When to (or not to) trust intelligent machines: Insights from an evolutionary game theory analysis of trust in repeated games

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Abstract

The actions of intelligent agents, such as chatbots, recommender systems, and virtual assistants are typically not fully transparent to the user. Consequently, users take the risk that such agents act in ways opposed to the users' preferences or goals. It is often argued that people use trust as a cognitive shortcut to reduce the complexity of such interactions. Here we formalise this by using the methods of evolutionary game theory to study the viability of trust-based strategies in repeated games. These are reciprocal strategies that cooperate as long as the other player is observed to be cooperating. Unlike classic reciprocal strategies, once mutual cooperation has been observed for a threshold number of rounds they stop checking their co-player's behaviour every round, and instead only check it with some probability. By doing so, they reduce the *opportunity cost* of verifying whether the action of their co-player was actually cooperative. We demonstrate that these trustbased strategies can outcompete strategies that are always conditional, such as Tit-for-Tat, when the opportunity cost is non-negligible. We argue that

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this cost is likely to be greater when the interaction is between people and intelligent agents, because of the reduced transparency of the agent. Consequently, we expect people to use trust-based strategies more frequently in interactions with intelligent agents. Our results provide new, important insights into the design of mechanisms for facilitating interactions between humans and intelligent agents, where trust is an essential factor.

Keywords: Trust, evolutionary game theory, intelligent agents, cooperation, prisoner's dilemma, repeated games

1 1. Introduction

Artificial intelligence is undoubtedly becoming more integrated into our 2 every day lives. While much attention has recently been paid to deep machine 3 learning, intelligent agents that exhibit goal directed behaviour (Wooldridge, Δ 2009) have also come of age. These range from purely software systems such 5 as videogame characters or chatbots, through to cyberphysical systems such 6 as smart fridges or autonomous vehicles. We are delegating more and more 7 aspects of our daily lives to these agents, from the virtual sales agent that 8 recommends products and services to us on an e-commerce website (Beldad 9 et al., 2016), to the intelligent virtual assistant (e.g. Amazon Alexa, Apple 10 Siri, Google Home) that plans our route to work and orders goods and ser-11 vices for us on command (Chung et al., 2017). But in all of these cases, the 12 operation of the agent is not fully transparent to the end user. Although 13 research in explainable AI is beginning to address these issues (Nunes and 14 Jannach, 2017), it seems unlikely that a user will ever be able to get complete 15 information about how and why the agent has taken a particular decision. 16 Consequently, using such an agent, and accepting its recommendations, nec-17 essarily involves the user placing some degree of trust in the agent. In the 18 broadest sense, trust is willingness to take risk under uncertainty (Luhmann, 19 1979). Here the risk is that the agent will act in a way opposed to our own 20 goals, and the uncertainty comes from us lacking complete information about 21 the behaviour of the agent to be able to ascertain this. 22

For example, consider again the virtual sales agent operating on the website of an e-commerce company (Chattaraman et al., 2012), which sells products to customers based on the information that it learns about the customer through a chat dialogue, i.e. an agent-based recommender system (Pu and Chen, 2007; Yoo et al., 2012; Jugovac and Jannach, 2017). When a customer

interacts with this virtual sales agent it does not have complete information 28 about why product A from company X is being recommended as opposed 29 to product B from company Y (Grabner-Kraeuter, 2002). Thus, if the cus-30 tomer is going to use the virtual sales agent, they must take some degree 31 of risk, for example, that the virtual sales agent recommends more expen-32 sive products, or those from manufacturers that the seller has a preferential 33 relationship with, or does not provide full information about the quality of 34 the product. Without a full understanding of the virtual sales agent's source 35 code, the specifications of the alternative products, and the relationships be-36 tween the sellers and manufacturers (Akerlof, 1970; Mahadevan, 2000; Lewis, 37 2011), some degree of risk and hence trust must be involved (Luhmann, 1979; 38 Grabner-Kraeuter, 2002; Kumar et al., 2020). Similarly, when a virtual as-39 sistant gives us directions, we do not have complete information either about 40 the route planning algorithm that it is using, or about relevant environmen-41 tal conditions such as traffic levels. Again, this means that the use of such 42 systems necessarily involves some degree of risk and hence trust. 43

This raises the question: how will people behave when interacting with 44 these kinds of intelligent agents? How will they handle the complexity of the 45 interaction? Ultimately, this question will need to be answered by empirical 46 work. However, to guide the empirical work it is necessary to generate hy-47 potheses about how we expect people to behave. Because intelligent agents 48 exhibit goal directed behaviour, and their goals (as programmed by their 49 designers) may be in conflict with the goals of their users, evolutionary game 50 theory (EGT) (Maynard Smith, 1982; Sigmund, 2010) provides a suitable 51 formal framework for modelling the strategic interaction and understanding 52 behavioural dynamics (Shoham, 2008). This is because not only is the inter-53 action strategic, but there is empirical evidence that people use a standard 54 set of social scripts whether they are interacting with a person or a machine in 55 a particular social situation (Nass and Moon, 2000). This suggests that pre-56 dictions from game theoretical studies about human behaviour in traditional 57 (e-)commerce, for example (e.g. Laaksonen et al. 2009; Dahlstrom et al. 58 2014), can also be useful when the interaction is between a human and an 59 intelligent agent representing another entity (individual, firm, organisation), 60 rather than with that entity directly. 61

In light of this, we propose that the types of interaction discussed above can be modelled as repeated games between the user and the agent (acting to fulfil the goals of its designer). Moreover, in important cases the actions available to the agent and the user correspond to "cooperate" and "defect".

Cooperation between players represents both the user and agent behaving 66 honestly, reliably and transparently with each other. For example, coopera-67 tion would be a virtual sales agent selling products that match the preferences 68 that the user has revealed in the conversation, while defection might corre-69 spond to trying to upsell products or warranties. On the side of the user, 70 cooperation could represent continued use of the agent, which benefits the 71 seller by reducing their opportunity costs of answering customer enquiries 72 themselves. Defection would then represent refusing to use the agent and 73 instead speaking directly to a human sales advisor. 74

The folk theorem of repeated games tells us that the key to cooperative 75 outcomes, which benefit both sides, is sufficient information for the play-76 ers to be able to condition their actions on the past actions of the other 77 player(s) (Fudenberg and Maskin, 1986). This allows for reciprocal strate-78 gies, e.g. cooperate if the other player cooperated in the previous interaction. 79 as exemplified by the Tit-for-Tat strategy (Axelrod, 1984). However, the use 80 of reciprocal strategies necessarily carries an opportunity cost. Part of this 81 comes from devoting cognitive resources to remembering a history of past 82 actions, and processing this when deciding how to act. But in addition to 83 this, reciprocal strategies also involve *verifying* whether the observed action 84 of the other player actually was cooperative or not. In traditional face-to-face 85 interactions between humans verifying whether the other player cooperated 86 might involve, for example, checking the quality and specification of goods 87 that have been purchased, or that the correct amount of change has been 88 given. However, these costs are usually assumed to be low compared to the 89 benefit and cost of cooperation (Ho, 1996; Imhof et al., 2005a; Han, 2013), 90 and are mostly omitted in (evolutionary) game theoretic models (McNally 91 et al., 2012; Han et al., 2013b; Martinez-Vaquero et al., 2015; Garcia and 92 van Veelen, 2018; Hilbe et al., 2017; Glynatsi and Knight, 2020; Han et al., 93 2020). But the transition to interactions over the internet increases these 94 costs (Grabner-Kraeuter, 2002), since the increased separation in space and 95 time over the course of the interaction makes verifying the action of the other 96 player more costly. The move to interacting with intelligent agents increases 97 these costs even more, since the interaction becomes less transparent to the 98 user, and artificial agents have limited capacity to explain their action com-99 pared to humans. This issue becomes even more relevant when considering 100 hybrid societies of humans and intelligent agents (Paiva et al., 2018; Santos 101 et al., 2019). 102

¹⁰³ It is often argued that humans use trust as a cognitive shortcut, to reduce

the complexity of the interaction that they need to reason about (Luhmann, 104 1979; Grabner-Kraeuter, 2002; Petruzzi et al., 2014). In this paper, we for-105 malise this in EGT by introducing trust-based strategies in repeated games, 106 and study their evolutionary viability when competing with other strategies 107 in repeated games, in a similar fashion to Imhof et al. (2005a). Unlike tra-108 ditional Tit-for-Tat, trust-based strategies only check a co-player's actions 109 occasionally after a trust threshold has been reached, i.e. after their co-110 player has cooperated for a certain number of rounds. By doing so, they 111 reduce the opportunity cost of verifying the action of their co-player every 112 round. We demonstrate that trust-based strategies can be more successful 113 than Tit-for-Tat when the opportunity cost of using a conditional strategy 114 is non-negligible. Moreover, one may ask under what kinds of interaction 115 or business at hand are trust-based strategies more likely to be used by the 116 parties involved? For instance, will users trust in a chatbot to handle highly 117 important interactions such as a multi-million dollar transaction? We show 118 that trust-based strategies are most successful when the interaction is of in-119 termediate importance, and the interaction is repeated over many rounds. 120 These results provide game theoretic support for the theory that humans use 121 trust to reduce the complexity of interactions, and suggest that people are 122 likely to behave even more in this manner when interactions are with intelli-123 gent agents, since the opportunity costs of verifying the actions of intelligent 124 agents are likely to be greater. 125

¹²⁶ 2. Models and Methods

127 2.1. Models

We consider a population of constant size N. At each time step or generation, a random pair of players are chosen to play with each other.

130 2.2. Interaction between Individuals

Interactions are modelled as a symmetric two-player prisoner's dilemma
game, defined by the following payoff matrix (for row player)

$$\begin{array}{ccc}
C & D \\
C & R & S \\
D & T & P
\end{array}.$$

¹³³ A player who chooses to cooperate (C) with someone who defects (D) receives ¹³⁴ the sucker's payoff S, whereas the defecting player gains the temptation to

defect, T. Mutual cooperation (resp., defection) yields the reward R (resp., 135 punishment P) for both players. Depending on the ordering of these four 136 payoffs, different social dilemmas arise (Macy and Flache, 2002; Santos et al., 137 2006). Namely, in this work we are concerned with the prisoner's dilemma 138 (PD), where T > R > P > S. In a single round, it is always best to defect, 139 but cooperation may be rewarded if the game is repeated. In repeated PD, it 140 is also required that mutual cooperation is preferred over an equal probability 141 of unilateral cooperation and defection (2R > T + S); otherwise alternating 142 between cooperation and defection would lead to a higher payoff than mutual 143 cooperation. For convenience and a clear representation of results, we later 144 mostly use the Donation game (Sigmund, 2010)—a famous special case of 145 the PD—where T = b, R = b - c, P = 0, S = -c, satisfying that b > c > 0, 146 where b and c stand respectively for "benefit" and "cost" (of cooperation). 147

In addition, in order to understand how the duration of the interaction or business at hand impacts the evolutionary viability of trust-based strategies in relation to others, we model how important or beneficial an interaction is using parameter $\gamma > 0$ (Han et al., 2013a). Hence, the payoff matrix becomes

$$\begin{array}{ccc}
C & D \\
C \left(\begin{array}{cc}
\gamma R & \gamma S \\
\gamma T & \gamma P \end{array} \right).
\end{array}$$

In a population of N individuals interacting via a repeated (or iterated) PD, whenever two specific strategies are present in the population, say **A** and **B**, the fitness of an individual with a strategy **A** in a population with kAs and (N - k) **B**s can be written as

$$\Pi_A(k) = \frac{1}{r(N-1)} \sum_{j=1}^r [(k-1)\pi_{A,A}(j) + (N-k)\pi_{A,B}(j)], \qquad (1)$$

where $\pi_{A,A}(j)$ $(\pi_{A,B}(j))$ stands for the payoff obtained from a round j as a 156 result of their mutual behavior of an A strategist in an interaction with a A 157 (B) strategist (as specified by the payoff matrix above), and r is the total 158 number of rounds of the PD. As usual, instead of considering a fixed number 159 of rounds, upon completion of each round, there is a probability w that yet 160 another round of the game will take place, resulting in an average number of 161 $r = (1 - w)^{-1}$ rounds per interaction (Sigmund, 2010). In the following, all 162 values of Π will be computed analytically. 163

¹⁶⁴ 2.3. Strategies in IPD and the opportunity cost

The repeated (or iterated) PD is usually known as a story of tit-for-tat (TFT), which won both Axelrod's tournaments (Axelrod, 1984; Axelrod and Hamilton, 1981). *TFT* starts by cooperating, and does whatever the opponent did in the previous round. It will cooperate if the opponent cooperated, and will defect if the opponent defected.

As a conditional strategy, TFT incurs an additional opportunity cost, 170 denoted by ϵ , compared to the unconditional strategies, namely, ALLC (al-171 ways cooperate) and ALLD (always defect). This cost involves a cognitive 172 cost (to memorise previous interaction outcomes with co-players and make a 173 decision based on them) and moreover, a cost of revealing the actual actions 174 of co-players (cf. Introduction). The latter cost is usually ignored in previous 175 works of IPD, but it can be non-trivial and thus significantly influence the 176 nature of interactions. For instance, this cost is crucial to be considered in 177 the context of human-machine interactions. For example, it might be quite 178 costly and time consuming to check if one was charged the right amount 179 when pay online/by Card/on ATM/ and whether the quality of the coffee 180 produced by your coffee machine is reducing (and to what extent). This cost 181 is even greater when interacting with intelligent agents whose operation and 182 hence goals are less transparent, and which might, for example, be designed 183 to hide pertinent information from users. 184

185 Trust-based strategies

We consider a new trust-based strategy that is capable of switching off the 186 costly deliberation process when it trusts its co-players enough ¹. Namely, 187 this strategy starts an IPD interaction as a TFT player. When its ongoing 188 trust level towards the co-player—defined here as the difference between the 189 number of cooperative and defective moves from the co-player so far in the 190 IPD—reaches a certain threshold, denoted by θ , it will play C uncondition-191 ally. We denote this strategy by TUC. TUC is illustrated in the Figure 1 192 representing one game between TUC and TFT. 193

¹Our modelling approach is in accordance with the definition of trust often adopted in various multi-agent research, e.g. (Dasgupta, 2000; Ramchurn et al., 2004). That is, trust is a belief an agent has that the other party will do what it says it will (being honest and reliable) or reciprocate (being reciprocal for the common good of both), given an opportunity to defect to get higher payoffs.

Trust reached

Player 1	Checking	Yes	Yes	Yes	No	Yes	No	Yes	No
TUC	Action	С	С	С	C	С	С	С	С
Player 2	Action	С	C	C			C		

Figure 1: Diagram representing repeated interactions between a trust-based cooperator TUC and a tit-for-tat TFT. First, both strategies cooperate and check other player's action. After θ rounds (here $\theta = 3$), trust is reached and TUC now checks the action of TFT occasionally with a probability p. Because TFT continues to cooperate, TUC continues to trust and to cooperate.

Given the possibility of being exploited, but still to avoid costly deliberation, we assume that TUC will check, with a probability p, the co-player's actions after switching off². If the co-player is found out to defect, TUC will revert to its initial strategy, i.e. TFT. As a counterpart of TUC, we consider TUD that whenever the ongoing trust level reaches the threshold θ , switches to playing D unconditionally. TUD is illustrated in the Figure 2 representing one game between TUC and TUD.

The payoff matrix for the five strategies ALLC, ALLD, TFT, TUC and TUD, can be given as follows

	AllC	AllD	\mathbf{TFT}	TUC	\mathbf{TUD}
AllC	(R	S	R	R	$\frac{\theta R + (r - \theta)S}{r}$
AllD	T	P	$\frac{T + (r-1)P}{r}$	$\frac{T+(r-1)P}{r}$	$\frac{T+(r-1)P}{r}$
TFT	$R-\varepsilon$	$\frac{S+(r-1)P}{r} - \varepsilon$	$R-\varepsilon$	$R-\varepsilon$	$\frac{\theta R + S + (r - \theta - 1)P}{r} - \varepsilon$
TUC	$R - \frac{\theta \varepsilon}{r} - \frac{p(r-\theta)\varepsilon}{r}$	$\frac{S+(r-1)P}{r} - \varepsilon$	$R - \frac{\theta \varepsilon}{r} - \frac{p(r-\theta)\varepsilon}{r}$	$R - \frac{\theta \varepsilon}{r} - \frac{p(r-\theta)\varepsilon}{r}$	$\Pi_{TUC,TUD}$
TUD	$\frac{\theta R + (r - \theta)T - \theta \varepsilon}{r}$	$\frac{S + (r-1)P}{r} - \varepsilon$	$\frac{\theta R + T + (r - \theta - 1)P - \theta \varepsilon}{r}$	$\Pi_{TUD,TUC}$	$\frac{\theta R + (r - \theta) P - \theta \varepsilon}{r}$
		·	·	(2)) , , , ,

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For clarity, we write the payoff of TUC against TUD and TUD against

 $^{^2 \}rm We$ assume that, given a sufficient cost of checking, TUC can always correctly find out the co-player's actions.



Figure 2: Diagram representing repeated interactions between a trust-based cooperator TUC and a trust-based defector TUD. First, both strategies cooperate and check the other player's action. After θ rounds (here $\theta = 3$), trust is reached for both strategies. TUC now cooperates and TUD defects. This continues until TUC checks and realises that TUD defects. After that, TUC looses trust, plays as a TFT and defects.

TUC separately. Namely, the payoff of TUC against TUD is given by

$$\Pi_{TUC,TUD} = \frac{1}{r} \left(\theta R - \theta \varepsilon + S + p(r'-1)(P-\epsilon) + (1-p)(S+p(r'-2)(P-\epsilon) + (1-p)[....]) \right) \\ = \frac{1}{r} \left(\theta R - \theta \varepsilon + S \sum_{i=0}^{r'-1} (1-p)^i + p(P-\epsilon) \sum_{i=0}^{r'-1} (r'-i-1)(1-p)^i \right) \\ = \frac{\theta R - \theta \varepsilon}{r} + \frac{1}{r} \left(\frac{S(1-(1-p)^{r-\theta})}{p} + \frac{(P-\varepsilon)((1-p)^{r-\theta} + (r-\theta)p-1))}{p} \right)$$

where $r' = r - \theta$. Similarly,

$$\Pi_{TUD,TUC} = \frac{\theta R - \theta \varepsilon}{r} + \frac{1}{r} \left(\frac{T(1 - (1 - p)^{r - \theta})}{p} + \frac{P((1 - p)^{r - \theta} + (r - \theta)p - 1)}{p} \right)$$

The payoff formulas can be explained as follows. In the first θ rounds both TUC and TUD play C and keep checking, so they obtain in each round $R-\epsilon$. As trust is reached, from next rounds TUC will check only occasionally with probability p. For example, if in the next round TUC checks, it obtains Sin that round and $P - \epsilon$ in the remaining rounds since it will play TFT. Otherwise, i.e. if TUC does not check in that round (with probability 1-p), the process above is iterated for the payoffs calculation.

211 2.4. Evolutionary dynamics in finite populations

We resort in this paper to Evolutionary Game Theory methods for finite populations understanding evolutionary dynamics of trust-based behaviours, in relation to other strategies (Imhof et al., 2005b). In this context, agents' payoff represents their *fitness* or social *success*, and evolutionary dynamics is shaped by social learning (Sigmund, 2010), assuming that more successful agents will tend to be imitated more often by the others. We adapt here the pairwise comparison rule (Traulsen et al., 2006) to model social learning, where an agent A with fitness f_A adopts the strategy of another agent Bwith fitness f_B with probability given by the Fermi function,

$$P_{A\to B} = \left(1 + e^{-\beta(f_B - f_A)}\right)^{-1}.$$

The parameter β stands for the imitation strength or intensity of selection, i.e., how strongly agents base their decision to imitate on fitness comparison, where with $\beta = 0$, the imitation decision is random, while for increasing β , imitation becomes increasingly deterministic.

In the absence of behavioural exploration or mutations, end states of 216 evolution inevitably are monomorphic. That is, whenever such a state is 217 reached, it cannot be escaped via imitation. Thus, we further assume that. 218 with some mutation probability, an agent can freely explore its behavioural 219 space. In the limit of small mutation rates, the behavioural dynamics can 220 be conveniently described by a Markov Chain, where each state represents a 221 monomorphic population, whereas the transition probabilities are given by 222 the fixation probability of a single mutant. The resulting Markov Chain has a 223 stationary distribution, which characterises the average time the population 224 spends in each of these monomorphic end states. 225

Suppose there exist at most two strategies in the population, say, k agents using strategy A ($0 \le k \le N$) and (N - k) agents using strategies B. Let us denote by $\pi_{X,Y}$ the payoff an agent using strategy X obtained in an interaction with another individual using strategy Y (as given in the payoff matrix (2)). Hence, the (average) payoff of the agent that uses A and B can be written as follows, respectively,

$$\Pi_{A}(k) = \frac{(k-1)\pi_{A,A} + (N-k)\pi_{A,B}}{N-1},$$

$$\Pi_{B}(k) = \frac{k\pi_{B,A} + (N-k-1)\pi_{B,B}}{N-1},$$
(3)

Now, the probability to change the number k of agents using strategy A by \pm one in each time step can be written as (Traulsen et al., 2006)

$$T^{\pm}(k) = \frac{N-k}{N} \frac{k}{N} \left[1 + e^{\mp\beta [\Pi_A(k) - \Pi_B(k)]} \right]^{-1}.$$
 (4)

The fixation probability of a single mutant with a strategy A in a population of (N-1) agents using B is given by (Traulsen et al., 2006; Karlin and Taylor, 1975; Imhof et al., 2005b)

$$\rho_{B,A} = \left(1 + \sum_{i=1}^{N-1} \prod_{j=1}^{i} \frac{T^{-}(j)}{T^{+}(j)}\right)^{-1}.$$
(5)

When considering a set $\{1, ..., s\}$ of distinct strategies, these fixation probabilities determine the Markov Chain transition matrix $M = \{T_{ij}\}_{i,j=1}^{s}$, with $T_{ij,j\neq i} = \rho_{ji}/(s-1)$ and $T_{ii} = 1 - \sum_{j=1, j\neq i}^{s} T_{ij}$. The normalised eigenvector of the transposed of M associated with the eigenvalue 1 provides the above described stationary distribution (Imhof et al., 2005b), which defines the relative time the population spends while adopting each of the strategies.

243 **3. Results**

We use the model defined above to answer two questions. First, when will 244 individuals use trust? To answer this question, we investigate under which 245 conditions trust is an evolutionary viable strategy. We measure the success 246 of trust by the frequency of the trust-based cooperative strategy (TUC), i.e. 247 the proportion of time the population is composed of only TUC. Second, 248 when should there be trust? This is measured by how well the prevalence 249 of trust-based behaviour enhances cooperation outcomes. We investigate the 250 second question by looking under which conditions the presence of trust-251 based strategies (both TUC and TUD) increase the frequency of cooperation 252 in the population. 253

The default values of the parameters, unless otherwise specified, are for the game payoffs R = 1, S = -1, T = 2, P = 0 (i.e. b = 2 and c = 1 in Donation game), the importance of the game $\gamma = 1$, the number of rounds r = 50, the population size N = 100, the intensity of selection $\beta = 0.1$, the trust threshold $\theta = 3$, the probability of checking its partner p = 0.25 and the opportunity cost $\epsilon = 0.25$. The analysis of the model has been implemented using the package EGTTools (Fernández Domingos, 2020).



Figure 3: Left: Frequency of strategies as a function of the opportunity cost ϵ . Right: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the opportunity cost ϵ . The difference in frequency of cooperation between the two scenario is shaded in green when positive and red when negative.

²⁶¹ 3.1. Trust as a mechanism to reduce opportunity costs

The intuitive benefit of trusting something is to limit the cost of monitoring their actions in a long-term interaction, providing a shortcut in the decision making process. This is in line with several common definitions and theories of trust (Luhmann, 1979; Grabner-Kraeuter, 2002; Petruzzi et al., 2014). Thus, we explore first the effect of opportunity cost ϵ on the strategies employed by individuals and the resulting frequency of cooperation.

The left panel of Figure 3 shows that TUC is the most common strategy 268 for a low to intermediate opportunity cost ϵ (between 0 and 0.3). When the 260 opportunity cost ϵ is zero, both TUC and TFT are successful strategies and 270 the population is composed of either one of them for most of the time. The 271 success of TUC and TFT is explained by the capacity of these strategies to 272 maintain high levels of cooperation within their homogeneous populations, 273 while avoiding exploitation by AllD. Yet, the success of TFT is limited by 274 the opportunity cost paid to check its partner's actions. This is shown in the 275 results by the population being mostly AllD when the opportunity cost ϵ is 276 high. Compared to TFT, TUC can limit this opportunity cost by reducing 277 its attention to its partner's actions once trust is reached. This is why as 278 the opportunity cost increases, the frequency of TFT plummets while TUC 279 becomes more commonly observed. 280

²⁸¹ The right panel of Figure 3 shows that the presence of trust-based strate-

gies increases the frequency of cooperation ³. Importantly, this increase happens even when the opportunity cost ϵ is high ($\epsilon \approx c$), and not only when TUC is the most frequent, e.g. for low ϵ . This is because a high frequency of cooperation is already reached for a low opportunity cost due to TFT. The presence of TUC has a more important effect on cooperation when the opportunity cost increases since in that case the performance of TFT significantly reduces.

To conclude, trust-based cooperation is a particularly common strategy, in particular in interactions with moderate opportunity cost, and it promotes cooperation for a large range of opportunity costs.

²⁹² 3.2. Length of interactions and importance of the game

We now investigate (i) the importance of the game γ because this affects 293 the *relative* cost of checking the other player and (ii) the number of rounds, 294 because this affects the *relative* time that is required for trust to be estab-295 lished. The results are presented in Figure 4. First, we discuss the cases 296 on the left column, where repeated interactions are short (expected num-297 ber of rounds r = 20). The top left panel of Figure 4 shows that in such 298 conditions, TUC is successful for medium values of the importance of the 299 game parameter. TUC is also the most frequent strategy for a large range of 300 the importance of the game parameter (note that the results presented are 301 on a logarithmic scale). When the importance of the game is very low e.g. 302 $\gamma = 0.1$, the most frequent strategy is AllD. In this condition, the opportu-303 nity cost is too high relative to the benefit provided by cooperation for either 304 of the conditionally cooperative strategies, TUC or TFT, to thrive. When 305 the importance of the game is very high, e.g. $\gamma = 1000$, TUC is almost never 306 observed and TUD is, by far, the most frequent strategy. When the impor-307 tance of game is high, defecting while the other player cooperates provides 308 a huge benefit. AllD gets this benefit on the first round played with AllC, 309 TFT and TUC. On the other hand, TUD obtains this advantageous payoff 310 at least on the round after trust is established when interacting with TUC 311 and TFT. This advantage by TUD is hard to recover through reciprocity if 312

³It is noteworthy that we compare the overall cooperation in our model to a baseline model that includes AllC, AllD and TFT. That is, there are three out of five cooperative strategies in our model, in comparison to two out of three in the baseline model. Thus, under neutrality (i.e. when all strategies have the same strategies, when $\beta \rightarrow 0$), it would be 60% cooperation vs 66.6% cooperation which is not in favour of our model.



Figure 4: Top: Frequency of strategies as a function of the number of rounds r and importance of the game γ (logarithmic scale); Bottom: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the number of rounds r and importance of the game γ (logarithmic scale). For clarity, the difference in frequency of cooperation is shaded in green when positive and red when negative.

the number of rounds is not sufficiently high. It is noteworthy that β and 313 the game importance parameter γ do not have the same effect. The former 314 scales the whole fitness function, while the latter only scales the entries of 315 the PD payoff matrix. Thus, β also scales the opportunity cost ϵ . A supple-316 mentary figure in appendix B shows that a higher β steepens the relationship 317 between opportunity cost and frequencies or cooperation. In addition, a high 318 intensity of selection leads to trust evolving only for a low opportunity cost. 319 However, beside this expected effect, the qualitative results remain similar 320 for a wide range of reasonable values of β (0.05 to 1). 321

This result is dependent of the length of the interactions. The top part 322 of Figure 4 shows that a higher number of rounds r leads to (i) a higher 323 frequency of TUC and (ii) the prevalence of TUC for a wider range of im-324 portance of game γ . TUC remains the most frequent strategy even when 325 the importance of the game is high if the interactions are sufficiently long. 326 This is because the high number of rounds where both individuals cooperate 327 make up for the few initial rounds where TUC is exploited by TUD (and on 328 a lesser extent, AllD). 329

The bottom part of Figure 4 shows that the presence of trust-based strate-330 gies increases the frequency of cooperation for all conditions examined. The 331 highest frequency of cooperation is obtained for long interactions and high 332 importance of the game. As shown by the similar shape of the curves, the 333 higher frequency of cooperation appears to result from the high frequency 334 of TUC. There is one notable exception. As shown in the bottom left figure 335 (low r and high γ), the presence of trust based strategies also increases coop-336 eration when TUC is not present. This is because TUD strategies cooperate 337 more (for θ rounds) than AllD strategies which never cooperate. 338

In conclusion, trust is favoured for long-term interactions and can be observed on a wide range of importance of the game. The presence of trustbased strategies increases the frequency of cooperation for the whole set of parameter values studied.

343 3.3. Trustfulness and TUD

We have seen from the above results that trust-based cooperators are vulnerable to exploitation by TUD players, which are specifically tailored to take advantage of unconditional trust. This vulnerability was limited so far as we considered a rather careful truster with a p = 0.25. We now look at what is the effect of the probability of checking p on the success of TUC and the frequency of cooperation. For clarity, we present the result as a function



Figure 5: Top: Frequency of strategies as a function of the opportunity cost ϵ and trustfulness 1/p (average number of rounds between checking event). Bottom: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the opportunity cost ϵ and trustfulness 1/p (average number of rounds between checking event). For clarity, the difference in frequency of cooperation is shaded in green when positive and red when negative.

of 1/p, which approximates the trustfulness (which is larger for a smaller probability of checking) of TUC on the overall game, rather than p, which represents the carefulness of TUC on a single round.

The top part of Figure 5 first confirms that it is important for TUC's 353 success to continue checking after trust is reached as TUC is much less fre-354 quent for a high value of trustfulness (i.e high 1/p). If TUC is too trustful, 355 the game is either dominated by TFT when the opportunity cost is small, by 356 TUD when the opportunity cost is intermediate, and and AllD when the op-357 portunity cost is high. There is an intermediate optimal trustfulness 1/p at 358 which TUC is the most frequent strategy (except for zero opportunity costs 359 where the lowest trustfulness and the highest probability of checking is the 360 best strategy, which is equivalent to TFT). On the one hand, low trustful-361 ness makes TUC less successful because TUC checks its partner often and so 362 pays a higher opportunity cost. On the other hand, high trustfulness makes 363 TUC vulnerable to exploitation by TUD for a longer number of rounds. The 364 results show that there can be an optimal level of trust resulting from this 365 trade-off. 366

The bottom part of Figure 5 shows that the presence of trust-based strate-367 gies increases the frequency of cooperation when the opportunity cost is mod-368 erate or high. This cooperation improvement is the highest for the optimal 369 trustfulness at which TUC is very frequent. Again, the presence of trust-370 based strategies can lead to an increase in the frequency of cooperation even 371 if they are not the most frequent strategy e.g. for very high opportunity costs 372 ϵ . Unlike previously, the results also show that the presence of trust-based 373 strategies can reduce the frequency of cooperation. This happens when the 374 opportunity cost ϵ is low and the trustfulness 1/p is high. In these con-375 ditions, trustful and careless TUC players get exploited by TUD players, 376 which increases the frequency of TUD, making cooperation a less viable op-377 tion (evolutionarily). In the absence of trust-based strategies, TFT is careful 378 enough to avoid this pitfall. 379

To conclude, unconditional trust is a viable strategy only in limited conditions and how much TUC relies on trust can have significant effect on the success of the strategy.

383 4. Discussion

Trust is a commonly observed mechanism in human interactions, and discussions on the role of trust are being extended to social interactions between

humans and intelligent machines (Andras et al., 2018). It is therefore impor-386 tant to understand how people behave when interacting with those machines; 387 particularly, whether and when they might exhibit trust behaviour towards 388 them? Answering these questions is crucial for providing suitable designs 389 of mechanisms or infrastructures to facilitate human-intelligent machine in-390 teractions, e.g. in engineering pro-sociality in a hybrid society of humans 391 and machines (Paiva et al., 2018). To this end, this paper provides a game 392 theoretic analysis, where we formalised trust as a behavioural strategy and 393 integrated it into an EGT model to study (i) its success in competition with 394 non-trusting strategies and (ii) its effect on the level of cooperation. 395

Our results show first that trust is expected to be a pervasive cooperation 396 enabling strategy. It is a frequent strategy for a large range of parameters, 397 even in the presence of other strategies that are traditionally successful such 398 as unconditional defection and Tit-for-Tat. Second, our results show that 390 trust is a desirable mechanism in social systems because the presence of 400 trust-based strategies increases the level of cooperation for a wide range of 401 parameters. Finally, we show that trust-based cooperators are vulnerable to 402 trust-based defectors, which are specialised to exploit them. However, our 403 results also suggest that a minimum carefulness after trust is reached (low 404 p) strongly limits this vulnerability. 405

Overall, our analysis shows that trust can emerge because it reduces the 406 opportunity costs paid by individuals during interactions. It is a form of 407 cognitive shortcut that, while exposing the player to some risks, can allow 408 individuals to cooperate at lesser cost. If the pitfalls of trust have often been 409 discussed, our results underlie the importance of taking into account both 410 the benefits and the risk that the use of trust involves. Understanding the 411 balance between these two is a first step to optimise the benefits of trust in 412 intelligent machines while limiting the costs. On this line, further work could 413 expand the model to look at different forms of trust based cooperation and 414 defection strategies, how they co-evolve, and how exploitation of trust-based 415 cooperators can be avoided. It is noteworthy that our additional (numerical) 416 analyses have shown that all the observations described above (i.e. in Figures 417 3 - 5) are robust, e.g. for different values of the threshold number of rounds 418 required for trust to be established (i.e. θ) (see Appendix). Moreover, note 419 that in the current model we consider that TUC and TUD have the same 420 θ , which is the worst case scenario for the evolution of TUC (and cooper-421 ation), since it represents the situation where TUD can perfectly recognise 422 when TUC starts trusting a cooperative co-player and therefore becomes less 423

vigilant of exploitation. More realistically, TUD might need to spend extra resources to gather information about TUC (e.g. providers learn about their customers' preferences and behaviours) to determine what is TUC's θ . On the other hand, TUC should not easily reveal or make available their information (that can be used to infer their θ), to better deal with TUD. Future work should address how these aspects might change the outcome of the evolutionary dynamics.

One of the most famous previous formalisations of trust is an experiment 431 from behavioural economics called the trust game (Berg et al., 1995). This 432 game consists of one individual receiving an endowment of money, of which 433 it must choose a certain amount (which can be zero) to send to the other 434 player. The amount sent to the other player is tripled by the experimenter (so 435 that sending money represents an investment). The other player then decides 436 what amount of this money (if any) to send back to the first player (so that 437 there is risk in the first player sending money). While the Nash equilibrium 438 is for the first player to send nothing to the other player, in experiments in-439 dividuals usually deviate from this by sending a positive amount (Berg et al., 440 1995). The amount that the first player sends can be understood as mea-441 suring how much the first player trusts the second to reciprocate. However, 442 in contrast to our formalisation, the trust game measures more a willingness 443 to take risks blindly, as interactions are between anonymous individuals and 444 are played only once. By contrast, we have considered repeated interactions 445 between the same individuals, which has enabled us to look at the success of 446 strategies that build up trust over time. 447

Within the context of the trust game, it has been shown recently that 448 trust and trustworthiness cannot evolve in well-mixed and spatial networks 449 with a homogeneous structure; they can evolve only in heterogeneous net-450 works under highly advantageous conditions (Kumar et al., 2020). Moreover, 451 within an overall grand challenge to understand the evolution of moral be-452 haviour (beyond that of cooperation) (Capraro and Perc, 2018), the role of 453 network topology in promoting honesty has been studied in (Capraro et al., 454 2019), extending works on honest signalling (Smith, 1991). Similarly, ly-455 ing behaviour have recently been looked at within the context of well-mixed 456 populations (Capraro et al., 2020). 457

In line with our approach, trust enabling strategies were previously considered in the context of repeated games (Han et al., 2011), where trust is built over time as a component of a larger decision making process, for prediction of opponents' behaviour. Trust was also considered for enabling co-

operation in a one-shot prisoner's dilemma (Janssen, 2008; McNamara et al., 462 2009), but it was assumed that players can recognise how trustworthy a co-463 player is based on additional cues such as signalling. Our work differs from 464 these approaches in that we consider trust as a cognitive shortcut to avoid 465 deliberation and having to check the outcomes of previous interaction(s), 466 thereby limiting the opportunity cost of conditional strategies. More gener-467 ally, the role of an opportunity cost of monitoring the action of a co-player on 468 the equilibrium level of cooperation has been studied in classic game theory 469 models (for instance, see Lehrer and Solan (2018)). Using an evolutionary 470 game theory approach, we complement this literature by showing that trust-471 based strategies are likely to emerge to deal with the cost of monitoring, even 472 when players are short-sighted and only care about their immediate payoffs. 473 We show conditions under which the presence of trust-based strategies can 474 promote a high level of cooperation in comparison to the case where trust-475 based strategies are not available, e.g. where only classic reciprocal strategies 476 such as TFT are possible. 477

In addition, trust has been used extensively in various computerised sys-478 tems, such as in multi-agent open and distributed systems, to facilitate 479 agents' interactions. Agents may have limited computational and storage 480 capabilities that restrict their control over interactions, and trust is used 481 to minimise uncertainty associated with the interactions, especially when 482 agents inhabit in uncertain and constantly changing environments (Ram-483 churn et al., 2004; Falcone and Castelfranchi, 2001). This is the case for vari-484 ous applications including peer-to-peer computing, smart-grids, e-commerce, 485 etc (Kamhoua et al., 2011; Ramchurn et al., 2004; Papadopoulou et al., 2001; 486 Petruzzi et al., 2014; Brooks et al., 2020). These studies utilise trust for the 487 purpose of regulating individual and collective behaviours, formalising dif-488 ferent aspects of trust (such as reputation and belief) (Castelfranchi, 1997; 489 Castelfranchi and Falcone, 2010). Our results and approach provide novel 490 insights into the design of such computerised and hybrid systems as these 491 require trust to ensure high levels of cooperation or efficient collaboration 492 within a group or team of agents, including human-machine hybrid interac-493 tions. For instance, our results show that the importance of the business 494 at hand (relative to the opportunity cost) needs to be taken into account 495 to ensure a desired level of cooperation. Also, the system needs to be de-496 signed so that the opportunity cost of verifying the actions of an intelligent 497 machine is sufficiently low (relative to the benefit and cost of the game) to 498 enable a long-term trusting relationship with customers, e.g. making the 490

activities transparent either directly to the user or to expert auditors that follow professional codes of ethics (Andras et al., 2018).

In the current work, since our goal was to explore the effect of trust-502 based strategies and a non-trivial opportunity cost in the context of human-503 intelligent machine interactions, we have based our analysis on a baseline 504 model of IPD with three strategies (i.e. AllC, AllD and TFT), as described 505 (Imhof et al., 2005a). There are other important strategies in this context, 506 such as win-stay-lose-shift, grim and generous TFT, which are particularly 507 relevant if errors in players' behavioural implementation is taken into account 508 (Nowak and Sigmund, 1993; Imhof et al., 2007; Sigmund, 2010). For example, 509 forgiveness is an important mechanism to deal with such errors, e.g. to 510 resolve conflicts and avoid long-term retaliation in a long-term relationships. 511 We will explore how trust-based strategies can be enhanced with forgiveness, 512 as for instance errors might lead to difficulty in building initial trust and/or 513 destroying built mutual trust not on purpose, and thus more forgiving trust-514 based strategies might better promote cooperation. On the other hand, these 515 more forgiving strategies might be subject to more exploitation. In general, 516 it is important to investigate a larger space of strategic behaviours in the 517 context of IPD as it might influence the outcome of evolutionary dynamics. 518

An assumption made in our work is that the mutation or behavioural 519 exploration is rare (Sigmund, 2010; Traulsen et al., 2006), allowing us to 520 conveniently calculate the long-term frequencies (i.e. stationary distribution) 521 of the strategies in the population. In reality, the mutation rate might be non-522 negligible and might have an effect on the evolutionary dynamics (Traulsen 523 et al., 2009; Rand et al., 2013; Duong and Han, 2019). In general, larger 524 mutation rates add more randomness to the system dynamics and might 525 enable cooperation in situations where it is difficult to evolve otherwise, and 526 vice versa (Hauert et al., 2007; Han et al., 2012; Rand et al., 2013; García 527 and Traulsen, 2012). We aim to study the effect of mutation in future work. 528

In the current work we have focused on the prisoner's dilemma as it repre-529 sents the hardest (pairwise) scenario for cooperation to emerge. Many other 530 scenarios might be represented using other social dilemmas such as coordi-531 nation or snowdrift games (Santos et al., 2006; Sigmund, 2010). Considering 532 such games where it is easier for cooperation to emerge has the potential to 533 open new windows of opportunity for long-term trust-based relationships to 534 be established. Our future work will study how trust-based strategies (as we 535 have modelled) evolve in the context of other social dilemmas. Moreover, 536 given the importance of population structures in the emergence of trust and 537

trustworthiness in the context of the trust game (Kumar et al., 2020), our 538 future work will examine how different population structures influence the 539 outcome of trustful behaviours in our context. Finally, we have assumed that 540 agents always pay the cost of checking, but an alternative is that, they might 541 choose not to check when it is too difficult or costly to do so (for example, 542 checking if an AI development company complies with safety requirements in 543 the development process within a competition to reach technology supremacy 544 (Han et al., 2020)). 545

546 5. Conclusion

We have demonstrated in this paper that evolutionary game theory pro-547 vides a valuable framework to study trust. Social interactions often result 548 in complex dynamics with unexpected consequences, which a quantitative 549 model is able to shed light on. Our model provides formal support for the 550 theory that trust is a cognitive shortcut which people use to reduce the com-551 plexity of their interactions. The results of the model provide new insights 552 into the questions of whether and when humans might trust intelligent ma-553 chines, generating reasonable behavioural hypotheses that empirical studies 554 can test. 555

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560 References

- ⁵⁶¹ Akerlof, G. (1970). The market for 'lemons': Quality uncertainty and the ⁵⁶² market mechanism. *quarterly Journal of Economics*, 84(3):488–500.
- Andras, P., Esterle, L., Guckert, M., Han, T. A., Lewis, P. R., Milanovic,
 K., Payne, T., Perret, C., Pitt, J., Powers, S. T., Urquhart, N., and Wells,
 S. (2018). Trusting Intelligent Machines: Deepening Trust Within SocioTechnical Systems. *IEEE Technology and Society Magazine*, 37(4):76–83.
- Axelrod, R. (1984). The Evolution of Cooperation. Basic Books, ISBN 0 465-02122-2.

- Axelrod, R. and Hamilton, W. (1981). The evolution of cooperation. Science,
 211:1390–1396.
- Beldad, A., Hegner, S., and Hoppen, J. (2016). The effect of virtual sales
 agent (VSA) gender product gender congruence on product advice credibility, trust in VSA and online vendor, and purchase intention. *Computers*
- in Human Behavior, 60:62–72.
- Berg, J., Dickhaut, J., and McCabe, K. (1995). Trust, reciprocity, and social
 history. *Games and Economic Behavior*, 10:122–142.
- Brooks, N. A., Powers, S. T., and Borg, J. M. (2020). A mechanism to
 promote social behaviour in household load balancing. *Artificial Life Con- ference Proceedings*, 32:95–103.
- Capraro, V. and Perc, M. (2018). Grand challenges in social physics: In
 pursuit of moral behavior. *Frontiers in Physics*, 6:107.
- ⁵⁸² Capraro, V., Perc, M., and Vilone, D. (2019). The evolution of ly⁵⁸³ ing in well-mixed populations. *Journal of the Royal Society Interface*,
 ⁵⁸⁴ 16(156):20190211.
- Capraro, V., Perc, M., and Vilone, D. (2020). Lying on networks: The
 role of structure and topology in promoting honesty. *Physical Review E*, 101(3):032305.
- Castelfranchi, C. (1997). Modeling social action for AI agents. IJCAI International Joint Conference on Artificial Intelligence, 2(c):1567–1576.
- Castelfranchi, C. and Falcone, R. (2010). Trust theory: A socio-cognitive and
 computational model, volume 18. John Wiley & Sons.
- ⁵⁹² Chattaraman, V., Kwon, W.-S., and Gilbert, J. E. (2012). Virtual agents
 ⁵⁹³ in retail web sites: Benefits of simulated social interaction for older users.
 ⁵⁹⁴ Computers in Human Behavior, 28(6):2055–2066.
- ⁵⁹⁵ Chung, H., Iorga, M., Voas, J., and Lee, S. (2017). Alexa, can i trust you?
 ⁵⁹⁶ Computer, 50(9):100–104. Conference Name: Computer.
- ⁵⁹⁷ Dahlstrom, R., Nygaard, A., Kimasheva, M., and M. Ulvnes, A. (2014).
 ⁵⁹⁸ How to recover trust in the banking industry? A game theory approach

- to empirical analyses of bank and corporate customer relationships. *International Journal of Bank Marketing*, 32(4):268–278. Publisher: Emerald Group Publishing Limited.
- ⁶⁰² Dasgupta, P. (2000). Trust as a commodity. *Trust: Making and breaking* ⁶⁰³ *cooperative relations*, 4:49–72.
- ⁶⁰⁴ Duong, M. H. and Han, T. A. (2019). On equilibrium properties of the ⁶⁰⁵ replicator-mutator equation in deterministic and random games. *Dynamic* ⁶⁰⁶ *Games and Applications*, pages 1–23.
- Falcone, R. and Castelfranchi, C. (2001). Social trust: A cognitive approach.
 In *Trust and deception in virtual societies*, pages 55–90. Springer.
- Fernández Domingos, E. (2020). Egttools: Toolbox for evolutionary game
 theory. https://github.com/Socrats/EGTTools.
- Fudenberg, D. and Maskin, E. (1986). The folk theorem in repeated games
 with discounting or with incompete information. *Econometrica*, 54:533–
 554.
- García, J. and Traulsen, A. (2012). The structure of mutations and the evolution of cooperation. *PloS one*, 7(4):e35287.
- Garcia, J. and van Veelen, M. (2018). No strategy can win in the repeated
 prisoner's dilemma: linking game theory and computer simulations. *Fron*-*tiers in Robotics and AI*, 5:102.
- ⁶¹⁹ Glynatsi, N. and Knight, V. (2020). Using a theory of mind to find best ⁶²⁰ responses to memory-one strategies. *Scientific Reports*, 17287:10.
- Grabner-Kraeuter, S. (2002). The role of consumers' trust in online-shopping.
 Journal of Business Ethics, 39(1):43–50.
- Han, T. A. (2013). Intention recognition, commitment and their roles in the
 evolution of cooperation: From Artificial intelligence techniques to evolu tionary game theory models. Springer SAPERE, vol. 9.
- Han, T. A., Moniz Pereira, L., and Santos, F. C. (2011). Intention recognition
 promotes the emergence of cooperation. *Adaptive Behavior*, 19(4):264–279.

- Han, T. A., Pereira, L. M., and Santos, F. C. (2012). The emergence of commitments and cooperation. In *Proceedings of the 11th International Con- ference on Autonomous Agents and Multiagent Systems (AAMAS'2012)*,
 pages 559–566. ACM.
- Han, T. A., Pereira, L. M., Santos, F. C., and Lenaerts, T. (2013a). Good
 agreements make good friends. *Scientific reports*, 3:2695.
- Han, T. A., Pereira, L. M., Santos, F. C., and Lenaerts, T. (2013b). Why is
 it so hard to say sorry? evolution of apology with commitments in the iterated prisoner's dilemma. In *Proceedings of the Twenty-Third international joint conference on Artificial Intelligence*, pages 177–183.
- Han, T. A., Pereira, L. M., Santos, F. C., and Lenaerts, T. (2020). To Regulate or Not: A Social Dynamics Analysis of an Idealised AI Race. *Journal of Artificial Intelligence Research, pre-print available at arXiv:1907.12393*.
 In Press.
- Hauert, C., Traulsen, A., Brandt, H., Nowak, M. A., and Sigmund, K. (2007).
 Via freedom to coercion: the emergence of costly punishment. *science*, 316(5833):1905–1907.
- Hilbe, C., Martinez-Vaquero, L. A., Chatterjee, K., and Nowak, M. A. (2017).
 Memory-n strategies of direct reciprocity. *Proceedings of the National Academy of Sciences*, 114(18):4715–4720.
- Ho, T.-H. (1996). Finite automata play repeated prisoner's dilemma with
 information processing costs. Journal of economic dynamics and control,
 20(1-3):173-207.
- Imhof, L. A., Fudenberg, D., and Nowak, M. A. (2005a). Evolutionary cycles
 of cooperation and defection. *Proceedings of the National Academy of Sciences of the United States of America*, 102(31):10797–10800.
- Imhof, L. A., Fudenberg, D., and Nowak, M. A. (2005b). Evolutionary cycles
 of cooperation and defection. *Proceedings of the National Academy of Sciences of the United States of America*, 102:10797–10800.
- Imhof, L. A., Fudenberg, D., and Nowak, M. A. (2007). Tit-for-tat or winstay, lose-shift? *Journal of Theoretical Biology*, 247(3):574 – 580.

Janssen, M. A. (2008). Evolution of cooperation in a one-shot prisoner's
 dilemma based on recognition of trustworthy and untrustworthy agents.
 Journal of Economic Behavior & Organization, 65(3-4):458-471.

⁶⁶² Jugovac, M. and Jannach, D. (2017). Interacting with Recom-⁶⁶³ menders:Overview and research directions. *ACM Transactions on Inter-*⁶⁶⁴ *active Intelligent Systems*, 7(3):10:1–10:46.

Kamhoua, C. A., Pissinou, N., and Makki, K. (2011). Game theoretic modeling and evolution of trust in autonomous multi-hop networks: Application
to network security and privacy. In 2011 IEEE International Conference
on Communications (ICC), pages 1–6. IEEE.

- Karlin, S. and Taylor, H. E. (1975). A First Course in Stochastic Processes.
 Academic Press, New York.
- Kumar, A., Capraro, V., and Perc, M. (2020). The evolution of trust and
 trustworthiness. *Journal of the Royal Society Interface*, 17(169):20200491.

Laaksonen, T., Jarimo, T., and Kulmala, H. I. (2009). Cooperative strategies
in customer–supplier relationships: The role of interfirm trust. *International Journal of Production Economics*, 120(1):79–87.

- Lehrer, E. and Solan, E. (2018). High frequency repeated games with costly monitoring. *Theoretical Economics*, 13(1):87–113.
- Lewis, G. (2011). Asymmetric information, adverse selection and online disclosure: The case of eBay Motors. American Economic Review,
 101(4):1535-1546.
- ⁶⁸¹ Luhmann, N. (1979). Trust and Power. John Wiley & Sons, Chichester.
- Macy, M. W. and Flache, A. (2002). Learning dynamics in social dilemmas.
 Proceedings of the National Academy of Sciences of the United States of America, 99:7229–7236.
- Mahadevan, B. (2000). Business models for internet-based e-commerce: An
 anatomy. *California Management Review*, 42(4):55–69. Publisher: SAGE
 Publications Inc.

- Martinez-Vaquero, L. A., Han, T. A., Pereira, L. M., and Lenaerts, T. (2015).
 Apology and forgiveness evolve to resolve failures in cooperative agree ments. *Scientific reports*, 5:10639.
- Maynard Smith, J. (1982). Evolution and the Theory of Games. Cambridge
 University Press, Cambridge, UK.
- McNally, L., Brown, S. P., and Jackson, A. L. (2012). Cooperation and the
 evolution of intelligence. *Proceedings of the Royal Society B: Biological Sciences*, 279(1740):3027–3034.
- McNamara, J. M., Stephens, P. A., Dall, S. R., and Houston, A. I. (2009).
 Evolution of trust and trustworthiness: social awareness favours personality differences. *Proceedings of the Royal Society B: Biological Sciences*, 276(1657):605–613.
- Nass, C. and Moon, Y. (2000). Machines and mindlessness: Social responses
 to computers. *Journal of Social Issues*, 56(1):81–103.
- Nowak, M. A. and Sigmund, K. (1993). A strategy of win-stay, lose-shift
 that outperforms tit-for-tat in prisoner's dilemma. *Nature*, 364:56–58.
- Nunes, I. and Jannach, D. (2017). A systematic review and taxonomy of
 explanations in decision support and recommender systems. User Modeling
 and User-Adapted Interaction, 27(3):393-444.
- Paiva, A., Santos, F. P., and Santos, F. C. (2018). Engineering pro-sociality
 with autonomous agents. In *Thirty-second AAAI conference on artificial intelligence*.
- Papadopoulou, P., Andreou, A., Kanellis, P., and Martakos, D. (2001). Trust
 and relationship building in electronic commerce. *Internet research*.
- Petruzzi, P. E., Busquets, D., and Pitt, J. (2014). Experiments with social capital in multi-agent systems. In Dam, H. K., Pitt, J., Xu, Y., Governatori, G., and Ito, T., editors, *PRIMA 2014: Principles and Practice of Multi-Agent Systems*, Lecture Notes in Computer Science, pages 18–33, Cham. Springer International Publishing.
- ⁷¹⁷ Pu, P. and Chen, L. (2007). Trust-inspiring explanation interfaces for rec-⁷¹⁸ ommender systems. *Knowledge-Based Systems*, 20(6):542–556.

- Ramchurn, S. D., Huynh, D., and Jennings, N. R. (2004). Trust in multi-agent systems. *The Knowledge Engineering Review*, 19(1):1–25.
- Rand, D. G., Tarnita, C. E., Ohtsuki, H., and Nowak, M. A. (2013). Evolution of fairness in the one-shot anonymous ultimatum game. *Proceedings of the National Academy of Sciences*, 110(7):2581–2586.
- Santos, F. C., Pacheco, J. M., and Lenaerts, T. (2006). Evolutionary dynam ics of social dilemmas in structured heterogeneous populations. *Proceed- ings of the National Academy of Sciences of the United States of America*,
 103:3490–3494.
- Santos, F. P., Pacheco, J. M., Paiva, A., and Santos, F. C. (2019). Evolution of collective fairness in hybrid populations of humans and agents. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 33, pages 6146–6153.
- Shoham, Y. (2008). Computer science and game theory. Communications of
 the ACM, 51(8):74–79.
- ⁷³⁴ Sigmund, K. (2010). *The Calculus of Selfishness*. Princeton University Press.
- Smith, J. M. (1991). Honest signalling: the philip sidney game. Animal
 Behaviour.
- Traulsen, A., Hauert, C., De Silva, H., Nowak, M. A., and Sigmund, K.
 (2009). Exploration dynamics in evolutionary games. *Proceedings of the National Academy of Sciences*, 106(3):709–712.
- Traulsen, A., Nowak, M. A., and Pacheco, J. M. (2006). Stochastic dynamics
 of invasion and fixation. *Phys. Rev. E*, 74:11909.
- Wooldridge, M. (2009). An introduction to multiagent systems. John Wiley & Sons.
- Yoo, K.-H., Gretzel, U., and Zanker, M. (2012). Persuasive Recommender
 Systems: Conceptual Background and Implications. Springer Publishing
 Company, Incorporated, 1st edition.

747 Competing interests statement

The authors have not competing interests.

750 Author contributions

- ⁷⁵¹ The Anh Han: Conceptualization, Methodology, Formal Analysis, Writing
- 752 Original draft preparation
- 753 Cedric Perret: Conceptualization, Methodology, Formal Analysis, Soft-
- 754 ware, Writing Original draft preparation
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- 756 draft preparation

757

758 Appendices

759 Appendix A: Results for different trust threshold θ



Figure 6: Left: Frequency of strategies as a function of the opportunity cost ϵ . Right: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the opportunity cost ϵ . The difference in frequency of cooperation between the two scenario is shaded in green when positive and red when negative. Each results are presented for different trust threshold $\theta = 5$ and $\theta = 10$. Parameters: $\beta = 0.1$, N = 100, $\gamma = 1$, r = 50, p = 0.25, R = 1, S = -1, T = 2, P = 0.





Figure 7: Top: Frequency of strategies as a function of the number of rounds r and importance of the game γ (logarithmic scale); Bottom: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the number of rounds r and importance of the game γ (logarithmic scale). For clarity, the difference in frequency of cooperation is shaded in green when positive and red when negative. Each results are presented for different trust threshold $\theta = 5$ and $\theta = 10$. Parameters: $\beta = 0.1$, $N \Im 100$, p = 0.25, R = 1, S = -1, T = 2, P = 0.

Trust threshold $\theta = 5$



Figure 8: Top: Frequency of strategies as a function of the opportunity cost ϵ and trustfulness 1/p (average number of rounds between checking event). Bottom: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the opportunity cost ϵ and trustfulness 1/p (average number of rounds between checking event). For clarity, the difference in frequency of cooperation is shaded in green when positive and red when negative. Each results are presented for different trust threshold $\theta = 5$ and $\theta = 10$. Parameters: $\beta = 0.1$, N = 100, $\gamma = 1, r = 50$, R = 1, S = -1, T = 2, P = 0.

760 Appendix B: Results for different intensity of selection β



Figure 9: Left: Frequency of strategies as a function of the opportunity cost ϵ . Right: Frequency of cooperation in absence or presence of trust-based strategies TUC and TUD, as a function of the opportunity cost ϵ . The difference in frequency of cooperation between the two scenario is shaded in green when positive and red when negative. Each results are presented for different intensity of selection, from top to bottom $\beta = 0.05$, $\beta = 0.1$ and $\beta = 0.5$. Parameters: N = 100, $\gamma = 1$, r = 50, p = 0.25, R = 1, S = -1, T = 2, P = 0.