17 | -3.463 | -2.673 | -2.608 |
| 1971 | 3.773 | 6.234 | 9.374 | 7.172 | 7.807 | 7.702 |
| 1972 | 1.017 | -1.743 | -0.595 | -2.764 | -1.387 | -1.346 |
| 1973 | -4.387 | -3.024 | -0.646 | -0.886 | -1.692 | -1.757 |
| 1974 | 1.221 | 0.829 | 2.797 | 0.685 | 4.452 | 4.46 |
| 1975 | -4.759 | -5.68 | -4.087 | -5.34 | -7.891 | -7.864 |
| 1976 | -7.376 | -8.355 | -7.984 | -7.248 | -5.862 | -5.936 |
| 1977 | 0.401 | 1.357 | 2.1 | 1.694 | 2.338 | 2.409 |
| 1978 | 4.818 | 3.52 | 3.138 | 1.246 | 1.461 | 1.494 |
| 1979 | 4.882 | 4.675 | 5.84 | 4.55 | 5.974 | 5.861 |
| 1980 | 0.817 | 0.024 | 1.951 | 0.051 | 3.812 | 3.897 |
| 1981 | -4.823 | -4.292 | -2.966 | -4.374 | -4.729 | -4.603 |
| 1982 | -2.758 | -2.667 | -3.818 | -3.016 | -2.644 | -2.678 |
| 1983 | -1.874 | -1.899 | -3.892 | -0.171 | -2.893 | -2.915 |
| 1984 | 2.799 | 2.82 | 0.622 | 3.066 | 2.142 | 2.093 |
| 1985 | 0.675 | 0.37 | 1.65 | 0.375 | 1.914 | 1.898 |
| 1986 | 0.685 | 1.799 | 4.16 | 0.48 | 2.172 | 2.186 |
| 1987 | 1.555 | 0.597 | 2.973 | 0.855 | 1.402 | 1.425 |
| 1988 | 2.622 | 3.629 | 6.084 | 4.931 | 3.755 | 3.706 |
| 1989 | -3.822 | -6.228 | -4.538 | -5.506 | -3.972 | -3.969 |
| 1990 | -7.56 | -6.552 | -5.162 | -6.489 | -5.648 | -5.659 |
| 1991 | -7.67 | -8.685 | -8.164 | -7.648 | -6.377 | -6.335 |
| 1992 | -0.046 | 1.02 | -1.457 | 1.125 | -2.676 | -2.653 |
| 1993 | 4.312 | 3.239 | 2.131 | 4.671 | 4.987 | 4.926 |
| 1994 | 7.824 | 9.295 | 7.085 | 6.297 | 7.421 | 7.496 |
| 1995 | 5.741 | 4.291 | 3.885 | 2.535 | 5.711 | 5.776 |
| 1996 | 0.217 | 1.573 | -0.93 | 0.359 | -1.061 | -0.949 |
| 1997 | 2.126 | 1.979 | -0.226 | 3.491 | 0.963 | 0.962 |
| 1998 | -0.955 | -0.091 | -2.701 | 0.184 | -2.652 | -2.712 |
| 1999 | -1.127 | -2.01 | -2.709 | -1.75 | -2.449 | -2.532 |
| 2000 | -2.149 | -1.669 | 0.220 | -1.508 | -0.931 | -0.972 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | Employment | | | GDP | | |
| | 402 | 403 | 404 | 100 | 101 | 102 |
| 1964 | -0.277 | -0.299 | -0.272 | 4.022 | 2.964 | 3.589 |
| 1965 | 1.336 | 1.545 | 1.36 | -0.701 | -0.155 | -0.466 |
| 1966 | -2.367 | -2.422 | -2.397 | -1.092 | -1.124 | -0.850 |
| 1967 | -0.062 | -0.053 | -0.109 | -0.164 | 0.174 | 0.200 |
| 1968 | -2.291 | -2.528 | -2.446 | 2.067 | 1.037 | 1.839 |
| 1969 | -0.017 | 0.068 | 0.36 | -1.511 | -1.439 | -1.029 |
| 1970 | -3.577 | -3.314 | -2.98 | -1.791 | -2.827 | -0.595 |
| 1971 | 7.564 | 6.859 | 7.131 | 1.465 | 7.061 | 5.881 |
| 1972 | -3.638 | -2.691 | -2.891 | 3.903 | 0.429 | -0.639 |
| 1973 | -2.334 | -2.907 | -1.818 | 5.244 | 2.601 | 2.338 |
| 1974 | 1.545 | 2.451 | 2.169 | -5.428 | -0.779 | -3.135 |
| 1975 | -9.203 | -9.833 | -9.5 | -2.417 | -1.753 | -4.095 |
| 1976 | -7.709 | -6.788 | -6.593 | -2.599 | -9.241 | -8.121 |
| 1977 | 0.585 | 0.765 | 1.766 | -2.285 | 3.165 | 4.302 |
| 1978 | 1.023 | 0.786 | 0.358 | 1.866 | 0.117 | 1.680 |
| 1979 | 3.381 | 4.452 | 4.667 | 1.339 | 4.111 | 3.009 |
| 1980 | 1.059 | 1.472 | 3.114 | -5.051 | -4.630 | -6.303 |
| 1981 | -4.028 | -4.631 | -6.067 | -4.028 | -1.686 | -4.680 |
| 1982 | -1.626 | -1.642 | -3.701 | -0.322 | -2.860 | -3.947 |
| 1983 | -2.458 | -2.596 | -0.959 | 0.523 | 0.643 | -0.482 |
| 1984 | 2.197 | 2.288 | 3.504 | -0.527 | -0.918 | -0.732 |
| 1985 | 0.876 | 1.05 | 0.266 | 1.802 | 3.126 | 2.123 |
| 1986 | 2.123 | 1.725 | 1.338 | 2.223 | 0.485 | 0.443 |
| 1987 | 0.8 | 1.056 | 1.511 | 3.141 | 4.497 | 2.884 |
| 1988 | 2.251 | 2.16 | 2.868 | 5.278 | 5.947 | 3.395 |
| 1989 | -6.939 | -6.243 | -6.34 | -0.351 | -2.676 | -5.626 |
| 1990 | -7.36 | -7.479 | -7.176 | -4.548 | -5.264 | -5.729 |
| 1991 | -7.319 | -7.333 | -7.256 | -8.237 | -8.756 | -7.336 |
| 1992 | -1.632 | -1.912 | -1.897 | -4.986 | -3.458 | -0.118 |
| 1993 | 4.898 | 5.089 | 5.717 | -0.493 | -0.011 | 3.055 |
| 1994 | 7.805 | 7.986 | 8.516 | 3.641 | 4.952 | 7.004 |
| 1995 | 7.12 | 6.892 | 5.872 | 1.957 | 1.579 | 2.116 |
| 1996 | 2.105 | 1.886 | 0.194 | 0.619 | 0.006 | 0.885 |
| 1997 | 4.645 | 4.000 | 3.283 | 1.688 | 3.111 | 2.616 |
| 1998 | -0.715 | -1.074 | -0.815 | 2.412 | 1.804 | 1.206 |
| 1999 | -1.592 | -1.635 | -1.363 | 0.749 | -0.855 | -1.129 |
| 2000 | -1.804 | -1.659 | -1.521 | 1.045 | 1.103 | 1.709 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | GDP | | | | | |
| | 103 | 104 | 200 | 201 | 202 | 203 |
| 1964 | 4.527 | 3.236 | 4.028 | 3.670 | 4.197 | 4.569 |
| 1965 | -0.687 | -0.381 | -0.647 | -0.527 | -0.683 | -0.790 |
| 1966 | -0.591 | -1.070 | -0.797 | -0.915 | -0.652 | -0.530 |
| 1967 | 0.016 | 0.326 | 0.185 | 0.129 | 0.236 | 0.216 |
| 1968 | 2.518 | 1.292 | 2.050 | 1.544 | 2.288 | 2.609 |
| 1969 | -1.368 | -1.242 | -1.527 | -1.781 | -1.331 | -1.373 |
| 1970 | -0.347 | -1.192 | -1.119 | -1.925 | -0.259 | 0.004 |
| 1971 | 4.121 | 8.990 | 4.487 | 6.972 | 6.438 | 5.792 |
| 1972 | 0.040 | -2.106 | 1.859 | -0.549 | -0.039 | 0.434 |
| 1973 | 4.388 | -0.649 | 1.140 | 2.062 | 2.255 | 3.032 |
| 1974 | -4.169 | 1.444 | -3.601 | -0.694 | -3.680 | -4.392 |
| 1975 | -3.459 | -8.174 | -1.372 | -2.615 | -3.821 | -3.753 |
| 1976 | -6.934 | -9.571 | -6.712 | -9.491 | -9.073 | -8.470 |
| 1977 | 4.393 | 5.902 | 0.900 | 4.830 | 4.360 | 4.029 |
| 1978 | 0.834 | 2.102 | 5.352 | 1.593 | 2.637 | 2.599 |
| 1979 | 2.732 | 2.166 | 0.519 | 1.548 | 2.725 | 2.608 |
| 1980 | -8.087 | -3.300 | -6.086 | -4.808 | -6.580 | -7.135 |
| 1981 | -4.463 | -8.188 | -5.347 | -4.246 | -5.673 | -5.939 |
| 1982 | -3.733 | -1.248 | -1.956 | -1.713 | -4.260 | -4.365 |
| 1983 | 1.151 | -4.636 | -0.151 | -0.171 | -1.429 | -1.376 |
| 1984 | -0.820 | 1.891 | 0.756 | 0.865 | -0.858 | -1.152 |
| 1985 | 3.223 | 0.634 | 3.028 | 2.378 | 1.874 | 1.823 |
| 1986 | 0.553 | -0.233 | 1.850 | 1.364 | 0.554 | 0.526 |
| 1987 | 4.390 | 3.859 | 3.004 | 3.637 | 2.783 | 2.893 |
| 1988 | 4.144 | 1.955 | 5.562 | 6.499 | 3.907 | 3.878 |
| 1989 | -3.577 | -7.253 | -3.059 | -4.477 | -6.370 | -6.028 |
| 1990 | -4.728 | -8.712 | -5.482 | -4.341 | -6.248 | -6.134 |
| 1991 | -7.426 | -7.388 | -6.275 | -7.957 | -8.057 | -8.217 |
| 1992 | -1.522 | -1.162 | -1.519 | -2.106 | -0.004 | -0.307 |
| 1993 | 1.077 | 5.397 | 2.019 | 0.585 | 3.474 | 3.136 |
| 1994 | 5.350 | 6.947 | 4.279 | 4.590 | 7.632 | 7.452 |
| 1995 | 0.485 | 3.902 | 0.697 | 0.807 | 2.325 | 2.104 |
| 1996 | 0.381 | -0.112 | -1.176 | -0.631 | 0.906 | 0.985 |
| 1997 | 1.908 | 4.938 | 1.761 | 3.134 | 2.833 | 2.624 |
| 1998 | 1.520 | 0.664 | 1.898 | 1.449 | 1.383 | 1.487 |
| 1999 | -0.691 | -2.303 | -0.889 | -1.081 | -1.232 | -1.036 |
| 2000 | 2.482 | 3.231 | 1.456 | 1.938 | 1.955 | 2.151 |

| Year | ARIMAX Order | | | | | |
|------|--------------|--------|--------|--------|--------|--------|
| | GDP | | | | | |
| | 204 | 300 | 301 | 302 | 303 | 304 |
| 1964 | 3.178 | 4.313 | 3.709 | 3.149 | 3.428 | 3.430 |
| 1965 | -0.344 | -0.774 | -0.552 | -0.334 | -0.432 | -0.438 |
| 1966 | -0.979 | -0.732 | -0.914 | -1.113 | -0.905 | -0.881 |
| 1967 | 0.069 | 0.021 | 0.089 | 0.227 | 0.255 | 0.178 |
| 1968 | 1.524 | 2.015 | 1.535 | 1.426 | 1.524 | 1.572 |
| 1969 | -0.525 | -1.820 | -1.844 | -1.051 | -1.200 | -1.063 |
| 1970 | 0.126 | -1.268 | -1.985 | -1.060 | -1.012 | -0.835 |
| 1971 | 4.275 | 4.637 | 6.918 | 7.233 | 7.610 | 5.956 |
| 1972 | -0.248 | 1.130 | -0.594 | -0.798 | -1.721 | -1.079 |
| 1973 | 3.942 | 2.007 | 2.391 | 0.790 | 0.763 | 2.491 |
| 1974 | -3.865 | -2.466 | -0.518 | -2.430 | 0.460 | -1.854 |
| 1975 | -6.967 | -1.603 | -2.832 | -4.385 | -7.094 | -5.012 |
| 1976 | -7.258 | -7.921 | -9.497 | -9.408 | -8.249 | -8.221 |
| 1977 | 2.969 | 2.190 | 4.977 | 4.067 | 5.373 | 5.516 |
| 1978 | 0.779 | 4.495 | 1.178 | 2.605 | 1.753 | 0.992 |
| 1979 | 3.885 | -0.756 | 1.376 | 3.071 | 1.927 | 1.314 |
| 1980 | -4.015 | -5.997 | -4.541 | -5.161 | -3.518 | -3.728 |
| 1981 | -2.980 | -4.899 | -4.243 | -5.012 | -7.672 | -4.945 |
| 1982 | -4.556 | -1.523 | -1.503 | -3.833 | -0.649 | -4.727 |
| 1983 | -2.315 | 0.313 | -0.174 | -1.388 | -3.797 | 0.346 |
| 1984 | -3.458 | 0.941 | 0.848 | -0.317 | 2.106 | 0.518 |
| 1985 | 1.509 | 2.779 | 2.236 | 1.834 | 0.938 | 0.151 |
| 1986 | 2.041 | 1.452 | 1.348 | 0.722 | 0.339 | 1.136 |
| 1987 | 5.195 | 3.405 | 3.732 | 2.331 | 4.328 | 3.955 |
| 1988 | 2.178 | 6.189 | 6.601 | 3.626 | 2.756 | 2.798 |
| 1989 | -6.251 | -3.360 | -4.441 | -6.659 | -5.434 | -6.152 |
| 1990 | -7.426 | -4.888 | -4.176 | -6.655 | -7.056 | -3.945 |
| 1991 | -7.780 | -6.731 | -8.166 | -7.684 | -6.785 | -7.831 |
| 1992 | -1.164 | -2.639 | -2.498 | 0.220 | -1.213 | -1.963 |
| 1993 | 3.857 | 0.604 | 0.306 | 4.161 | 4.196 | 3.831 |
| 1994 | 8.668 | 3.655 | 4.464 | 7.895 | 6.109 | 6.860 |
| 1995 | 5.467 | 0.612 | 0.921 | 3.129 | 2.946 | 0.736 |
| 1996 | 3.112 | -0.594 | -0.487 | 0.836 | -0.455 | 1.045 |
| 1997 | 1.569 | 2.677 | 3.312 | 3.109 | 4.219 | 3.747 |
| 1998 | -1.780 | 2.107 | 1.446 | 1.111 | 0.371 | -0.130 |
| 1999 | -1.922 | -0.769 | -0.987 | -1.502 | -1.887 | -1.367 |
| 2000 | 2.332 | 2.115 | 2.036 | 1.151 | 2.765 | 2.846 |

| Year | ARIMAX Order | | | | | VAR (1) |
|------|--------------|--------|--------|--------|--------|---------|
| | GDP | | | | | |
| | 400 | 401 | 402 | 403 | 404 | |
| 1964 | 3.326 | 3.457 | 3.154 | 3.482 | 2.957 | |
| 1965 | -0.378 | -0.416 | -0.331 | -0.369 | -0.282 | |
| 1966 | -1.016 | -0.953 | -1.072 | -0.885 | -1.163 | |
| 1967 | 0.187 | 0.187 | 0.192 | 0.231 | 0.178 | |
| 1968 | 1.359 | 1.518 | 1.186 | 1.514 | 0.966 | |
| 1969 | -1.123 | -0.958 | -1.004 | -1.057 | -1.016 | 3.425 |
| 1970 | -1.453 | -0.815 | -1.017 | -1.067 | -1.315 | -1.502 |
| 1971 | 7.121 | 6.346 | 7.202 | 6.573 | 7.241 | 1.893 |
| 1972 | -0.217 | -0.107 | -1.174 | -0.889 | -1.002 | 2.665 |
| 1973 | 2.507 | 2.674 | 2.402 | 3.322 | 2.162 | 1.766 |
| 1974 | -1.302 | -1.501 | -1.433 | -0.938 | -1.461 | 4.438 |
| 1975 | -7.091 | -7.361 | -7.553 | -6.460 | -7.749 | -8.323 |
| 1976 | -8.279 | -8.634 | -8.822 | -8.691 | -8.782 | -5.088 |
| 1977 | 5.800 | 5.601 | 4.977 | 5.910 | 4.897 | -0.721 |
| 1978 | 0.351 | 1.273 | 0.415 | 1.541 | 0.067 | 2.442 |
| 1979 | 2.963 | 1.876 | 2.984 | 2.466 | 2.356 | 2.089 |
| 1980 | -0.155 | -0.318 | -1.474 | -1.922 | -1.360 | -2.433 |
| 1981 | -5.960 | -5.081 | -5.208 | -4.092 | -5.657 | -6.667 |
| 1982 | -3.369 | -3.555 | -2.732 | -3.011 | -3.965 | -1.036 |
| 1983 | -1.982 | -2.209 | -2.250 | -2.754 | -2.384 | -0.627 |
| 1984 | -0.092 | -0.633 | -0.459 | -0.909 | -0.442 | 4.129 |
| 1985 | 2.238 | 1.786 | 1.219 | 2.103 | 0.767 | -0.701 |
| 1986 | 2.518 | 2.358 | 1.639 | 3.711 | 0.981 | -0.555 |
| 1987 | 4.325 | 4.487 | 3.575 | 5.987 | 2.523 | 3.796 |
| 1988 | 5.546 | 5.372 | 4.731 | 6.160 | 3.302 | 3.889 |
| 1989 | -5.231 | -5.094 | -5.887 | -5.518 | -7.190 | 1.474 |
| 1990 | -4.878 | -4.876 | -5.077 | -5.296 | -6.411 | -8.031 |
| 1991 | -8.510 | -7.720 | -7.928 | -8.424 | -8.723 | -11.748 |
| 1992 | -2.495 | -2.351 | -1.318 | -2.451 | -2.081 | -0.961 |
| 1993 | 4.306 | 4.328 | 4.657 | 2.710 | 4.472 | 4.156 |
| 1994 | 8.026 | 8.567 | 8.757 | 7.685 | 8.757 | 7.516 |
| 1995 | 3.752 | 4.636 | 5.318 | 4.137 | 5.113 | 4.577 |
| 1996 | -0.689 | 0.310 | 1.562 | -0.055 | 1.637 | 0.255 |
| 1997 | 1.453 | 1.429 | 3.240 | 0.150 | 3.727 | 0.519 |
| 1998 | -1.005 | -1.399 | -0.611 | -3.143 | 0.398 | -0.872 |
| 1999 | -2.046 | -2.661 | -2.367 | -2.727 | -1.232 | 1.258 |
| 2000 | 1.375 | 1.096 | 0.496 | 2.981 | 1.362 | -1.896 |

| Year | VAR (2) | VAR (3) | SES | HLT | BLT | MR |
|------|---------|---------|-------|-------|-------|--------|
| 1964 | | | 0.688 | 0.779 | 0.018 | |
| 1965 | | | 0.732 | 0.813 | 0.020 | -3.733 |
| 1966 | | | 0.699 | 0.784 | 0.019 | 2.662 |
| 1967 | | | 0.670 | 0.759 | 0.018 | -5.416 |
| 1968 | | | 0.645 | 0.736 | 0.017 | 1.376 |
| 1969 | 1.593 | -0.423 | 0.622 | 0.716 | 0.017 | -1.511 |
| 1970 | 2.000 | 6.032 | 0.517 | 0.628 | 0.014 | 2.684 |
| 1971 | 4.246 | 9.041 | 0.630 | 0.719 | 0.017 | 1.346 |
| 1972 | -0.054 | -2.706 | 0.755 | 0.821 | 0.020 | 1.411 |
| 1973 | -1.243 | -0.660 | 0.697 | 0.772 | 0.019 | 4.666 |
| 1974 | 6.882 | 4.713 | 0.791 | 0.849 | 0.021 | -2.481 |
| 1975 | -9.219 | -11.502 | 0.807 | 0.861 | 0.021 | -5.952 |
| 1976 | -8.070 | -6.426 | 0.553 | 0.649 | 0.015 | 0.793 |
| 1977 | 2.224 | 0.999 | 0.421 | 0.538 | 0.012 | 0.374 |
| 1978 | 4.926 | 4.913 | 0.467 | 0.575 | 0.013 | -0.389 |
| 1979 | -1.021 | 2.123 | 0.547 | 0.639 | 0.015 | -1.884 |
| 1980 | -2.591 | -0.372 | 0.620 | 0.698 | 0.017 | -5.865 |
| 1981 | -4.440 | -6.576 | 0.573 | 0.658 | 0.015 | -3.640 |
| 1982 | 0.183 | 0.514 | 0.485 | 0.583 | 0.013 | -0.764 |
| 1983 | 1.897 | -0.337 | 0.405 | 0.515 | 0.011 | -0.577 |
| 1984 | 4.813 | 2.708 | 0.382 | 0.494 | 0.010 | 3.682 |
| 1985 | -0.367 | -0.533 | 0.399 | 0.507 | 0.011 | 3.998 |
| 1986 | -0.384 | -2.201 | 0.431 | 0.532 | 0.011 | 4.040 |
| 1987 | 4.441 | 7.829 | 0.482 | 0.572 | 0.012 | 8.351 |
| 1988 | 3.060 | 2.809 | 0.635 | 0.697 | 0.016 | 5.368 |
| 1989 | -1.397 | -0.115 | 0.686 | 0.738 | 0.017 | -5.901 |
| 1990 | -7.532 | -8.822 | 0.540 | 0.617 | 0.014 | -9.347 |
| 1991 | -12.782 | -10.789 | 0.320 | 0.432 | 0.008 | -9.803 |
| 1992 | -2.997 | -3.336 | 0.120 | 0.265 | 0.003 | -4.762 |
| 1993 | 4.946 | 5.270 | 0.059 | 0.212 | 0.001 | 3.150 |
| 1994 | 6.738 | 5.609 | 0.128 | 0.267 | 0.003 | 4.925 |
| 1995 | 5.178 | 6.413 | 0.245 | 0.362 | 0.006 | 0.854 |
| 1996 | -0.720 | 0.430 | 0.264 | 0.375 | 0.006 | 0.904 |
| 1997 | 1.250 | 0.836 | 0.307 | 0.409 | 0.007 | 3.587 |
| 1998 | -1.784 | -2.682 | 0.379 | 0.467 | 0.008 | 3.528 |
| 1999 | 0.384 | -1.794 | 0.367 | 0.455 | 0.008 | -3.660 |
| 2000 | -1.036 | -1.848 | 0.332 | 0.425 | 0.007 | 3.461 |

| Year | Simple Regression | | | |
|------|-------------------|--------------------|---------------------|------------|
| | Bank Rate | Construction Costs | Construction Orders | Employment |
| 1964 | 0.129 | -0.032 | | -0.174 |
| 1965 | -0.040 | -0.032 | -3.909 | 0.754 |
| 1966 | 0.045 | -0.015 | -2.200 | 0.226 |
| 1967 | -0.089 | -0.009 | -2.973 | 0.126 |
| 1968 | 0.031 | -0.043 | 0.617 | -0.757 |
| 1969 | 0.023 | -0.026 | 0.082 | -0.438 |
| 1970 | -0.103 | -0.038 | 1.696 | -0.165 |
| 1971 | -0.188 | -0.055 | 3.243 | -0.638 |
| 1972 | 0.002 | -0.009 | -0.338 | -0.256 |
| 1973 | 0.233 | -0.049 | -0.641 | 0.891 |
| 1974 | 0.205 | -0.130 | -6.106 | 1.646 |
| 1975 | -0.148 | -0.193 | -3.837 | 0.153 |
| 1976 | 0.030 | 0.037 | 0.978 | 1.009 |
| 1977 | -0.270 | -0.061 | 0.098 | 0.545 |
| 1978 | -0.033 | 0.135 | 1.864 | -0.538 |
| 1979 | 0.379 | -0.198 | -1.869 | 0.349 |
| 1980 | 0.045 | -0.233 | 0.129 | -0.445 |
| 1981 | -0.294 | 0.117 | 2.404 | -2.222 |
| 1982 | -0.050 | 0.071 | -0.157 | -1.412 |
| 1983 | -0.205 | 0.146 | -0.112 | -1.062 |
| 1984 | -0.032 | -0.055 | 2.744 | 1.258 |
| 1985 | 0.171 | -0.089 | 0.780 | 0.141 |
| 1986 | -0.173 | 0.112 | 2.756 | -0.441 |
| 1987 | -0.173 | -0.072 | 7.086 | 0.630 |
| 1988 | -0.033 | -0.078 | 5.660 | 1.678 |
| 1989 | 0.006 | -0.221 | 0.175 | 1.139 |
| 1990 | 0.288 | -0.175 | -7.337 | 0.495 |
| 1991 | -0.209 | 0.192 | -6.649 | -2.295 |
| 1992 | -0.336 | 0.140 | -4.644 | -1.436 |
| 1993 | -0.273 | 0.135 | -0.135 | -1.605 |
| 1994 | -0.040 | -0.095 | 0.453 | -0.395 |
| 1995 | 0.034 | -0.118 | 1.070 | 0.210 |
| 1996 | -0.089 | 0.066 | 1.754 | -0.229 |
| 1997 | 0.030 | -0.089 | 2.561 | 0.723 |
| 1998 | -0.024 | -0.221 | 4.610 | -0.680 |
| 1999 | -0.169 | -0.100 | -4.170 | 0.992 |
| 2000 | -0.001 | -0.036 | -0.208 | 0.904 |

| Year | Simple Regression | | |
|------|-------------------|---------------------|---------------------|
| | GDP | Construction Output | Construction Starts |
| 1964 | 4.784 | -0.245 | -0.184 |
| 1965 | -0.488 | -0.310 | -0.072 |
| 1966 | -0.977 | 0.197 | 0.378 |
| 1967 | -0.100 | -0.152 | -0.293 |
| 1968 | 2.710 | 0.617 | -0.280 |
| 1969 | -0.739 | 0.039 | -0.134 |
| 1970 | -0.460 | -0.050 | 0.141 |
| 1971 | -0.704 | -0.463 | 0.039 |
| 1972 | 1.828 | 0.457 | -0.123 |
| 1973 | 7.564 | 0.023 | -0.421 |
| 1974 | -6.225 | 0.920 | 0.392 |
| 1975 | -5.103 | 0.917 | 0.015 |
| 1976 | 0.177 | 1.060 | -0.321 |
| 1977 | -0.240 | 0.240 | -0.011 |
| 1978 | 1.144 | -0.460 | -0.217 |
| 1979 | 0.254 | 0.550 | -0.385 |
| 1980 | -7.392 | 0.197 | -0.004 |
| 1981 | -6.068 | 0.114 | 0.219 |
| 1982 | -0.528 | -0.672 | 0.150 |
| 1983 | 1.885 | 0.039 | -0.118 |
| 1984 | 0.265 | -0.423 | 0.006 |
| 1985 | 1.775 | -0.521 | 0.077 |
| 1986 | 2.408 | -0.762 | 0.094 |
| 1987 | 3.296 | -1.782 | 0.118 |
| 1988 | 4.058 | -1.546 | -0.281 |
| 1989 | -0.400 | -3.616 | -0.201 |
| 1990 | -2.834 | -1.946 | 0.003 |
| 1991 | -6.353 | 2.674 | -0.004 |
| 1992 | -3.859 | 3.310 | -0.033 |
| 1993 | -0.496 | 2.515 | 0.156 |
| 1994 | 2.839 | 0.245 | 0.097 |
| 1995 | 0.849 | -0.138 | -0.173 |
| 1996 | 0.579 | -1.097 | 0.041 |
| 1997 | 1.263 | -1.433 | 0.080 |
| 1998 | 1.748 | -1.120 | -0.067 |
| 1999 | 1.531 | -1.904 | 0.018 |
| 2000 | 2.248 | 0.143 | -0.025 |

B.2 Out-of-sample

| Year | IPD Rents | ARIMA (1,0,2) | ARIMAX (1,0,2) | ARIMAX (1,0,2) | ARIMAX (1,0,2) |
|------|-----------|------------------|-------------------|-------------------|-------------------|
| | | | B.Rate | C. Orders | C. Costs |
| 2001 | -3.611 | 0.809 | 0.218 | -2.303 | 1.069 |
| 2002 | -4.250 | -1.688 | -1.807 | -2.36 | -1.236 |
| 2003 | -0.734 | -1.032 | -1.064 | -2.647 | -1.391 |
| 2004 | 3.876 | -0.659 | -0.586 | 1.356 | -0.53 |
| 2005 | 0.401 | -0.447 | -0.430 | 0.450 | -0.607 |
| 2006 | 1.543 | -0.326 | -0.289 | 4.151 | -0.581 |
| 2007 | 0.063 | -0.258 | -0.200 | -0.056 | -0.121 |
| 2008 | -5.500 | -0.218 | -0.369 | -6.805 | -1.051 |
| 2009 | -6.700 | -0.196 | -0.481 | -7.496 | -1.833 |
| 2010 | 7.100 | -0.184 | -0.239 | 0.523 | 0.32 |

| Year | ARIMAX (1,0,2) | ARIMAX (1,0,2) | ARIMAX (1,0,2) | ARIMAX (4,0,0) | SES |
|------|-------------------|-------------------|-------------------|-------------------|-------|
| | C. Output | C. Starts | Employment | GDP | |
| 2001 | 0.738 | 0.859 | 0.662 | -0.844 | 0.349 |
| 2002 | -1.797 | -1.463 | -1.804 | -1.077 | 0.349 |
| 2003 | -1.095 | -0.787 | -1.011 | 2.007 | 0.349 |
| 2004 | -0.684 | -0.416 | -0.641 | 1.75 | 0.349 |
| 2005 | -0.468 | -0.393 | -0.392 | -0.783 | 0.349 |
| 2006 | -0.324 | -0.257 | -0.293 | 0.158 | 0.349 |
| 2007 | -0.253 | -0.164 | -0.321 | -0.014 | 0.349 |
| 2008 | -0.229 | -0.828 | -0.223 | -3.827 | 0.349 |
| 2009 | -0.259 | -0.339 | -0.550 | -8.577 | 0.349 |
| 2010 | -0.198 | 0.036 | -0.469 | -0.716 | 0.349 |

| Year | HLT | BLT | MR | VAR (1) | VAR (2) |
|------|-------|-------|---------|---------|---------|
| 2001 | 0.438 | 0.007 | 0.207 | 1.365 | -4.876 |
| 2002 | 0.437 | 0.007 | -1.748 | -0.307 | -1.792 |
| 2003 | 0.437 | 0.007 | 0.034 | -1.357 | -2.197 |
| 2004 | 0.437 | 0.006 | 3.773 | 0.641 | -1.665 |
| 2005 | 0.437 | 0.006 | 0.925 | -0.076 | -0.114 |
| 2006 | 0.436 | 0.006 | 4.653 | -0.344 | -1.028 |
| 2007 | 0.436 | 0.006 | -0.912 | -1.385 | 1.627 |
| 2008 | 0.436 | 0.005 | -17.340 | -2.899 | -1.107 |
| 2009 | 0.436 | 0.005 | -16.698 | -5.668 | -10.470 |
| 2010 | 0.435 | 0.005 | 1.004 | -0.477 | -12.420 |

| Year | VAR (3) | Simple Regression | | | |
|------|---------|-------------------|------------------------|-----------------------|------------------------|
| | | Bank Rate | Construction Orders | Construction Costs | Construction Output |
| 2001 | -8.723 | -0.117 | -1.195 | -0.183 | 0.323 |
| 2002 | -3.219 | -0.122 | -2.021 | -0.307 | -0.269 |
| 2003 | 0.305 | -0.068 | -3.523 | 0.228 | 0.736 |
| 2004 | 0.869 | 0.020 | 3.553 | -0.099 | -0.889 |
| 2005 | -3.273 | -0.029 | 1.610 | 0.088 | 0.112 |
| 2006 | 2.060 | -0.008 | 8.473 | 0.147 | -2.131 |
| 2007 | 2.984 | 0.013 | 0.484 | -0.115 | -2.280 |
| 2008 | -0.494 | -0.171 | -12.273 | 0.524 | -0.278 |
| 2009 | -14.590 | -0.290 | -13.590 | 1.055 | 6.119 |
| 2010 | -18.408 | -0.082 | 1.525 | -0.363 | 0.140 |

| Year | Simple Regression | | |
|------|---------------------|------------|---------|
| | Construction Starts | Employment | GDP |
| 2001 | 0.032 | 0.834 | -0.108 |
| 2002 | 0.013 | 0.260 | -0.699 |
| 2003 | 0.076 | 0.592 | 0.454 |
| 2004 | 0.104 | 0.306 | 0.685 |
| 2005 | -0.020 | 0.468 | -0.576 |
| 2006 | 0.002 | 0.291 | 0.421 |
| 2007 | 0.026 | -0.391 | 0.254 |
| 2008 | -0.497 | 0.033 | -4.203 |
| 2009 | -0.145 | -2.430 | -11.997 |
| 2010 | 0.128 | -1.937 | -1.825 |

B.3 SA Combination Forecasting

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|---------------|--------------|---------------|--------------|
| | SES/ HES | SES/BES | SES/ARMA | SES/ ARMAXBR | SES/ ARMAXCC |
| 2001 | 0.394 | 0.178 | 0.579 | 0.284 | 0.709 |
| 2002 | 0.393 | 0.178 | -0.670 | -0.729 | -0.444 |
| 2003 | 0.393 | 0.178 | -0.342 | -0.358 | -0.521 |
| 2004 | 0.393 | 0.178 | -0.155 | -0.119 | -0.091 |
| 2005 | 0.393 | 0.178 | -0.049 | -0.041 | -0.129 |
| 2006 | 0.393 | 0.178 | 0.012 | 0.030 | -0.116 |
| 2007 | 0.393 | 0.178 | 0.046 | 0.075 | 0.114 |
| 2008 | 0.393 | 0.177 | 0.066 | -0.010 | -0.351 |
| 2009 | 0.393 | 0.177 | 0.077 | -0.066 | -0.742 |
| 2010 | 0.392 | 0.177 | 0.083 | 0.055 | 0.335 |
| | SES/ ARMAXCOr | SES/ ARMAXCOu | SES/ ARMAXCS | SES / ARMAXBR | SES/ ARMAXE |
| 2001 | -0.977 | 0.544 | 0.604 | 0.284 | 0.506 |
| 2002 | -1.006 | -0.724 | -0.557 | -0.729 | -0.728 |
| 2003 | -1.149 | -0.373 | -0.219 | -0.358 | -0.331 |
| 2004 | 0.853 | -0.168 | -0.034 | -0.119 | -0.146 |
| 2005 | 0.400 | -0.060 | -0.022 | -0.041 | -0.022 |
| 2006 | 2.250 | 0.013 | 0.046 | 0.030 | 0.028 |
| 2007 | 0.147 | 0.048 | 0.093 | 0.075 | 0.014 |
| 2008 | -3.228 | 0.060 | -0.240 | -0.010 | 0.063 |
| 2009 | -3.574 | 0.045 | 0.005 | -0.066 | -0.101 |
| 2010 | 0.436 | 0.076 | 0.193 | 0.055 | -0.060 |
| | SES/ ARMAGDP | SES/ SRBR | SES/ SRCC | SES/ SRCOr | SES/ ARMAGDP |
| 2001 | -0.248 | 0.116 | 0.083 | -0.423 | -0.248 |
| 2002 | -0.364 | 0.114 | 0.021 | -0.836 | -0.364 |
| 2003 | 1.178 | 0.140 | 0.289 | -1.587 | 1.178 |
| 2004 | 1.050 | 0.184 | 0.125 | 1.951 | 1.050 |
| 2005 | -0.217 | 0.160 | 0.219 | 0.980 | -0.217 |
| 2006 | 0.254 | 0.170 | 0.248 | 4.411 | 0.254 |
| 2007 | 0.168 | 0.181 | 0.117 | 0.416 | 0.168 |
| 2008 | -1.739 | 0.089 | 0.436 | -5.962 | -1.739 |
| 2009 | -4.114 | 0.030 | 0.702 | -6.621 | -4.114 |
| 2010 | -0.184 | 0.133 | -0.007 | 0.937 | -0.184 |
| | SES/ SRCOu | SES/ SRCS | SES/ SRE | SES/ SRGDP | SES/ MR |
| 2001 | 0.336 | 0.191 | 0.592 | 0.120 | 0.278 |
| 2002 | 0.040 | 0.181 | 0.305 | -0.175 | -0.699 |
| 2003 | 0.543 | 0.213 | 0.470 | 0.402 | 0.192 |
| 2004 | -0.270 | 0.226 | 0.328 | 0.517 | 2.061 |
| 2005 | 0.231 | 0.164 | 0.409 | -0.113 | 0.637 |
| 2006 | -0.891 | 0.175 | 0.320 | 0.385 | 2.501 |
| 2007 | -0.965 | 0.187 | -0.021 | 0.302 | -0.281 |
| 2008 | 0.036 | -0.074 | 0.191 | -1.927 | -8.495 |
| 2009 | 3.234 | 0.102 | -1.040 | -5.824 | -8.174 |
| 2010 | 0.244 | 0.239 | -0.794 | -0.738 | 0.677 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|------------------|-----------------|-----------------|------------------|
| | SES/ VAR | HES/ BES | HES/ ARMA | HES/ ARMAXBR | HES/ ARMAXCC |
| 2001 | 1.714 | 0.223 | 0.624 | 0.328 | 0.754 |
| 2002 | 0.042 | 0.222 | -0.626 | -0.685 | -0.400 |
| 2003 | -1.008 | 0.222 | -0.298 | -0.314 | -0.477 |
| 2004 | 0.990 | 0.222 | -0.111 | -0.075 | -0.047 |
| 2005 | 0.273 | 0.222 | -0.005 | 0.004 | -0.085 |
| 2006 | 0.005 | 0.221 | 0.055 | 0.074 | -0.073 |
| 2007 | -1.036 | 0.221 | 0.089 | 0.118 | 0.158 |
| 2008 | -2.550 | 0.221 | 0.109 | 0.034 | -0.308 |
| 2009 | -5.319 | 0.221 | 0.120 | -0.023 | -0.699 |
| 2010 | -0.128 | 0.220 | 0.126 | 0.098 | 0.378 |
| | HES/ ARMAXCOr | HES/ ARMAXCOu | HES/ ARMAXCS | HES/ ARMAXE | HES/ ARMAXGDP |
| 2001 | -0.933 | 0.588 | 0.649 | 0.550 | -0.203 |
| 2002 | -0.962 | -0.680 | -0.513 | -0.684 | -0.320 |
| 2003 | -1.105 | -0.329 | -0.175 | -0.287 | 1.222 |
| 2004 | 0.897 | -0.124 | 0.011 | -0.102 | 1.094 |
| 2005 | 0.444 | -0.016 | 0.022 | 0.023 | -0.173 |
| 2006 | 2.294 | 0.056 | 0.090 | 0.072 | 0.297 |
| 2007 | 0.190 | 0.092 | 0.136 | 0.058 | 0.211 |
| 2008 | -3.185 | 0.104 | -0.196 | 0.107 | -1.696 |
| 2009 | -3.530 | 0.089 | 0.049 | -0.057 | -4.071 |
| 2010 | 0.479 | 0.119 | 0.236 | -0.017 | -0.141 |
| | HES/ SRBR | HES/ SRCC | HES/ SRCOr | HES/ SRCOu | HES/ SRCS |
| 2001 | 0.160 | 0.127 | -0.379 | 0.381 | 0.235 |
| 2002 | 0.158 | 0.065 | -0.792 | 0.084 | 0.225 |
| 2003 | 0.184 | 0.333 | -1.543 | 0.587 | 0.257 |
| 2004 | 0.228 | 0.169 | 1.995 | -0.226 | 0.270 |
| 2005 | 0.204 | 0.263 | 1.024 | 0.275 | 0.208 |
| 2006 | 0.214 | 0.291 | 4.455 | -0.848 | 0.219 |
| 2007 | 0.224 | 0.160 | 0.460 | -0.922 | 0.231 |
| 2008 | 0.132 | 0.480 | -5.919 | 0.079 | -0.030 |
| 2009 | 0.073 | 0.745 | -6.577 | 3.278 | 0.145 |
| 2010 | 0.176 | 0.036 | 0.980 | 0.287 | 0.282 |
| | HES/ SRE | HES/ SRGDP | HES/ MR | HES/ VAR | BES/ ARMA |
| 2001 | 0.636 | 0.165 | 0.323 | 0.902 | 0.408 |
| 2002 | 0.349 | -0.131 | -0.655 | 0.065 | -0.841 |
| 2003 | 0.514 | 0.446 | 0.236 | -0.460 | -0.513 |
| 2004 | 0.372 | 0.561 | 2.105 | 0.539 | -0.327 |
| 2005 | 0.453 | -0.069 | 0.681 | 0.181 | -0.221 |
| 2006 | 0.363 | 0.428 | 2.544 | 0.046 | -0.160 |
| 2007 | 0.022 | 0.345 | -0.238 | -0.475 | -0.126 |
| 2008 | 0.234 | -1.883 | -8.452 | -1.231 | -0.107 |
| 2009 | -0.997 | -5.780 | -8.131 | -2.616 | -0.096 |
| 2010 | -0.751 | -0.695 | 0.720 | -0.021 | -0.090 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|------------------|------------------------------|-------------------------------|-------------------------------|
| | BES/ ARMAXBR | BES/ ARMAXCC | BES/ ARMAXCO _r | BES/ ARMAXCO _u | BES/ ARMAXCS |
| 2001 | 0.113 | 0.538 | -1.148 | 0.373 | 0.433 |
| 2002 | -0.900 | -0.615 | -1.177 | -0.895 | -0.728 |
| 2003 | -0.529 | -0.692 | -1.320 | -0.544 | -0.390 |
| 2004 | -0.290 | -0.262 | 0.681 | -0.339 | -0.205 |
| 2005 | -0.212 | -0.301 | 0.228 | -0.231 | -0.194 |
| 2006 | -0.142 | -0.288 | 2.079 | -0.159 | -0.126 |
| 2007 | -0.097 | -0.058 | -0.025 | -0.124 | -0.079 |
| 2008 | -0.182 | -0.523 | -3.400 | -0.112 | -0.412 |
| 2009 | -0.238 | -0.914 | -3.746 | -0.127 | -0.167 |
| 2010 | -0.117 | 0.163 | 0.264 | -0.097 | 0.021 |
| | BES/ ARMAXE | BES/ ARMAXGDP | BES/ SRBR | BES/ SRCC | BES/ SRCO _r |
| | | | | | |
| 2001 | 0.335 | -0.419 | -0.055 | -0.088 | -0.594 |
| 2002 | -0.899 | -0.535 | -0.057 | -0.150 | -1.007 |
| 2003 | -0.502 | 1.007 | -0.031 | 0.118 | -1.758 |
| 2004 | -0.318 | 0.878 | 0.013 | -0.046 | 1.779 |
| 2005 | -0.193 | -0.389 | -0.012 | 0.047 | 0.808 |
| 2006 | -0.144 | 0.082 | -0.001 | 0.076 | 4.240 |
| 2007 | -0.158 | -0.004 | 0.009 | -0.055 | 0.245 |
| 2008 | -0.109 | -1.911 | -0.083 | 0.264 | -6.134 |
| 2009 | -0.273 | -4.286 | -0.142 | 0.530 | -6.793 |
| 2010 | -0.232 | -0.356 | -0.039 | -0.179 | 0.765 |
| | BES/ SRCO _u | BES/ SRCS | BES/ SRE | BES/ SRGDP | BES/ MR |
| | | | | | |
| 2001 | 0.165 | 0.020 | 0.421 | -0.051 | 0.107 |
| 2002 | -0.131 | 0.010 | 0.134 | -0.346 | -0.870 |
| 2003 | 0.372 | 0.042 | 0.299 | 0.231 | 0.021 |
| 2004 | -0.442 | 0.055 | 0.156 | 0.346 | 1.889 |
| 2005 | 0.059 | -0.007 | 0.237 | -0.285 | 0.466 |
| 2006 | -1.063 | 0.004 | 0.148 | 0.213 | 2.329 |
| 2007 | -1.137 | 0.016 | -0.193 | 0.130 | -0.453 |
| 2008 | -0.136 | -0.246 | 0.019 | -2.099 | -8.667 |
| 2009 | 3.062 | -0.070 | -1.212 | -5.996 | -8.346 |
| 2010 | 0.072 | 0.067 | -0.966 | -0.910 | 0.505 |
| | BES/ VAR | ARMA/ ARMAXBR | ARMA/ ARMAXCC | ARMA/ ARMAXCO _r | ARMA/ ARMAXCO _u |
| | | | | | |
| 2001 | 0.686 | 0.514 | 0.939 | -0.747 | 0.774 |
| 2002 | -0.150 | -1.748 | -1.462 | -2.024 | -1.743 |
| 2003 | -0.675 | -1.048 | -1.212 | -1.840 | -1.064 |
| 2004 | 0.323 | -0.623 | -0.595 | 0.349 | -0.672 |
| 2005 | -0.035 | -0.439 | -0.527 | 0.002 | -0.458 |
| 2006 | -0.169 | -0.308 | -0.454 | 1.913 | -0.325 |
| 2007 | -0.690 | -0.229 | -0.190 | -0.157 | -0.256 |
| 2008 | -1.447 | -0.294 | -0.635 | -3.512 | -0.224 |
| 2009 | -2.832 | -0.339 | -1.015 | -3.846 | -0.228 |
| 2010 | -0.236 | -0.212 | 0.068 | 0.170 | -0.191 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|--------------------|----------------------|---------------------|----------------------|
| | ARMA/ ARMAXCS | ARMA/ ARMAXE | ARMA/ ARMAXGDP | ARMA/ SRBR | ARMA/ SRCC |
| 2001 | 0.834 | 0.736 | -0.018 | 0.346 | 0.313 |
| 2002 | -1.576 | -1.746 | -1.383 | -0.905 | -0.998 |
| 2003 | -0.910 | -1.022 | 0.488 | -0.550 | -0.402 |
| 2004 | -0.538 | -0.650 | 0.546 | -0.320 | -0.379 |
| 2005 | -0.420 | -0.420 | -0.615 | -0.238 | -0.179 |
| 2006 | -0.292 | -0.310 | -0.084 | -0.167 | -0.090 |
| 2007 | -0.211 | -0.290 | -0.136 | -0.123 | -0.187 |
| 2008 | -0.523 | -0.221 | -2.023 | -0.195 | 0.153 |
| 2009 | -0.268 | -0.373 | -4.387 | -0.243 | 0.429 |
| 2010 | -0.074 | -0.327 | -0.450 | -0.133 | -0.273 |
| | ARMA/ SRCOr | ARMA/ SRCOu | ARMA/ SRCs | ARMA/ SRE | ARMA/ SRGDP |
| | | | | | |
| 2001 | -0.193 | 0.566 | 0.421 | 0.822 | 0.350 |
| 2002 | -1.854 | -0.978 | -0.837 | -0.714 | -1.193 |
| 2003 | -2.277 | -0.148 | -0.478 | -0.220 | -0.289 |
| 2004 | 1.447 | -0.774 | -0.278 | -0.176 | 0.013 |
| 2005 | 0.582 | -0.167 | -0.234 | 0.011 | -0.511 |
| 2006 | 4.074 | -1.229 | -0.162 | -0.018 | 0.047 |
| 2007 | 0.113 | -1.269 | -0.116 | -0.325 | -0.002 |
| 2008 | -6.246 | -0.248 | -0.357 | -0.093 | -2.210 |
| 2009 | -6.893 | 2.962 | -0.171 | -1.313 | -6.096 |
| 2010 | 0.670 | -0.022 | -0.028 | -1.060 | -1.005 |
| | ARMA/ MR | ARMA/ VAR | ARMAXBR/ ARMAXCC | ARMAXBR/ ARMAXCO | ARMAXBR/ ARMAXCOu |
| | | | | | |
| 2001 | 0.508 | 1.087 | 0.644 | -1.043 | 0.478 |
| 2002 | -1.718 | -0.998 | -1.522 | -2.084 | -1.802 |
| 2003 | -0.499 | -1.195 | -1.228 | -1.856 | -1.080 |
| 2004 | 1.557 | -0.009 | -0.558 | 0.385 | -0.635 |
| 2005 | 0.239 | -0.261 | -0.519 | 0.010 | -0.449 |
| 2006 | 2.163 | -0.335 | -0.435 | 1.931 | -0.307 |
| 2007 | -0.585 | -0.822 | -0.161 | -0.128 | -0.227 |
| 2008 | -8.779 | -1.558 | -0.710 | -3.587 | -0.299 |
| 2009 | -8.447 | -2.932 | -1.157 | -3.989 | -0.370 |
| 2010 | 0.410 | -0.331 | 0.041 | 0.142 | -0.219 |
| | ARMAXRB/ ARMAXCS | ARMAXBR/ ARMAXE | ARMAXBR/ ARMAXGDP | ARMAXBR/ SRBR | ARMAXBR/ SRCC |
| | | | | | |
| 2001 | 0.539 | 0.440 | -0.313 | 0.050 | 0.017 |
| 2002 | -1.635 | -1.806 | -1.442 | -0.964 | -1.057 |
| 2003 | -0.926 | -1.038 | 0.472 | -0.566 | -0.418 |
| 2004 | -0.501 | -0.614 | 0.582 | -0.283 | -0.342 |
| 2005 | -0.412 | -0.411 | -0.607 | -0.230 | -0.171 |
| 2006 | -0.273 | -0.291 | -0.066 | -0.149 | -0.071 |
| 2007 | -0.182 | -0.261 | -0.107 | -0.094 | -0.158 |
| 2008 | -0.599 | -0.296 | -2.098 | -0.270 | 0.077 |
| 2009 | -0.410 | -0.516 | -4.529 | -0.385 | 0.287 |
| 2010 | -0.102 | -0.354 | -0.478 | -0.161 | -0.301 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|----------------------|----------------------|----------------------|---------------------|
| | ARMAXBR/ SRCOr | ARMAXBR/ SRCOu | ARMAXBR/ SRCS | ARMAXBR/ SRE | ARMAXBR/ SRGDP |
| 2001 | -0.489 | 0.271 | 0.125 | 0.526 | 0.055 |
| 2002 | -1.914 | -1.038 | -0.897 | -0.773 | -1.253 |
| 2003 | -2.293 | -0.164 | -0.494 | -0.236 | -0.305 |
| 2004 | 1.483 | -0.738 | -0.241 | -0.140 | 0.050 |
| 2005 | 0.590 | -0.159 | -0.225 | 0.019 | -0.503 |
| 2006 | 4.092 | -1.210 | -0.144 | 0.001 | 0.066 |
| 2007 | 0.142 | -1.240 | -0.087 | -0.296 | 0.027 |
| 2008 | -6.321 | -0.323 | -0.433 | -0.168 | -2.286 |
| 2009 | -7.036 | 2.819 | -0.313 | -1.455 | -6.239 |
| 2010 | 0.643 | -0.050 | -0.055 | -1.088 | -1.032 |
| | ARMAXBR/ MR | ARMAXBR/ VAR | ARMAXCC/ ARMAXCOr | ARMAXCC/ ARMAXCOu | ARMAXCC/ ARMAXCS |
| 2001 | 0.213 | 0.792 | -0.617 | 0.904 | 0.964 |
| 2002 | -1.777 | -1.057 | -1.798 | -1.517 | -1.350 |
| 2003 | -0.515 | -1.211 | -2.019 | -1.243 | -1.089 |
| 2004 | 1.593 | 0.027 | 0.413 | -0.607 | -0.473 |
| 2005 | 0.248 | -0.253 | -0.079 | -0.538 | -0.500 |
| 2006 | 2.182 | -0.317 | 1.785 | -0.453 | -0.419 |
| 2007 | -0.556 | -0.793 | -0.089 | -0.187 | -0.143 |
| 2008 | -8.854 | -1.634 | -3.928 | -0.640 | -0.940 |
| 2009 | -8.589 | -3.075 | -4.665 | -1.046 | -1.086 |
| 2010 | 0.383 | -0.358 | 0.422 | 0.061 | 0.178 |
| | ARMAXCC/ ARMAXE | ARMAXCC/ ARMAXGDP | ARMAXCC/ SRBR | ARMAXCC/ SRCC | ARMAXCC/ SRCOr |
| 2001 | 0.866 | 0.113 | 0.476 | 0.443 | -0.063 |
| 2002 | -1.520 | -1.157 | -0.679 | -0.772 | -1.628 |
| 2003 | -1.201 | 0.308 | -0.730 | -0.581 | -2.457 |
| 2004 | -0.586 | 0.610 | -0.255 | -0.314 | 1.511 |
| 2005 | -0.500 | -0.695 | -0.318 | -0.259 | 0.502 |
| 2006 | -0.437 | -0.212 | -0.295 | -0.217 | 3.946 |
| 2007 | -0.221 | -0.068 | -0.054 | -0.118 | 0.181 |
| 2008 | -0.637 | -2.439 | -0.611 | -0.264 | -6.662 |
| 2009 | -1.192 | -5.205 | -1.061 | -0.389 | -7.712 |
| 2010 | -0.075 | -0.198 | 0.119 | -0.021 | 0.922 |
| | ARMAXCC/ SRCOu | ARMAXCC/ SRCS | ARMAXCC/ SRE | ARMAXCC/ SRGDP | ARMAXCC/ MR |
| 2001 | 0.696 | 0.551 | 0.952 | 0.480 | 0.638 |
| 2002 | -0.752 | -0.611 | -0.488 | -0.967 | -1.492 |
| 2003 | -0.327 | -0.657 | -0.400 | -0.468 | -0.678 |
| 2004 | -0.710 | -0.213 | -0.112 | 0.078 | 1.621 |
| 2005 | -0.247 | -0.314 | -0.069 | -0.591 | 0.159 |
| 2006 | -1.356 | -0.290 | -0.145 | -0.080 | 2.036 |
| 2007 | -1.200 | -0.048 | -0.256 | 0.067 | -0.516 |
| 2008 | -0.664 | -0.774 | -0.509 | -2.627 | -9.195 |
| 2009 | 2.143 | -0.989 | -2.131 | -6.915 | -9.265 |
| 2010 | 0.230 | 0.224 | -0.808 | -0.753 | 0.662 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|-----------------------|--------------------|--------------------|----------------------|
| | ARMAXCoR/ SRBR | ARMAXCoR/ SRCC | ARMAXCoR/ SRCOr | ARMAXCoR/ SRCOu | ARMAXCoR/ SRCs |
| 2001 | -1.210 | -1.243 | -1.749 | -0.990 | -1.135 |
| 2002 | -1.241 | -1.334 | -2.190 | -1.314 | -1.173 |
| 2003 | -1.358 | -1.209 | -3.085 | -0.955 | -1.285 |
| 2004 | 0.688 | 0.629 | 2.454 | 0.233 | 0.730 |
| 2005 | 0.210 | 0.269 | 1.030 | 0.281 | 0.215 |
| 2006 | 2.071 | 2.149 | 6.312 | 1.010 | 2.076 |
| 2007 | -0.022 | -0.086 | 0.214 | -1.168 | -0.015 |
| 2008 | -3.488 | -3.141 | -9.539 | -3.541 | -3.651 |
| 2009 | -3.893 | -3.221 | -10.543 | -0.688 | -3.821 |
| 2010 | 0.220 | 0.080 | 1.024 | 0.331 | 0.326 |
| | ARMAXCoR/ SRCE | ARMAXCoR/ SRGDP | ARMAXCoR/ MR | ARMAXCoR/ VAR | ARMAXCoU/ ARMAXCS |
| | | | | | |
| 2001 | -0.734 | -1.206 | -1.048 | -0.469 | 0.799 |
| 2002 | -1.050 | -1.529 | -2.054 | -1.334 | -1.630 |
| 2003 | -1.028 | -1.096 | -1.306 | -2.002 | -0.941 |
| 2004 | 0.831 | 1.021 | 2.564 | 0.998 | -0.550 |
| 2005 | 0.459 | -0.063 | 0.688 | 0.187 | -0.431 |
| 2006 | 2.221 | 2.286 | 4.402 | 1.903 | -0.291 |
| 2007 | -0.224 | 0.099 | -0.484 | -0.721 | -0.209 |
| 2008 | -3.386 | -5.504 | -12.072 | -4.852 | -0.529 |
| 2009 | -4.963 | -9.746 | -12.097 | -6.582 | -0.299 |
| 2010 | -0.707 | -0.651 | 0.764 | 0.023 | -0.081 |
| | ARMAXCoU/ ARMAXE | ARMAXCoU/ ARMAXGDP | ARMAXCoU/ SRBR | ARMAXCoU/ SRCC | ARMAXCoU/ SRCOr |
| | | | | | |
| 2001 | 0.700 | -0.053 | 0.310 | 0.277 | -0.229 |
| 2002 | -1.801 | -1.437 | -0.959 | -1.052 | -1.909 |
| 2003 | -1.053 | 0.456 | -0.582 | -0.433 | -2.309 |
| 2004 | -0.663 | 0.533 | -0.332 | -0.391 | 1.434 |
| 2005 | -0.430 | -0.626 | -0.249 | -0.190 | 0.571 |
| 2006 | -0.309 | -0.083 | -0.166 | -0.089 | 4.075 |
| 2007 | -0.287 | -0.134 | -0.120 | -0.184 | 0.115 |
| 2008 | -0.226 | -2.028 | -0.200 | 0.147 | -6.251 |
| 2009 | -0.405 | -4.418 | -0.274 | 0.398 | -6.925 |
| 2010 | -0.334 | -0.457 | -0.140 | -0.280 | 0.663 |
| | ARMAXCoU/ SRCOu | ARMAXCoU/ SRCs | ARMAXCoU/ SRCE | ARMAXCoU/ SRGDP | ARMAXCoU/ MR |
| | | | | | |
| 2001 | 0.531 | 0.385 | 0.786 | 0.315 | 0.473 |
| 2002 | -1.033 | -0.892 | -0.768 | -1.248 | -1.772 |
| 2003 | -0.179 | -0.509 | -0.252 | -0.320 | -0.530 |
| 2004 | -0.787 | -0.290 | -0.189 | 0.001 | 1.544 |
| 2005 | -0.178 | -0.244 | 0.000 | -0.522 | 0.229 |
| 2006 | -1.228 | -0.161 | -0.017 | 0.048 | 2.164 |
| 2007 | -1.266 | -0.114 | -0.322 | 0.001 | -0.582 |
| 2008 | -0.253 | -0.363 | -0.098 | -2.216 | -8.784 |
| 2009 | 2.930 | -0.202 | -1.344 | -6.128 | -8.478 |
| 2010 | -0.029 | -0.035 | -1.067 | -1.012 | 0.403 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|--------------------|----------------------|------------------|-------------------|
| | ARMAXCOu/ VAR | ARMAXCS/ ARMAXE | ARMAXCS/ ARMAXGDP | ARMAXCS/ SRBR | ARMAXCS/ SRCC |
| 2001 | 1.052 | 0.761 | 0.008 | 0.371 | 0.338 |
| 2002 | -1.052 | -1.634 | -1.270 | -0.792 | -0.885 |
| 2003 | -1.226 | -0.899 | 0.610 | -0.428 | -0.279 |
| 2004 | -0.022 | -0.529 | 0.667 | -0.198 | -0.257 |
| 2005 | -0.272 | -0.393 | -0.588 | -0.211 | -0.152 |
| 2006 | -0.334 | -0.275 | -0.050 | -0.133 | -0.055 |
| 2007 | -0.819 | -0.243 | -0.089 | -0.076 | -0.140 |
| 2008 | -1.564 | -0.526 | -2.328 | -0.500 | -0.152 |
| 2009 | -2.964 | -0.445 | -4.458 | -0.314 | 0.358 |
| 2010 | -0.338 | -0.217 | -0.340 | -0.023 | -0.163 |
| | ARMAXCS/ SRCOr | ARMAXCS/ SRCOu | ARMAXCS/ SRCS | ARMAXCS/ SRCE | ARMAXCS/ SRGDP |
| 2001 | -0.168 | 0.591 | 0.446 | 0.847 | 0.375 |
| 2002 | -1.742 | -0.866 | -0.725 | -0.601 | -1.081 |
| 2003 | -2.155 | -0.025 | -0.355 | -0.098 | -0.166 |
| 2004 | 1.568 | -0.653 | -0.156 | -0.055 | 0.135 |
| 2005 | 0.609 | -0.140 | -0.207 | 0.038 | -0.484 |
| 2006 | 4.108 | -1.194 | -0.128 | 0.017 | 0.082 |
| 2007 | 0.160 | -1.222 | -0.069 | -0.278 | 0.045 |
| 2008 | -6.551 | -0.553 | -0.662 | -0.398 | -2.515 |
| 2009 | -6.965 | 2.890 | -0.242 | -1.384 | -6.168 |
| 2010 | 0.780 | 0.088 | 0.082 | -0.950 | -0.895 |
| | ARMAXCS/ MR | ARMAXCS/ VAR | ARMAXE/ ARMAXGDP | ARMAXE/ SRBR | ARMAXE/ SRCC |
| 2001 | 0.533 | 1.112 | -0.091 | 0.272 | 0.239 |
| 2002 | -1.605 | -0.885 | -1.441 | -0.963 | -1.056 |
| 2003 | -0.376 | -1.072 | 0.498 | -0.540 | -0.391 |
| 2004 | 1.678 | 0.112 | 0.555 | -0.311 | -0.370 |
| 2005 | 0.266 | -0.234 | -0.588 | -0.211 | -0.152 |
| 2006 | 2.198 | -0.301 | -0.068 | -0.151 | -0.073 |
| 2007 | -0.538 | -0.775 | -0.168 | -0.154 | -0.218 |
| 2008 | -9.084 | -1.863 | -2.025 | -0.197 | 0.150 |
| 2009 | -8.518 | -3.004 | -4.564 | -0.420 | 0.252 |
| 2010 | 0.520 | -0.221 | -0.593 | -0.276 | -0.416 |
| | ARMAXE/ SRCOr | ARMAXE/ SRCOu | ARMAXE/ SRCS | ARMAXE/ SRE | ARMAXE/ SRGDP |
| 2001 | -0.267 | 0.493 | 0.347 | 0.748 | 0.277 |
| 2002 | -1.912 | -1.036 | -0.895 | -0.772 | -1.251 |
| 2003 | -2.267 | -0.137 | -0.467 | -0.210 | -0.278 |
| 2004 | 1.456 | -0.765 | -0.269 | -0.167 | 0.022 |
| 2005 | 0.609 | -0.140 | -0.206 | 0.038 | -0.484 |
| 2006 | 4.090 | -1.212 | -0.146 | -0.001 | 0.064 |
| 2007 | 0.081 | -1.300 | -0.148 | -0.356 | -0.033 |
| 2008 | -6.248 | -0.250 | -0.360 | -0.095 | -2.213 |
| 2009 | -7.070 | 2.785 | -0.348 | -1.490 | -6.273 |
| 2010 | 0.528 | -0.165 | -0.170 | -1.203 | -1.147 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|----------------|-------------------|-------------------|--------------------|
| | ARMAXE/ MR | ARMAXE/ VAR | ARMAXGDP/ SRBR | ARMAXGDP/ SRCC | ARMAXGDP/ SRCOr |
| 2001 | 0.435 | 1.014 | -0.481 | -0.514 | -1.195 |
| 2002 | -1.776 | -1.056 | -0.599 | -0.692 | -2.021 |
| 2003 | -0.488 | -1.184 | 0.969 | 1.118 | -3.523 |
| 2004 | 1.566 | 0.000 | 0.885 | 0.826 | 3.553 |
| 2005 | 0.267 | -0.234 | -0.406 | -0.347 | 1.610 |
| 2006 | 2.180 | -0.319 | 0.075 | 0.152 | 8.473 |
| 2007 | -0.616 | -0.853 | -0.001 | -0.065 | 0.484 |
| 2008 | -8.781 | -1.561 | -1.999 | -1.652 | -12.273 |
| 2009 | -8.624 | -3.109 | -4.433 | -3.761 | -13.590 |
| 2010 | 0.268 | -0.473 | -0.399 | -0.539 | 1.525 |

| | ARMAXGDP/ SRCOu | ARMAXGDP /SRCS | ARMAXGDP/ SRE | ARMAXGDP/ SRGDP | ARMAXGDP /MR |
|------|--------------------|-------------------|------------------|--------------------|-----------------|
| 2001 | -0.260 | -0.406 | -0.005 | -0.476 | -0.318 |
| 2002 | -0.673 | -0.532 | -0.408 | -0.888 | -1.412 |
| 2003 | 1.372 | 1.042 | 1.299 | 1.231 | 1.021 |
| 2004 | 0.430 | 0.927 | 1.028 | 1.218 | 2.761 |
| 2005 | -0.335 | -0.402 | -0.157 | -0.679 | 0.071 |
| 2006 | -0.987 | 0.080 | 0.224 | 0.289 | 2.405 |
| 2007 | -1.147 | 0.006 | -0.203 | 0.120 | -0.463 |
| 2008 | -2.052 | -2.162 | -1.897 | -4.015 | -10.583 |
| 2009 | -1.229 | -4.361 | -5.503 | -10.287 | -12.637 |
| 2010 | -0.288 | -0.294 | -1.326 | -1.271 | 0.144 |

| | ARMAXGDP/ VAR | SRBR/ SRCC | SRBR/ SRCOr | SRBR/ SRCOu | SRBR/ SRCS |
|------|------------------|---------------|----------------|----------------|---------------|
| 2001 | 0.261 | -0.150 | -0.656 | 0.103 | -0.042 |
| 2002 | -0.692 | -0.214 | -1.071 | -0.195 | -0.054 |
| 2003 | 0.325 | 0.080 | -1.795 | 0.334 | 0.004 |
| 2004 | 1.195 | -0.039 | 1.786 | -0.435 | 0.062 |
| 2005 | -0.429 | 0.029 | 0.791 | 0.041 | -0.025 |
| 2006 | -0.093 | 0.069 | 4.233 | -1.070 | -0.003 |
| 2007 | -0.700 | -0.051 | 0.248 | -1.133 | 0.019 |
| 2008 | -3.363 | 0.176 | -6.222 | -0.224 | -0.334 |
| 2009 | -7.123 | 0.383 | -6.940 | 2.915 | -0.217 |
| 2010 | -0.597 | -0.222 | 0.721 | 0.029 | 0.023 |

| | SRBR/ SRE | SRBR/ SRGDP | SRBR/ MR | SRBR/ VAR | SRCC/ SRCOr |
|------|--------------|----------------|-------------|--------------|----------------|
| 2001 | 0.359 | -0.113 | 0.045 | 0.624 | -0.689 |
| 2002 | 0.069 | -0.410 | -0.935 | -0.214 | -1.164 |
| 2003 | 0.262 | 0.193 | -0.017 | -0.713 | -1.647 |
| 2004 | 0.163 | 0.353 | 1.896 | 0.330 | 1.727 |
| 2005 | 0.219 | -0.303 | 0.448 | -0.053 | 0.849 |
| 2006 | 0.141 | 0.206 | 2.322 | -0.176 | 4.310 |
| 2007 | -0.189 | 0.134 | -0.449 | -0.686 | 0.184 |
| 2008 | -0.069 | -2.187 | -8.755 | -1.535 | -5.875 |
| 2009 | -1.360 | -6.143 | -8.494 | -2.979 | -6.268 |
| 2010 | -1.009 | -0.954 | 0.461 | -0.280 | 0.581 |

| Year | SA Combination Forecasting | | | | |
|------|----------------------------|-----------------|----------------|----------------|----------------|
| | SRCC/ SRCOu | SRC/ SRCS | SRCC/ SRE | SRCC/ SRGDP | SRCC /MR |
| 2001 | 0.070 | -0.076 | 0.325 | -0.146 | 0.012 |
| 2002 | -0.288 | -0.147 | -0.024 | -0.503 | -1.028 |
| 2003 | 0.482 | 0.152 | 0.410 | 0.341 | 0.131 |
| 2004 | -0.494 | 0.003 | 0.104 | 0.293 | 1.837 |
| 2005 | 0.100 | 0.034 | 0.278 | -0.244 | 0.507 |
| 2006 | -0.992 | 0.074 | 0.219 | 0.284 | 2.400 |
| 2007 | -1.197 | -0.045 | -0.253 | 0.069 | -0.514 |
| 2008 | 0.123 | 0.014 | 0.278 | -1.840 | -8.408 |
| 2009 | 3.587 | 0.455 | -0.688 | -5.471 | -7.821 |
| 2010 | -0.111 | -0.117 | -1.150 | -1.094 | 0.321 |
| | SRCC/ VAR | SRCOr/ SRCOu | SRCOr/ SRCS | SRCC/ SRGDP | SRCC /MR |
| 2001 | 0.591 | -0.436 | -0.581 | -0.146 | 0.012 |
| 2002 | -0.307 | -1.145 | -1.004 | -0.503 | -1.028 |
| 2003 | -0.564 | -1.393 | -1.723 | 0.341 | 0.131 |
| 2004 | 0.271 | 1.332 | 1.828 | 0.293 | 1.837 |
| 2005 | 0.006 | 0.861 | 0.795 | -0.244 | 0.507 |
| 2006 | -0.099 | 3.171 | 4.238 | 0.284 | 2.400 |
| 2007 | -0.750 | -0.898 | 0.255 | 0.069 | -0.514 |
| 2008 | -1.188 | -6.276 | -6.385 | -1.840 | -8.408 |
| 2009 | -2.307 | -3.736 | -6.868 | -5.471 | -7.821 |
| 2010 | -0.420 | 0.832 | 0.826 | -1.094 | 0.321 |
| | SRCOr/ SRE | SRCOr/ SRGDP | SRCOr/ MR | SRCOr/ VAR | SRCOu/ SRCS |
| 2001 | -0.180 | -0.652 | -0.494 | 0.085 | 0.178 |
| 2002 | -0.880 | -1.360 | -1.884 | -1.164 | -0.128 |
| 2003 | -1.466 | -1.534 | -1.744 | -2.440 | 0.406 |
| 2004 | 1.930 | 2.119 | 3.663 | 2.097 | -0.393 |
| 2005 | 1.039 | 0.517 | 1.268 | 0.767 | 0.046 |
| 2006 | 4.382 | 4.447 | 6.563 | 4.065 | -1.065 |
| 2007 | 0.046 | 0.369 | -0.214 | -0.451 | -1.127 |
| 2008 | -6.120 | -8.238 | -14.807 | -7.586 | -0.387 |
| 2009 | -8.010 | -12.793 | -15.144 | -9.629 | 2.987 |
| 2010 | -0.206 | -0.150 | 1.264 | 0.524 | 0.134 |
| | SRCS/ SRE | SRCS/ SRGDP | SRCS/ MR | SRCS/ VAR | SRE/ SRGDP |
| 2001 | 0.433 | -0.038 | 1.425 | 0.699 | 0.363 |
| 2002 | 0.137 | -0.343 | -0.631 | -0.147 | -0.219 |
| 2003 | 0.334 | 0.265 | 0.361 | -0.640 | 0.523 |
| 2004 | 0.205 | 0.395 | -1.871 | 0.372 | 0.496 |
| 2005 | 0.224 | -0.298 | -3.005 | -0.048 | -0.054 |
| 2006 | 0.146 | 0.211 | -4.235 | -0.171 | 0.356 |
| 2007 | -0.183 | 0.140 | -0.443 | -0.680 | -0.069 |
| 2008 | -0.232 | -2.350 | -8.918 | -1.698 | -2.085 |
| 2009 | -1.288 | -6.071 | -8.421 | -2.907 | -7.213 |
| 2010 | -0.904 | -0.848 | 0.566 | -0.174 | -1.881 |
| | SRE/ MR | SRE/ VAR | SRGDP/ MR | SRGDP/ VAR | MR/ VAR |
| 2001 | 0.521 | 1.100 | 0.049 | 0.629 | 0.786 |
| 2002 | -0.744 | -0.023 | -1.223 | -0.503 | -1.027 |
| 2003 | 0.313 | -0.383 | 0.244 | -0.452 | -0.661 |
| 2004 | 2.040 | 0.474 | 2.229 | 0.663 | 2.207 |
| 2005 | 0.697 | 0.196 | 0.175 | -0.326 | 0.425 |
| 2006 | 2.472 | -0.027 | 2.537 | 0.038 | 2.154 |
| 2007 | -0.651 | -0.888 | -0.329 | -0.565 | -1.148 |
| 2008 | -8.653 | -1.433 | -10.771 | -3.551 | -10.119 |
| 2009 | -9.564 | -4.049 | -14.347 | -8.832 | -11.183 |
| 2010 | -0.466 | -1.207 | -0.410 | -1.151 | 0.264 |

B.4 OLS Combination Forecasting

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|------------------|-----------------|-----------------|-----------------|
| | SES/ HES | SES/ BES | SES/ ARMA | SES/ ARMAXBR | SES/ ARMAXCC |
| 2001 | -1.580 | -1.416 | 1.130 | 0.411 | 1.445 |
| 2002 | -1.699 | -1.416 | -1.909 | -2.072 | -1.369 |
| 2003 | -1.699 | -1.416 | -1.111 | -1.161 | -1.559 |
| 2004 | -1.699 | -2.706 | -0.657 | -0.575 | -0.507 |
| 2005 | -1.699 | -2.706 | -0.399 | -0.384 | -0.601 |
| 2006 | -1.818 | -2.706 | -0.251 | -0.211 | -0.570 |
| 2007 | -1.818 | -2.706 | -0.169 | -0.102 | -0.008 |
| 2008 | -1.818 | -3.995 | -0.120 | -0.309 | -1.144 |
| 2009 | -1.818 | -3.995 | -0.093 | -0.446 | -2.098 |
| 2010 | -1.936 | -3.995 | -0.079 | -0.149 | 0.531 |
| | SES/ ARMAXCOr | SES/ ARMAXCOu | SES/ ARMAXCS | SES/ ARMAXE | SES/ ARMAGDP |
| 2001 | -2.731 | 1.076 | 1.153 | 1.019 | -0.760 |
| 2002 | -2.801 | -2.020 | -1.695 | -1.966 | -1.026 |
| 2003 | -3.154 | -1.163 | -0.866 | -1.006 | 2.500 |
| 2004 | 1.769 | -0.661 | -0.411 | -0.558 | 2.206 |
| 2005 | 0.655 | -0.397 | -0.383 | -0.257 | -0.690 |
| 2006 | 5.206 | -0.221 | -0.216 | -0.137 | 0.386 |
| 2007 | 0.032 | -0.134 | -0.102 | -0.171 | 0.189 |
| 2008 | -8.267 | -0.105 | -0.916 | -0.052 | -4.170 |
| 2009 | -9.117 | -0.142 | -0.317 | -0.448 | -9.601 |
| 2010 | 0.744 | -0.067 | 0.143 | -0.350 | -0.613 |
| | SES/ SRBR | SES/ SRCC | SES/ SRCOr | SES/ SRCOu | SES/ SRCS |
| 2001 | 0.794 | 1.550 | -0.407 | 0.782 | 0.946 |
| 2002 | 0.773 | 1.966 | -1.199 | 1.259 | 0.949 |
| 2003 | 1.028 | 0.169 | -2.640 | 0.450 | 0.937 |
| 2004 | 1.450 | 1.266 | 4.149 | 1.759 | 0.931 |
| 2005 | 1.214 | 0.639 | 2.285 | 0.952 | 0.956 |
| 2006 | 1.315 | 0.443 | 8.871 | 2.760 | 0.952 |
| 2007 | 1.417 | 1.322 | 1.204 | 2.879 | 0.947 |
| 2008 | 0.535 | -0.822 | -11.036 | 1.266 | 1.052 |
| 2009 | -0.032 | -2.604 | -12.300 | -3.886 | 0.981 |
| 2010 | 0.961 | 2.152 | 2.203 | 0.930 | 0.926 |
| | SES/ SRE | SES/ SRGDP | SES/ MR | SES/ VAR | HES/ BES |
| 2001 | 2.797 | 0.652 | 0.294 | 1.878 | 0.312 |
| 2002 | 1.858 | 0.089 | -1.643 | 0.257 | 0.339 |
| 2003 | 2.400 | 1.188 | 0.122 | -0.760 | 0.339 |
| 2004 | 1.933 | 1.409 | 3.827 | 1.176 | -0.278 |
| 2005 | 2.198 | 0.206 | 1.005 | 0.481 | -0.278 |
| 2006 | 1.908 | 1.157 | 4.699 | 0.221 | -0.252 |
| 2007 | 0.793 | 0.998 | -0.815 | -0.787 | -0.252 |
| 2008 | 1.486 | -3.253 | -17.094 | -2.253 | -0.869 |
| 2009 | -2.541 | -10.688 | -16.457 | -4.936 | -0.869 |
| 2010 | -1.734 | -0.986 | 1.084 | 0.093 | -0.843 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|-----------------|------------------|------------------------------|------------------------------|
| | HES/ ARMA | HES/ ARMAXBR | HES/ ARMAXCC | HES/ ARMAXCO _r | HES/ ARMAXCO _u |
| 2001 | 1.089 | 0.373 | 1.405 | -2.822 | 1.034 |
| 2002 | -1.959 | -2.116 | -1.418 | -2.894 | -2.069 |
| 2003 | -1.158 | -1.203 | -1.607 | -3.248 | -1.210 |
| 2004 | -0.703 | -0.615 | -0.553 | 1.689 | -0.707 |
| 2005 | -0.444 | -0.424 | -0.647 | 0.572 | -0.443 |
| 2006 | -0.298 | -0.251 | -0.616 | 5.135 | -0.267 |
| 2007 | -0.215 | -0.142 | -0.053 | -0.055 | -0.180 |
| 2008 | -0.166 | -0.349 | -1.192 | -8.380 | -0.151 |
| 2009 | -0.139 | -0.487 | -2.149 | -9.232 | -0.188 |
| 2010 | -0.125 | -0.190 | 0.486 | 0.657 | -0.114 |
| | HES/ ARMAXCS | HES/ ARMAXE | HES/ ARMAXGDP | HES/ SRBR | HES/ SRCC |
| | | | | | |
| 2001 | 1.101 | 0.981 | -0.752 | 0.909 | 1.498 |
| 2002 | -1.755 | -2.011 | -1.017 | 0.898 | 1.828 |
| 2003 | -0.924 | -1.049 | 2.517 | 1.132 | 0.431 |
| 2004 | -0.468 | -0.600 | 2.222 | 1.520 | 1.284 |
| 2005 | -0.439 | -0.298 | -0.680 | 1.303 | 0.796 |
| 2006 | -0.273 | -0.178 | 0.400 | 1.404 | 0.651 |
| 2007 | -0.159 | -0.212 | 0.203 | 1.497 | 1.335 |
| 2008 | -0.976 | -0.093 | -4.167 | 0.688 | -0.332 |
| 2009 | -0.374 | -0.490 | -9.610 | 0.168 | -1.717 |
| 2010 | 0.086 | -0.393 | -0.600 | 1.087 | 1.987 |
| | HES/ SRCOr | HES/ SRCOu | HES/ SRCS | HES/ SRE | HES/ SRGDP |
| | | | | | |
| 2001 | -0.370 | 0.868 | 1.025 | 2.792 | 0.699 |
| 2002 | -1.160 | 1.314 | 1.034 | 1.919 | 0.140 |
| 2003 | -2.605 | 0.569 | 1.027 | 2.428 | 1.242 |
| 2004 | 4.204 | 1.775 | 1.024 | 1.990 | 1.463 |
| 2005 | 2.335 | 1.032 | 1.038 | 2.239 | 0.257 |
| 2006 | 8.944 | 2.703 | 1.043 | 1.976 | 1.216 |
| 2007 | 1.255 | 2.813 | 1.040 | 0.927 | 1.056 |
| 2008 | -11.020 | 1.329 | 1.101 | 1.579 | -3.206 |
| 2009 | -12.287 | -3.414 | 1.060 | -2.209 | -10.660 |
| 2010 | 2.263 | 1.027 | 1.035 | -1.440 | -0.927 |
| | HES/ MR | HES/ VAR | BES/ ARMA | BES/ ARMAXBR | BES/ ARMAXCC |
| | | | | | |
| 2001 | 0.259 | 1.944 | 1.098 | 0.392 | 1.414 |
| 2002 | -1.687 | 0.323 | -1.939 | -2.088 | -1.400 |
| 2003 | 0.087 | -0.698 | -1.141 | -1.178 | -1.589 |
| 2004 | 3.809 | 1.244 | -0.704 | -0.605 | -0.553 |
| 2005 | 0.974 | 0.547 | -0.446 | -0.414 | -0.647 |
| 2006 | 4.685 | 0.291 | -0.299 | -0.241 | -0.616 |
| 2007 | -0.854 | -0.721 | -0.216 | -0.132 | -0.054 |
| 2008 | -17.207 | -2.192 | -0.185 | -0.351 | -1.205 |
| 2009 | -16.568 | -4.884 | -0.158 | -0.488 | -2.159 |
| 2010 | 1.054 | 0.167 | -0.143 | -0.192 | 0.469 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|-------------------|-------------------|------------------|------------------|
| | BES/ ARMAXCOr | BES/ ARMAXCOu | BES/ ARMAXCS | BES/ ARMAXE | BES/ ARMAXGDP |
| 2001 | -2.931 | 1.047 | 1.089 | 0.997 | -0.688 |
| 2002 | -3.002 | -2.022 | -1.757 | -1.985 | -0.955 |
| 2003 | -3.356 | -1.173 | -0.929 | -1.026 | 2.579 |
| 2004 | 1.507 | -0.677 | -0.507 | -0.593 | 2.337 |
| 2005 | 0.389 | -0.416 | -0.479 | -0.292 | -0.566 |
| 2006 | 4.958 | -0.242 | -0.312 | -0.172 | 0.512 |
| 2007 | -0.236 | -0.156 | -0.198 | -0.206 | 0.315 |
| 2008 | -8.649 | -0.129 | -1.045 | -0.101 | -4.003 |
| 2009 | -9.502 | -0.165 | -0.446 | -0.497 | -9.447 |
| 2010 | 0.400 | -0.091 | 0.014 | -0.399 | -0.437 |
| | BES/ SRBR | BES/ SRCC | BES/ SRCOr | BES/ SRCOu | BES/ SRCS |
| 2001 | 1.199 | 1.691 | -0.268 | 1.115 | 1.252 |
| 2002 | 1.178 | 1.983 | -1.063 | 1.535 | 1.254 |
| 2003 | 1.416 | 0.722 | -2.508 | 0.822 | 1.247 |
| 2004 | 2.077 | 1.723 | 4.455 | 2.222 | 1.460 |
| 2005 | 1.857 | 1.283 | 2.585 | 1.510 | 1.475 |
| 2006 | 1.951 | 1.145 | 9.192 | 3.104 | 1.472 |
| 2007 | 2.045 | 1.762 | 1.500 | 3.209 | 1.469 |
| 2008 | 1.492 | 0.489 | -10.628 | 2.032 | 1.746 |
| 2009 | 0.964 | -0.762 | -11.896 | -2.513 | 1.706 |
| 2010 | 1.888 | 2.575 | 2.655 | 1.736 | 1.675 |
| | BES/ SRE | BES/ SRGDP | BES/ MR | BES/ VAR | ARMA/ ARMAXBR |
| 2001 | 3.066 | 0.812 | 0.166 | 2.080 | 0.394 |
| 2002 | 2.201 | 0.249 | -1.795 | 0.450 | -2.019 |
| 2003 | 2.700 | 1.348 | -0.008 | -0.572 | -1.104 |
| 2004 | 2.570 | 1.729 | 3.735 | 1.520 | -0.509 |
| 2005 | 2.814 | 0.526 | 0.878 | 0.822 | -0.325 |
| 2006 | 2.547 | 1.477 | 4.617 | 0.560 | -0.151 |
| 2007 | 1.519 | 1.318 | -0.964 | -0.453 | -0.040 |
| 2008 | 2.458 | -2.772 | -17.449 | -1.781 | -0.271 |
| 2009 | -1.254 | -10.203 | -16.805 | -4.479 | -0.423 |
| 2010 | -0.510 | -0.505 | 0.950 | 0.578 | -0.101 |
| | ARMA/ ARMAXCC | ARMA/ ARMAXCOr | ARMA/ ARMAXCOu | ARMA/ ARMAXCS | ARMA/ ARMAXE |
| 2001 | 1.645 | -1.967 | 0.749 | 1.171 | 1.203 |
| 2002 | -1.036 | -2.431 | -2.675 | -1.652 | -1.818 |
| 2003 | -1.709 | -2.628 | -1.411 | -0.835 | -1.043 |
| 2004 | -0.373 | 1.662 | -0.573 | -0.386 | -0.592 |
| 2005 | -0.639 | 0.739 | -0.275 | -0.345 | -0.341 |
| 2006 | -0.665 | 4.669 | 0.105 | -0.181 | -0.192 |
| 2007 | 0.128 | 0.235 | 0.218 | -0.070 | -0.097 |
| 2008 | -1.580 | -6.890 | 0.105 | -0.824 | -0.056 |
| 2009 | -3.010 | -7.617 | -0.394 | -0.265 | 0.015 |
| 2010 | 0.882 | 0.858 | 0.116 | 0.163 | 0.021 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|----------------------|----------------------|---------------------|--------------------|
| | ARMA/ ARMAXGDP | ARMA/ SRBR | ARMA/ SRCC | ARMA/ SRCOr | ARMA/ SRCOu |
| 2001 | -0.909 | 0.995 | 0.823 | 0.194 | 0.944 |
| 2002 | -1.326 | -2.050 | -2.514 | -2.837 | -1.744 |
| 2003 | 2.152 | -1.120 | -0.372 | -3.158 | -1.515 |
| 2004 | 1.889 | -0.447 | -0.743 | 1.815 | -0.150 |
| 2005 | -0.920 | -0.313 | -0.016 | 0.764 | -0.457 |
| 2006 | 0.136 | -0.113 | 0.278 | 5.346 | 0.950 |
| 2007 | -0.051 | 0.022 | -0.299 | 0.220 | 1.116 |
| 2008 | -4.297 | -0.387 | 1.356 | -8.034 | 0.040 |
| 2009 | -9.589 | -0.655 | 2.717 | -8.868 | -3.528 |
| 2010 | -0.829 | -0.125 | -0.831 | 0.970 | -0.154 |
| | ARMA/ SRCS | ARMA/ SRE | ARMA/ SRGDP | ARMA/ MR | ARMA/ VAR |
| | | | | | |
| 2001 | 1.114 | 1.853 | 0.934 | 0.952 | 1.499 |
| 2002 | -1.897 | -1.578 | -2.063 | -2.493 | -1.383 |
| 2003 | -1.177 | -0.537 | -0.576 | -0.698 | -1.438 |
| 2004 | -0.757 | -0.312 | -0.028 | 2.233 | -0.054 |
| 2005 | -0.347 | 0.067 | -0.693 | 0.412 | -0.278 |
| 2006 | -0.227 | 0.074 | 0.131 | 3.126 | -0.329 |
| 2007 | -0.174 | -0.373 | 0.084 | -0.719 | -0.843 |
| 2008 | 0.516 | 0.003 | -2.998 | -12.204 | -1.637 |
| 2009 | 0.111 | -1.880 | -8.439 | -11.736 | -3.131 |
| 2010 | -0.210 | -1.483 | -1.297 | 0.686 | -0.289 |
| | ARMAXBR/ ARMAXCC | ARMAXBR/ ARMAXCOr | ARMAXBR/ ARMAXCOu | ARMAXBR/ ARMAXCS | ARMAXBR/ ARMAXE |
| | | | | | |
| 2001 | 0.866 | -2.055 | 0.466 | 0.913 | -0.597 |
| 2002 | -1.738 | -2.451 | -2.004 | -1.750 | -2.171 |
| 2003 | -1.253 | -2.630 | -1.098 | -0.891 | -1.361 |
| 2004 | -0.489 | 1.663 | -0.516 | -0.382 | -0.549 |
| 2005 | -0.408 | 0.735 | -0.326 | -0.282 | -0.550 |
| 2006 | -0.290 | 4.655 | -0.154 | -0.113 | -0.290 |
| 2007 | -0.007 | 0.241 | -0.045 | -0.003 | 0.063 |
| 2008 | -0.571 | -6.891 | -0.251 | -0.541 | -0.700 |
| 2009 | -1.023 | -7.637 | -0.387 | -0.273 | -0.391 |
| 2010 | 0.171 | 0.844 | -0.093 | 0.111 | 0.241 |
| | ARMAXBR/ ARMAXGDP | ARMAXBR/ SRBR | ARMAXBR/ SRCC | ARMAXBR/ SRCOr | ARMAXBR/ SRCOu |
| | | | | | |
| 2001 | -0.914 | 0.334 | 0.081 | -0.399 | 0.214 |
| 2002 | -1.362 | -2.146 | -2.717 | -2.973 | -1.922 |
| 2003 | 2.075 | -1.153 | -0.414 | -3.196 | -1.586 |
| 2004 | 1.841 | -0.427 | -0.682 | 1.862 | -0.079 |
| 2005 | -0.910 | -0.316 | -0.004 | 0.763 | -0.457 |
| 2006 | 0.131 | -0.110 | 0.321 | 5.344 | 0.990 |
| 2007 | -0.048 | 0.033 | -0.253 | 0.266 | 1.183 |
| 2008 | -4.227 | -0.470 | 1.204 | -8.156 | -0.161 |
| 2009 | -9.422 | -0.798 | 2.450 | -9.120 | -3.934 |
| 2010 | -0.818 | -0.168 | -0.944 | 0.900 | -0.240 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|----------------------------------|---------------------|--------------------|----------------------------------|
| | ARMAXBR/ SRCS | ARMAXBR/ SRE | ARMAXBR/ SRGDP | ARMAXBR/ MR | ARMAXBR/ VAR |
| 2001 | 0.393 | 1.093 | 0.312 | 0.454 | 1.021 |
| 2002 | -2.066 | -1.765 | -2.203 | -2.601 | -1.488 |
| 2003 | -1.224 | -0.629 | -0.635 | -0.739 | -1.464 |
| 2004 | -0.668 | -0.261 | 0.023 | 2.266 | -0.008 |
| 2005 | -0.344 | 0.045 | -0.685 | 0.412 | -0.270 |
| 2006 | -0.195 | 0.086 | 0.149 | 3.127 | -0.303 |
| 2007 | -0.112 | -0.305 | 0.127 | -0.675 | -0.793 |
| 2008 | 0.244 | -0.199 | -3.123 | -12.262 | -1.743 |
| 2009 | -0.272 | -2.130 | -8.615 | -11.909 | -3.324 |
| 2010 | -0.270 | -1.479 | -1.348 | 0.627 | -0.334 |
| | ARMAXCC/ ARMAXCo | ARMAXCC/ ARMAXCo _u | ARMAXCC/ ARMAXCS | ARMAXCC/ ARMAXE | ARMAXCC/ ARMAXGDP |
| | | | | | |
| 2001 | -1.749 | 1.513 | 1.370 | 1.550 | -0.883 |
| 2002 | -2.326 | -1.196 | -1.449 | -1.220 | -1.299 |
| 2003 | -2.649 | -1.704 | -1.040 | -1.558 | 2.115 |
| 2004 | 1.569 | -0.492 | -0.344 | -0.436 | 1.889 |
| 2005 | 0.641 | -0.695 | -0.366 | -0.581 | -0.930 |
| 2006 | 4.367 | -0.707 | -0.255 | -0.561 | 0.117 |
| 2007 | 0.242 | -0.004 | 0.041 | 0.074 | -0.043 |
| 2008 | -6.753 | -1.488 | -0.900 | -1.216 | -4.341 |
| 2009 | -7.624 | -2.717 | -0.939 | -2.237 | -9.670 |
| 2010 | 0.923 | 0.675 | 0.405 | 0.702 | -0.792 |
| | ARMAXCC/ SRBR | ARMAXCC/ SRCC | ARMAXCC/ SRCOr | ARMAXCC/ SRCOu | ARMAXCC/ SRCS |
| | | | | | |
| 2001 | 1.316 | 1.010 | 0.448 | 1.256 | 1.426 |
| 2002 | -1.503 | -2.219 | -2.407 | -1.218 | -1.364 |
| 2003 | -1.569 | -0.610 | -3.541 | -1.958 | -1.626 |
| 2004 | -0.317 | -0.657 | 1.934 | -0.020 | -0.608 |
| 2005 | -0.524 | -0.123 | 0.591 | -0.663 | -0.557 |
| 2006 | -0.444 | 0.105 | 5.087 | 0.600 | -0.551 |
| 2007 | 0.166 | -0.214 | 0.346 | 1.239 | -0.018 |
| 2008 | -1.392 | 0.796 | -8.899 | -0.988 | -0.543 |
| 2009 | -2.618 | 1.624 | -10.543 | -5.449 | -1.907 |
| 2010 | 0.484 | -0.506 | 1.467 | 0.447 | 0.400 |
| | ARMAXCC/ SRE | ARMAXCC/ SRGDP | ARMAXCC/ MR | ARMAXCC/ VAR | ARMAXCo/ ARMAXCo _u |
| | | | | | |
| 2001 | 2.122 | 1.198 | 1.168 | 1.695 | -1.959 |
| 2002 | -1.067 | -1.613 | -2.137 | -1.045 | -2.443 |
| 2003 | -1.007 | -0.967 | -1.017 | -1.736 | -2.627 |
| 2004 | -0.186 | 0.091 | 2.329 | 0.030 | 1.653 |
| 2005 | -0.158 | -0.873 | 0.266 | -0.419 | 0.736 |
| 2006 | -0.258 | -0.148 | 2.904 | -0.543 | 4.654 |
| 2007 | -0.211 | 0.214 | -0.615 | -0.740 | 0.240 |
| 2008 | -1.013 | -3.876 | -12.924 | -2.299 | -6.857 |
| 2009 | -3.771 | -10.151 | -13.129 | -4.420 | -7.589 |
| 2010 | -0.824 | -0.784 | 1.099 | 0.102 | 0.858 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|---------------------|-----------------------|---------------------|-----------------------|
| | ARMAXCor/ ARMAXCS | ARMAXCor/ ARMAXE | ARMAXCor/ ARMAXGDP | ARMAXCor/ SRBR | ARMAXCor/ SRCC |
| 2001 | -1.998 | -1.971 | -1.447 | -2.725 | -2.515 |
| 2002 | -2.396 | -2.441 | -1.672 | -2.811 | -2.689 |
| 2003 | -2.604 | -2.611 | 0.943 | -2.952 | -2.569 |
| 2004 | 1.726 | 1.666 | 2.114 | 2.243 | 1.918 |
| 2005 | 0.762 | 0.753 | -0.433 | 0.953 | 1.000 |
| 2006 | 4.736 | 4.667 | 1.688 | 5.521 | 5.459 |
| 2007 | 0.254 | 0.232 | 0.068 | 0.504 | 0.221 |
| 2008 | -7.052 | -6.859 | -5.646 | -8.392 | -7.267 |
| 2009 | -7.720 | -7.640 | -10.070 | -9.690 | -7.632 |
| 2010 | 0.902 | 0.817 | -0.348 | 0.836 | 0.697 |
| Year | ARMAXCor/ SRCor | ARMAXCor/ SRCou | ARMAXCor/ SRCs | ARMAXCor/ SRCE | ARMAXCor/ SRGDP |
| | | | | | |
| 2001 | -2.419 | -2.518 | -2.487 | -1.656 | -2.040 |
| 2002 | -2.742 | -2.391 | -2.530 | -2.196 | -2.418 |
| 2003 | -3.517 | -3.061 | -2.958 | -2.263 | -2.085 |
| 2004 | 2.861 | 2.214 | 1.806 | 2.234 | 2.099 |
| 2005 | 1.308 | 0.812 | 0.885 | 1.296 | 0.498 |
| 2006 | 7.308 | 5.932 | 5.294 | 5.524 | 4.789 |
| 2007 | 0.428 | 0.997 | 0.216 | -0.009 | 0.434 |
| 2008 | -10.590 | -7.653 | -7.184 | -7.637 | -8.821 |
| 2009 | -11.722 | -10.569 | -8.479 | -10.480 | -13.740 |
| 2010 | 1.356 | 0.890 | 0.775 | -0.596 | -0.105 |
| Year | ARMAXCor/ MR | ARMAXCor/ VAR | ARMAXCOu/ ARMAXCS | ARMAXCOu/ ARMAXE | ARMAXCOu/ ARMAXGDP |
| | | | | | |
| 2001 | -1.464 | -1.124 | 1.247 | 1.172 | -0.905 |
| 2002 | -2.559 | -1.962 | -1.619 | -1.925 | -1.333 |
| 2003 | -1.832 | -2.707 | -0.794 | -1.113 | 2.143 |
| 2004 | 3.373 | 1.715 | -0.334 | -0.598 | 1.884 |
| 2005 | 1.121 | 0.590 | -0.259 | -0.350 | -0.918 |
| 2006 | 6.079 | 3.681 | -0.092 | -0.158 | 0.138 |
| 2007 | -0.269 | -0.468 | 0.015 | -0.031 | -0.049 |
| 2008 | -14.476 | -7.049 | -0.620 | -0.032 | -4.286 |
| 2009 | -14.684 | -8.956 | -0.155 | 0.054 | -9.570 |
| 2010 | 1.222 | 0.464 | 0.222 | 0.119 | -0.825 |
| Year | ARMAXCOu/ SRBR | ARMAXCOu/ SRCC | ARMAXCOu/ SRCor | ARMAXCOu/ SRCou | ARMAXCOu/ SRCs |
| | | | | | |
| 2001 | 0.947 | 0.806 | 0.160 | 0.897 | 1.072 |
| 2002 | -2.152 | -2.559 | -2.915 | -1.837 | -1.990 |
| 2003 | -1.160 | -0.454 | -3.189 | -1.563 | -1.213 |
| 2004 | -0.432 | -0.721 | 1.826 | -0.130 | -0.746 |
| 2005 | -0.296 | -0.021 | 0.778 | -0.444 | -0.331 |
| 2006 | -0.066 | 0.290 | 5.387 | 1.021 | -0.183 |
| 2007 | 0.074 | -0.237 | 0.260 | 1.192 | -0.126 |
| 2008 | -0.370 | 1.287 | -8.016 | 0.070 | 0.544 |
| 2009 | -0.712 | 2.492 | -8.902 | -3.644 | 0.076 |
| 2010 | -0.104 | -0.749 | 0.992 | -0.132 | -0.185 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|--------------------|-------------------|-------------------|--------------------|
| | ARMAXCOu/ SRCE | ARMAXCOu/ SRGDP | ARMAXCOu/ MR | ARMAXCOu/ VAR | ARMAXCS/ ARMAXE |
| 2001 | 1.827 | 0.898 | 0.923 | 1.474 | 1.278 |
| 2002 | -1.666 | -2.142 | -2.554 | -1.443 | -1.517 |
| 2003 | -0.562 | -0.608 | -0.722 | -1.460 | -0.709 |
| 2004 | -0.296 | -0.020 | 2.238 | -0.046 | -0.260 |
| 2005 | 0.091 | -0.679 | 0.423 | -0.266 | -0.248 |
| 2006 | 0.123 | 0.168 | 3.153 | -0.298 | -0.081 |
| 2007 | -0.332 | 0.125 | -0.685 | -0.809 | 0.039 |
| 2008 | 0.033 | -2.971 | -12.171 | -1.615 | -0.814 |
| 2009 | -1.955 | -8.459 | -11.746 | -3.149 | -0.168 |
| 2010 | -1.491 | -1.274 | 0.703 | -0.271 | 0.304 |
| | ARMAXCS/ ARMAXGDP | ARMAXCS/ SRBR | ARMAXCS/ SRCC | ARMAXCS/ SRCOr | ARMAXCS/ SRCOu |
| 2001 | -0.754 | 1.080 | 0.972 | 0.260 | 1.016 |
| 2002 | -1.355 | -1.752 | -2.088 | -2.604 | -1.455 |
| 2003 | 1.990 | -0.803 | -0.190 | -2.899 | -1.217 |
| 2004 | 1.777 | -0.141 | -0.400 | 2.056 | 0.172 |
| 2005 | -0.882 | -0.231 | 0.004 | 0.821 | -0.379 |
| 2006 | 0.128 | -0.015 | 0.287 | 5.403 | 1.084 |
| 2007 | -0.039 | 0.148 | -0.129 | 0.321 | 1.282 |
| 2008 | -4.147 | -1.099 | 0.355 | -8.608 | -0.680 |
| 2009 | -9.064 | -0.789 | 2.017 | -8.971 | -3.788 |
| 2010 | -0.746 | 0.163 | -0.385 | 1.196 | 0.125 |
| | ARMAXCS/ SRCS | ARMAXCS/ SRCE | ARMAXCS/ SRGDP | ARMAXCS/ MR | ARMAXCS/ VAR |
| 2001 | 1.120 | 1.895 | 1.010 | 0.997 | 1.532 |
| 2002 | -1.691 | -1.303 | -1.844 | -2.285 | -1.195 |
| 2003 | -1.018 | -0.250 | -0.307 | -0.489 | -1.223 |
| 2004 | -0.631 | -0.018 | 0.248 | 2.410 | 0.138 |
| 2005 | -0.288 | 0.129 | -0.636 | 0.455 | -0.227 |
| 2006 | -0.176 | 0.161 | 0.224 | 3.151 | -0.263 |
| 2007 | -0.123 | -0.232 | 0.201 | -0.628 | -0.746 |
| 2008 | 0.383 | -0.712 | -3.704 | -12.563 | -2.080 |
| 2009 | 0.095 | -1.945 | -8.806 | -11.712 | -3.175 |
| 2010 | -0.136 | -1.133 | -1.088 | 0.866 | -0.103 |
| | ARMAXE/ ARMAXGDP | ARMAXE/ SRBR | ARMAXE/ SRCC | ARMAXE/ SRCOr | ARMAXE/ SRCOu |
| 2001 | -0.905 | 0.891 | 0.723 | 0.092 | 0.823 |
| 2002 | -1.335 | -2.098 | -2.547 | -2.904 | -1.809 |
| 2003 | 2.143 | -1.017 | -0.307 | -3.101 | -1.429 |
| 2004 | 1.884 | -0.366 | -0.645 | 1.913 | -0.052 |
| 2005 | -0.910 | -0.180 | 0.104 | 0.885 | -0.326 |
| 2006 | 0.141 | -0.011 | 0.363 | 5.490 | 1.079 |
| 2007 | -0.052 | 0.004 | -0.299 | 0.216 | 1.130 |
| 2008 | -4.277 | -0.303 | 1.351 | -8.063 | 0.101 |
| 2009 | -9.571 | -0.971 | 2.230 | -9.253 | -3.957 |
| 2010 | -0.841 | -0.395 | -1.070 | 0.752 | -0.434 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|--------------------|--------------------|--------------------|-------------------|
| | ARMAXE/ SRCS | ARMAXE/ SRE | ARMAXE/ SRGDP | ARMAXE/ MR | ARMAXE/ VAR |
| 2001 | 1.011 | 1.688 | 0.832 | 0.872 | 1.427 |
| 2002 | -1.947 | -1.655 | -2.110 | -2.540 | -1.419 |
| 2003 | -1.052 | -0.474 | -0.494 | -0.632 | -1.371 |
| 2004 | -0.632 | -0.241 | 0.047 | 2.303 | 0.010 |
| 2005 | -0.209 | 0.172 | -0.575 | 0.506 | -0.186 |
| 2006 | -0.111 | 0.162 | 0.220 | 3.209 | -0.255 |
| 2007 | -0.169 | -0.364 | 0.075 | -0.727 | -0.846 |
| 2008 | 0.464 | 0.059 | -2.926 | -12.199 | -1.596 |
| 2009 | -0.277 | -2.106 | -8.685 | -12.017 | -3.365 |
| 2010 | -0.448 | -1.654 | -1.524 | 0.498 | -0.466 |
| | ARMAXGDP/ SRBR | ARMAXGDP/ SRCC | ARMAXGDP/ SRCOr | ARMAXGDP/ SRCOu | ARMAXGDP/ SRCS |
| 2001 | -0.944 | -2.134 | -1.323 | -1.063 | -0.848 |
| 2002 | -1.211 | -3.331 | -1.900 | -1.257 | -1.167 |
| 2003 | 2.327 | 4.319 | 0.576 | 2.177 | 2.588 |
| 2004 | 1.954 | 1.584 | 3.259 | 2.088 | 2.356 |
| 2005 | -0.947 | -0.044 | -0.095 | -0.966 | -0.907 |
| 2006 | 0.129 | 1.511 | 3.704 | 0.408 | 0.245 |
| 2007 | -0.089 | -0.639 | 0.210 | 0.228 | 0.105 |
| 2008 | -4.364 | -0.438 | -8.926 | -4.432 | -5.641 |
| 2009 | -9.783 | -2.154 | -14.249 | -10.735 | -10.310 |
| 2010 | -0.825 | -3.311 | -0.063 | -0.892 | -0.460 |
| | ARMAXGDP/ SRE | ARMAXGDP/ SRGDP | ARMAXGDP/ MR | ARMAXGDP/ VAR | SRBR/ SRCC |
| 2001 | -0.903 | -0.946 | -0.603 | -0.353 | -0.586 |
| 2002 | -1.240 | -1.335 | -1.733 | -1.038 | -0.919 |
| 2003 | 2.359 | 2.184 | 1.738 | 1.659 | 0.589 |
| 2004 | 2.029 | 1.971 | 3.300 | 1.959 | -0.088 |
| 2005 | -0.876 | -0.996 | -0.210 | -0.690 | 0.301 |
| 2006 | 0.189 | 0.235 | 2.366 | 0.147 | 0.497 |
| 2007 | -0.090 | 0.013 | -0.431 | -0.306 | -0.146 |
| 2008 | -4.441 | -5.077 | -11.497 | -4.413 | 1.154 |
| 2009 | -10.216 | -11.966 | -15.230 | -9.773 | 2.303 |
| 2010 | -1.084 | -1.231 | -0.115 | -0.736 | -0.985 |
| | SRBR/ SRCOr | SRBR/ SRCOu | SRBR/ SRCS | SRBR/ SRE | SRBR/ SRGDP |
| 2001 | -1.557 | -0.312 | -0.062 | 1.238 | 0.120 |
| 2002 | -2.432 | 0.017 | -0.095 | 0.552 | -0.465 |
| 2003 | -3.766 | -0.574 | 0.070 | 0.813 | 0.528 |
| 2004 | 3.942 | 0.257 | 0.239 | 0.233 | 0.468 |
| 2005 | 1.721 | -0.258 | -0.005 | 0.560 | -0.648 |
| 2006 | 8.927 | 0.961 | 0.056 | 0.289 | 0.294 |
| 2007 | 0.729 | 1.027 | 0.121 | -0.597 | 0.053 |
| 2008 | -13.274 | 0.057 | -0.871 | 0.407 | -3.859 |
| 2009 | -15.137 | -3.377 | -0.562 | -2.273 | -11.382 |
| 2010 | 1.410 | -0.236 | 0.121 | -2.223 | -1.741 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|-----------------|----------------|-----------------|----------------|
| | SRBR/ MR | SRBR/ SRCOu | SRBR/ SRCS | SRBR/ SRE | SRBR/ SRGDP |
| 2001 | -0.135 | -0.312 | -0.062 | 1.238 | 0.120 |
| 2002 | -2.165 | 0.017 | -0.095 | 0.552 | -0.465 |
| 2003 | -0.089 | -0.574 | 0.070 | 0.813 | 0.528 |
| 2004 | 4.156 | 0.257 | 0.239 | 0.233 | 0.468 |
| 2005 | 1.004 | -0.258 | -0.005 | 0.560 | -0.648 |
| 2006 | 4.931 | 0.961 | 0.056 | 0.289 | 0.294 |
| 2007 | -0.690 | 1.027 | 0.121 | -0.597 | 0.053 |
| 2008 | -18.414 | 0.057 | -0.871 | 0.407 | -3.859 |
| 2009 | -18.296 | -3.377 | -0.562 | -2.273 | -11.382 |
| 2010 | 0.843 | -0.236 | 0.121 | -2.223 | -1.741 |
| Year | SRBR/ VAR | SRCC/ SRCOr | SRCC/ SRCOu | SRC/ SRCS | SRCC/ SRE |
| | | | | | |
| 2001 | 1.620 | -1.420 | -1.112 | -0.093 | -0.004 |
| 2002 | -0.068 | -2.434 | -1.299 | -0.212 | -2.121 |
| 2003 | -1.304 | -3.125 | 0.665 | 0.287 | 3.496 |
| 2004 | 0.454 | 3.461 | 0.219 | 0.044 | -0.070 |
| 2005 | -0.121 | 1.800 | 0.420 | 0.081 | 1.966 |
| 2006 | -0.461 | 8.759 | 2.386 | 0.149 | 2.229 |
| 2007 | -1.587 | 0.364 | 1.170 | -0.043 | -1.374 |
| 2008 | -2.551 | -11.437 | 2.914 | -0.012 | 5.372 |
| 2009 | -5.000 | -11.950 | 0.839 | 0.756 | 6.353 |
| 2010 | -0.364 | 1.031 | -1.883 | -0.149 | -6.255 |
| Year | SRCC/ SRGDP | SRCC/ MR | SRCC/ VAR | SRCOr/ SRCOu | SRCOr/ SRCS |
| | | | | | |
| 2001 | -0.342 | 1.059 | 0.411 | -1.057 | -1.027 |
| 2002 | -1.084 | -0.243 | -2.159 | -2.246 | -1.918 |
| 2003 | 0.750 | -1.470 | 0.414 | -3.357 | -3.261 |
| 2004 | 0.547 | 4.241 | 0.241 | 3.448 | 3.992 |
| 2005 | -0.444 | 0.246 | 0.779 | 1.861 | 1.667 |
| 2006 | 0.610 | 3.743 | 0.901 | 8.125 | 8.688 |
| 2007 | 0.103 | -0.480 | -1.961 | -0.563 | 0.657 |
| 2008 | -3.428 | -21.014 | 0.839 | -13.304 | -13.774 |
| 2009 | -10.374 | -23.386 | 1.607 | -11.489 | -14.103 |
| 2010 | -2.261 | 2.902 | -2.712 | 1.782 | 2.005 |
| Year | SRCOr/ SRE | SRCOr/ SRGDP | SRCOr/ MR | SRCOr/ VAR | SRCOu/ SRCS |
| | | | | | |
| 2001 | -0.437 | -0.847 | 0.207 | 0.230 | -0.191 |
| 2002 | -1.746 | -1.792 | -1.748 | -1.613 | 0.109 |
| 2003 | -2.944 | -2.081 | 0.034 | -3.395 | -0.362 |
| 2004 | 3.798 | 2.916 | 3.773 | 2.682 | 0.563 |
| 2005 | 2.019 | 0.775 | 0.925 | 0.881 | -0.143 |
| 2006 | 8.644 | 6.117 | 4.653 | 5.039 | 1.114 |
| 2007 | 0.167 | 0.536 | -0.912 | -0.867 | 1.226 |
| 2008 | -12.067 | -11.066 | -17.340 | -10.180 | -0.531 |
| 2009 | -15.484 | -16.972 | -16.698 | -13.199 | -3.589 |
| 2010 | -0.134 | -0.086 | 1.004 | 0.511 | 0.030 |

| Year | OLS Combination Forecasting | | | | |
|------|-----------------------------|--------------|----------------|--------------|---------------|
| | SRCOu/ SRE | SRCS/ SRE | SRCS/ SRGDP | SRCS/ MR | SRCS/ VAR |
| 2001 | 0.621 | 1.035 | 0.552 | 0.207 | 1.580 |
| 2002 | 0.251 | 0.381 | -0.399 | -1.748 | -0.172 |
| 2003 | 0.324 | 0.864 | 1.739 | 0.034 | -1.018 |
| 2004 | 0.423 | 0.614 | 2.329 | 3.773 | 1.091 |
| 2005 | 0.350 | 0.536 | -0.608 | 0.925 | -0.053 |
| 2006 | 0.672 | 0.390 | 0.891 | 4.653 | -0.250 |
| 2007 | 0.115 | -0.292 | 0.943 | -0.912 | -1.217 |
| 2008 | 0.057 | -0.896 | -10.335 | -17.340 | -4.516 |
| 2009 | -3.422 | -2.824 | -16.418 | -16.698 | -6.119 |
| 2010 | -1.730 | -1.741 | -0.588 | 1.004 | 0.046 |
| | SRE/ SRGDP | SRE/ MR | SRE/ VAR | SRGDP/ MR | SRGDP/ VAR |
| | | | | | |
| 2001 | -0.196 | 0.860 | 1.049 | 0.207 | 1.116 |
| 2002 | -0.746 | -1.508 | -0.445 | -1.748 | -0.499 |
| 2003 | 0.372 | 0.505 | -1.670 | 0.034 | -0.786 |
| 2004 | 0.615 | 3.986 | 0.518 | 3.773 | 0.917 |
| 2005 | -0.637 | 1.293 | -0.292 | 0.925 | -0.256 |
| 2006 | 0.355 | 4.844 | -0.496 | 4.653 | 0.005 |
| 2007 | 0.228 | -1.175 | -1.291 | -0.912 | -0.904 |
| 2008 | -4.187 | -17.099 | -3.035 | -17.340 | -4.236 |
| 2009 | -11.735 | -18.331 | -4.881 | -16.698 | -10.160 |
| 2010 | -1.738 | -0.453 | 0.291 | 1.004 | -1.172 |
| | MR/ VAR | SRE/ MR | SRE/ VAR | SRGDP/ MR | SRGDP/ VAR |
| | | | | | |
| 2001 | 0.915 | 0.860 | 1.049 | 0.207 | 1.116 |
| 2002 | -1.483 | -1.508 | -0.445 | -1.748 | -0.499 |
| 2003 | -0.767 | 0.505 | -1.670 | 0.034 | -0.786 |
| 2004 | 3.134 | 3.986 | 0.518 | 3.773 | 0.917 |
| 2005 | 0.622 | 1.293 | -0.292 | 0.925 | -0.256 |
| 2006 | 3.221 | 4.844 | -0.496 | 4.653 | 0.005 |
| 2007 | -1.481 | -1.175 | -1.291 | -0.912 | -0.904 |
| 2008 | -14.473 | -17.099 | -3.035 | -17.340 | -4.236 |
| 2009 | -15.581 | -18.331 | -4.881 | -16.698 | -10.160 |
| 2010 | 0.452 | -0.453 | 0.291 | 1.004 | -1.172 |